

Foregrounds Removal for Spectral Distortion Anisotropies

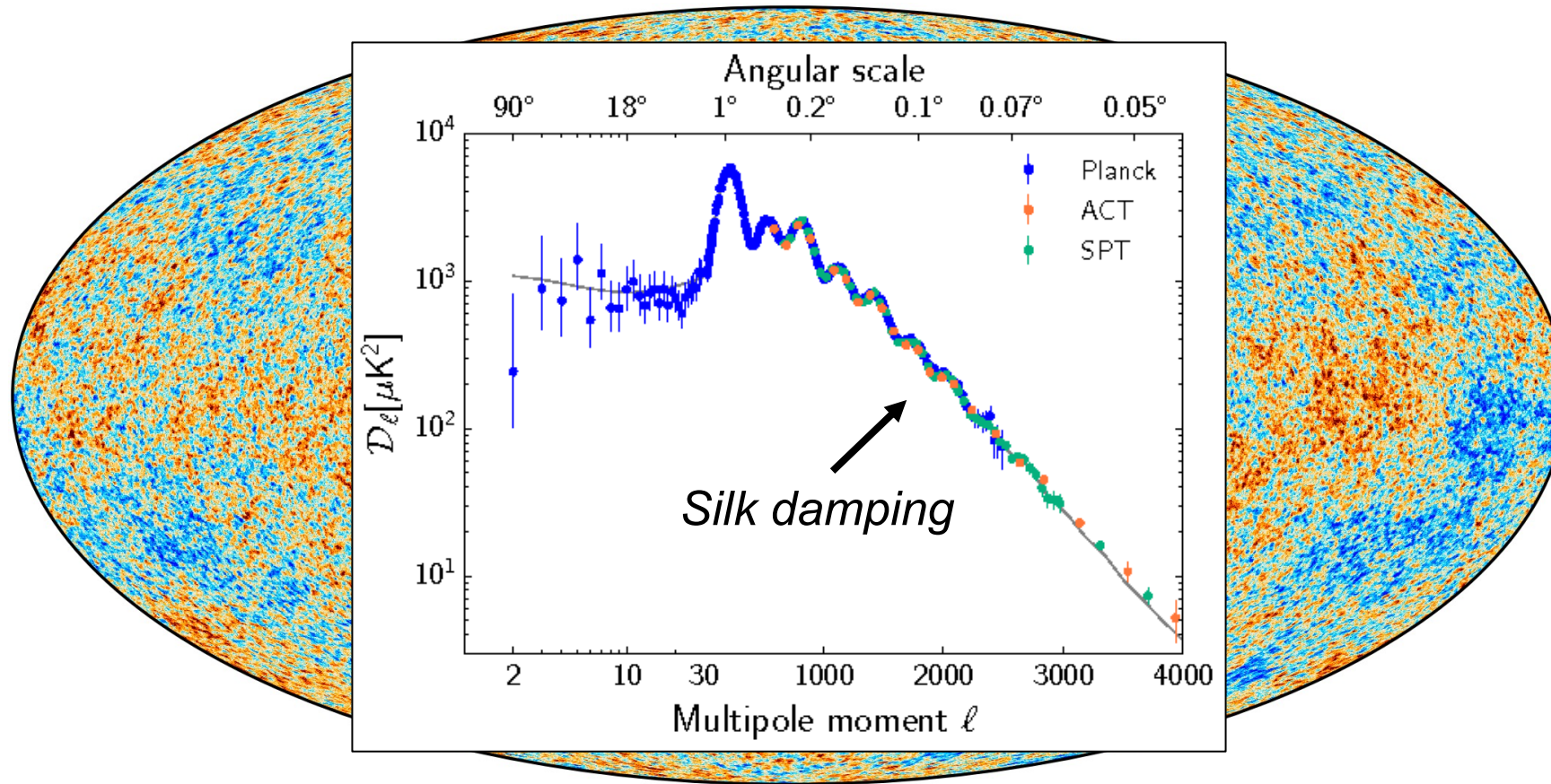
Mathieu Remazeilles



Remazeilles, Ravenni, Chluba, MNRAS 2022

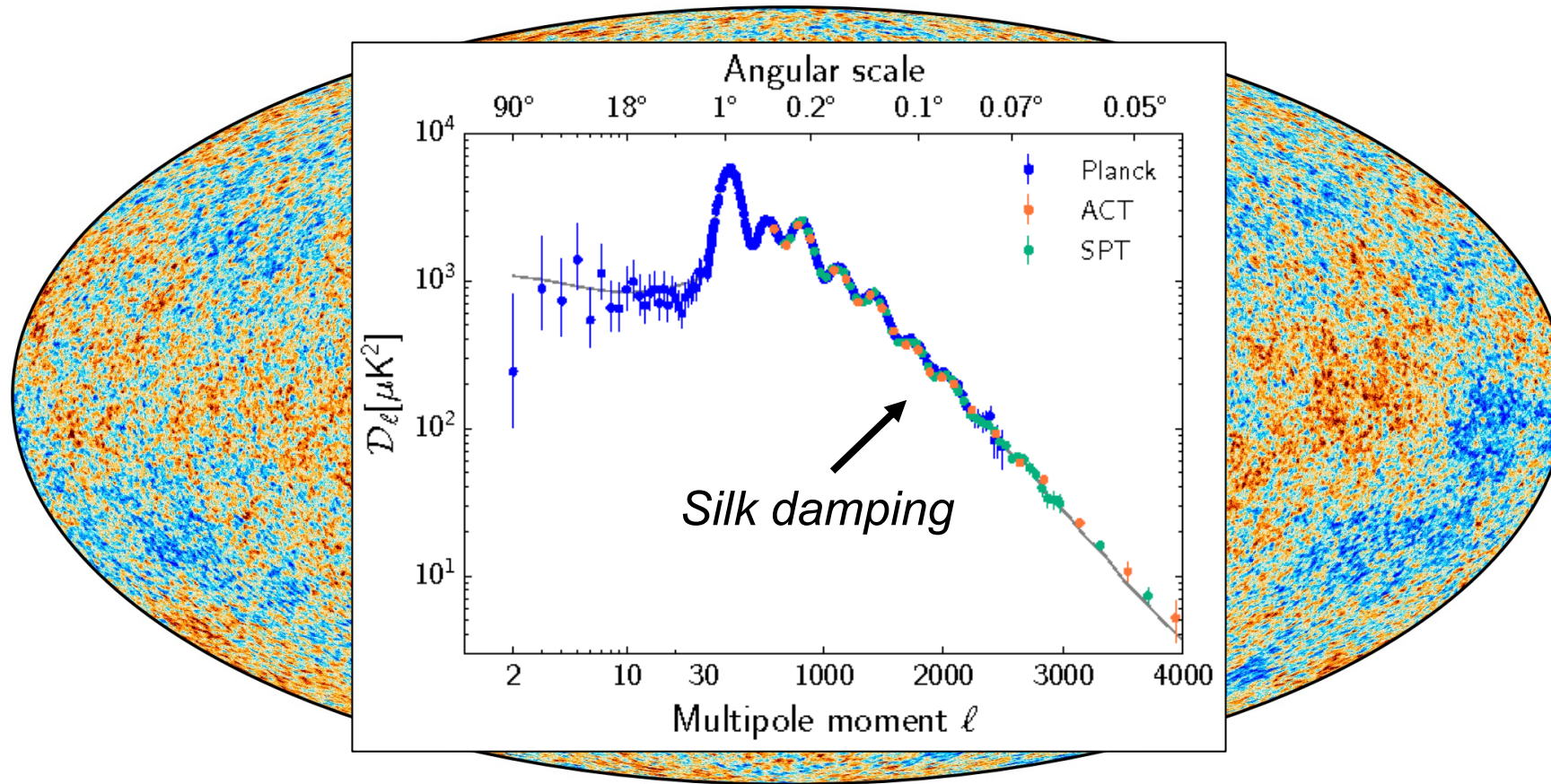
Remazeilles & Chluba, MNRAS 2018

Dissipation of primordial acoustic modes



Photons random-walk out of **overdense/hot** regions towards **underdense/cold** regions, thus uniformizing the temperature and erasing anisotropies at small scales foremost

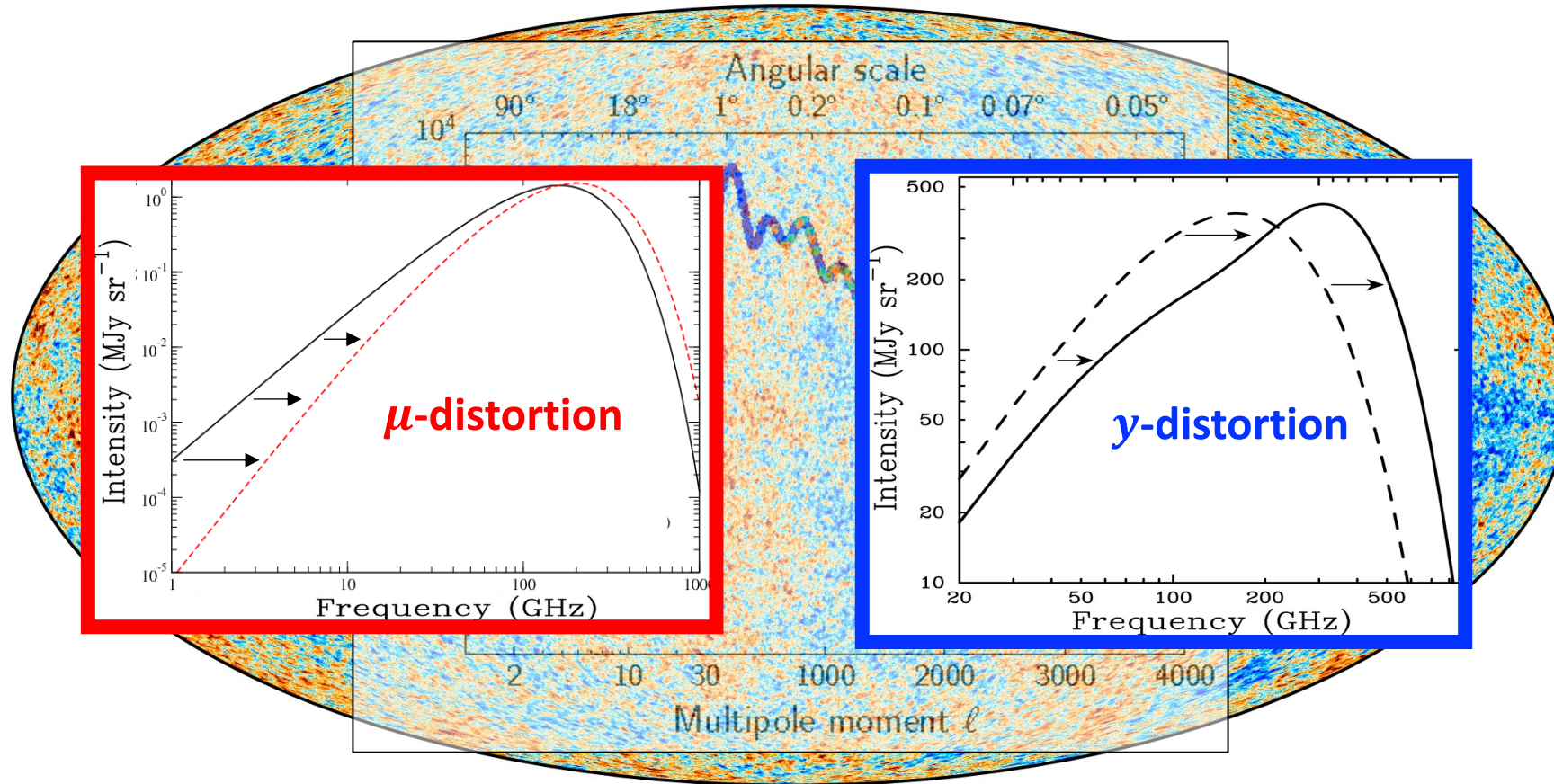
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$\Rightarrow$ mixing blackbodies of different temperatures

Dissipation of primordial acoustic modes



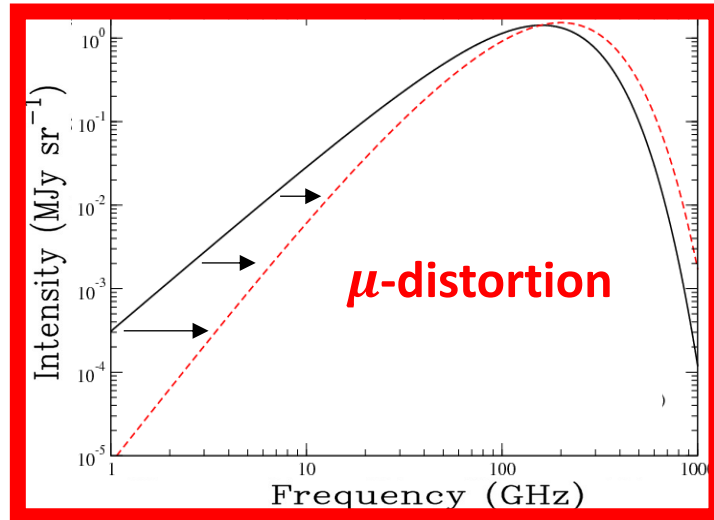
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⇒ mixing blackbodies of different temperatures

CMB spectral distortions

Important at early times

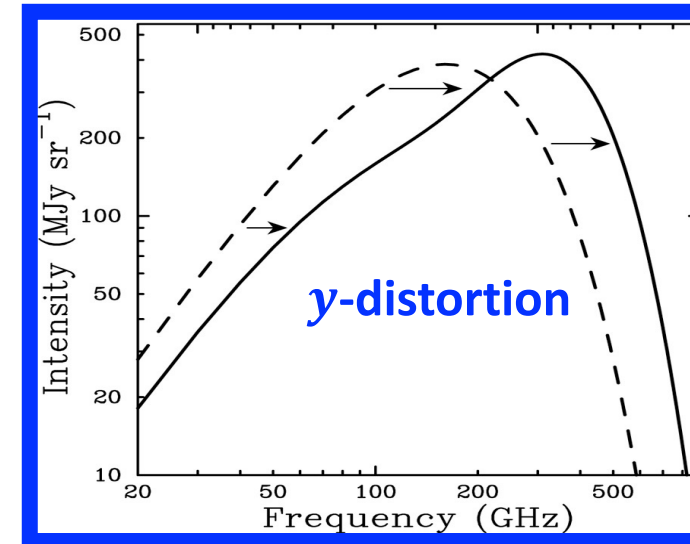
$$z > 10^4$$



Sunyaev & Zeldovich, ApSS (1970)

Important at late times

$$z < 10^4$$

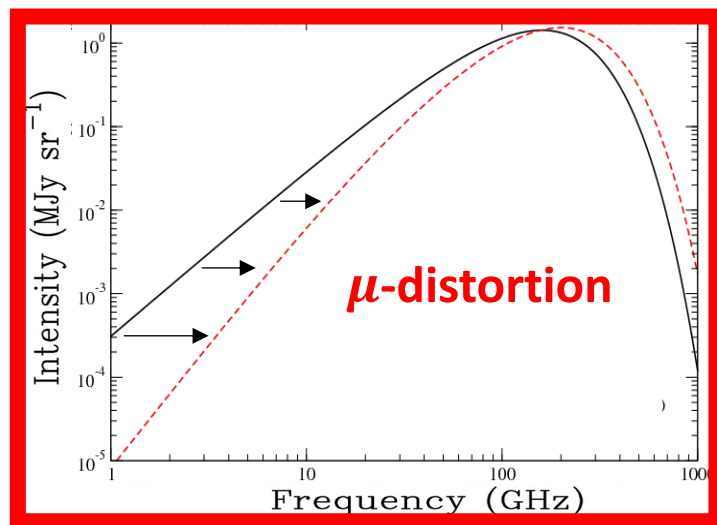


Zeldovich & Sunyaev, ApSS (1969)

CMB spectral distortions

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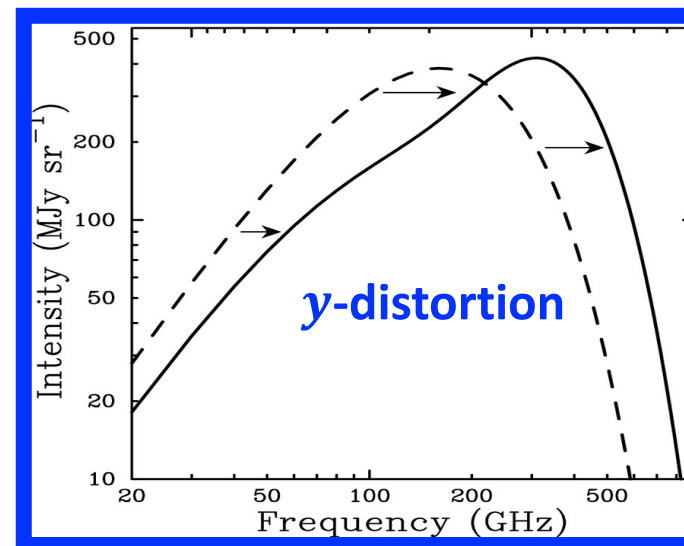
Sunyaev & Zeldovich, ApSS (1970)

$$I_{\nu}^{\text{CMB}} \simeq I_{\nu}^{\text{Planck}} \left(1 + \underbrace{\mu \frac{x e^x}{e^x - 1} \left[\frac{\pi^2}{18\zeta(3)} - \frac{1}{x} \right]}_{\text{spectral signature of } \mu\text{-distortion}} \right)$$

Blackbody

Important at late times

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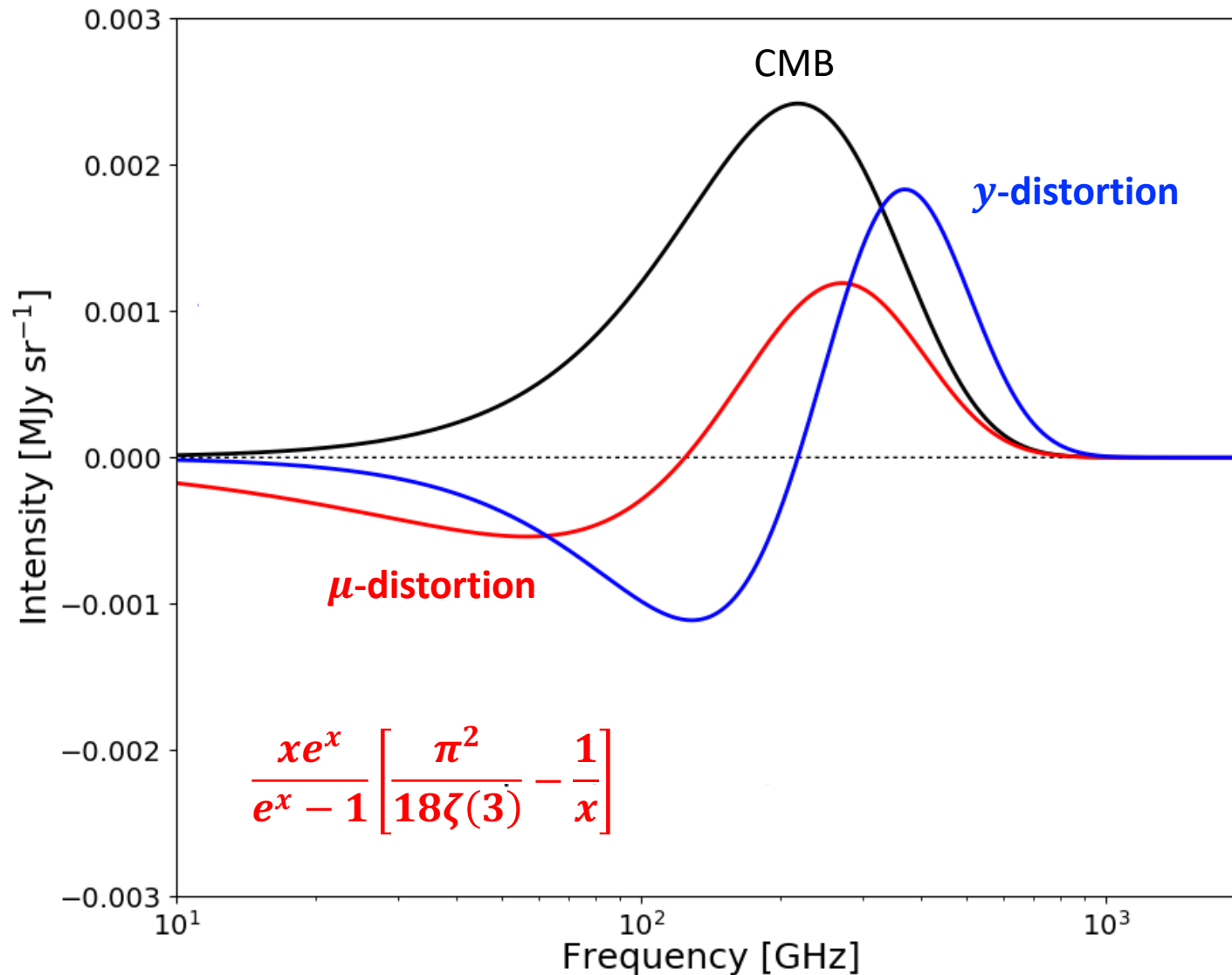
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$$I_{\nu}^{\text{CMB}} \simeq I_{\nu}^{\text{Planck}} \left(1 + \underbrace{y \frac{x e^x}{e^x - 1} \left[x \coth \frac{x}{2} - 4 \right]}_{\text{spectral signature of } y\text{-distortion}} \right)$$

Blackbody

$$x \equiv h\nu/kT$$

Spectral shapes of the distortions

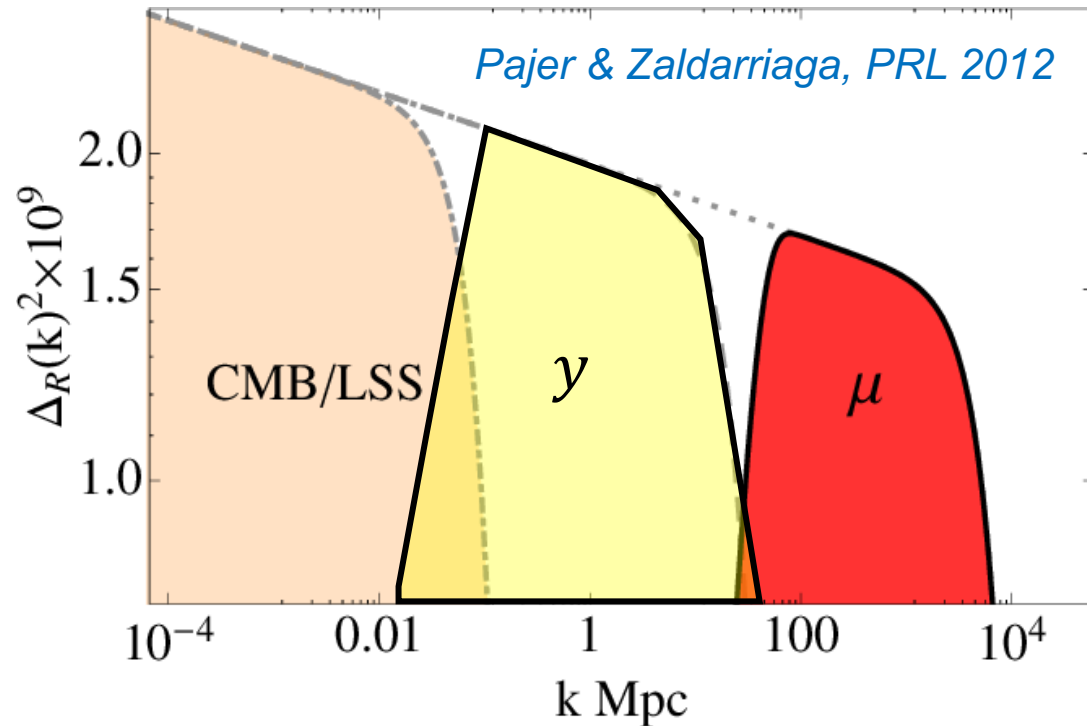


$$\frac{xe^x}{e^x - 1} \left[x \coth \frac{x}{2} - 4 \right]$$

$$\frac{xe^x}{e^x - 1} \left[\frac{\pi^2}{18\zeta(3)} - \frac{1}{x} \right]$$

Spectral distortions probe the primordial power spectrum at very small scales

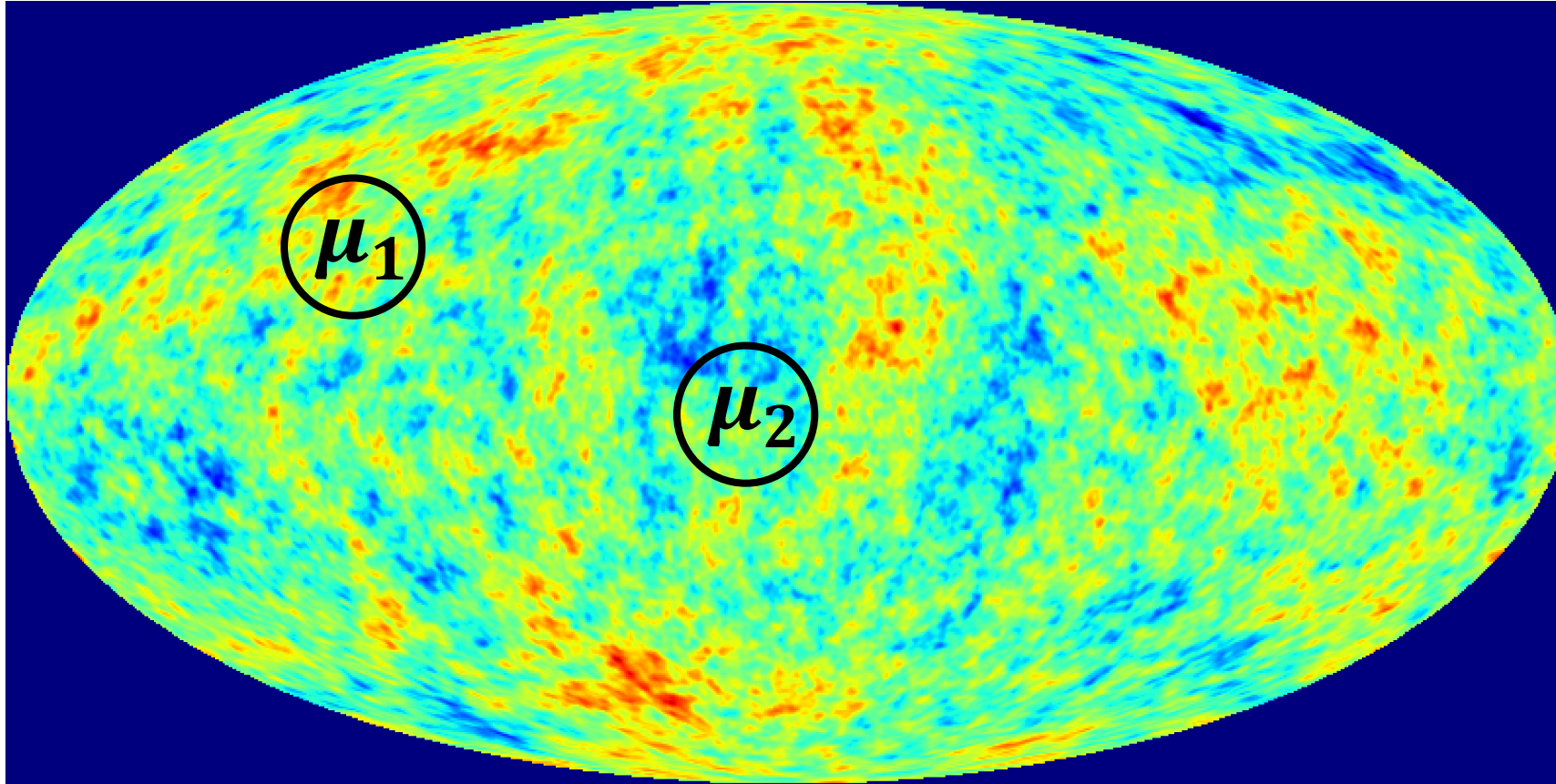
The primordial power spectrum is mostly unknown at scales $k > 3 \text{ Mpc}^{-1}$



- CMB: $k > 0.2 \text{ Mpc}^{-1}$ erased by Silk damping
- LSS: $k > 0.2 \text{ Mpc}^{-1}$ very non-linear
- Spectral distortions can extend our lever arm up to $k \simeq 10^4 \text{ Mpc}^{-1}$ in the linear regime!

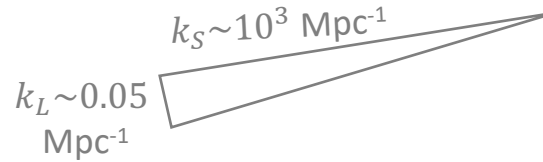
Aside from average distortions...

Anisotropies of spectral distortions from non-Gaussian primordial perturbations



Anisotropic distortions from non-Gaussianity

Local type non-Gaussianity
“ultra squeezed”



Pajer & Zaldarriaga, PRL 2012

Ganc & Komatsu, PRD 2012

Dimastrogiovanni et al JCAP 2016

- ❑ Multi-field inflation and non-Bunch-Davies vacuum models predict sizeable, scale-dependent, non-Gaussianity of the primordial perturbation field
- ❑ Non-gaussian couplings between short- and long-wavelength modes modulate the damping of primordial perturbations across different directions in the sky

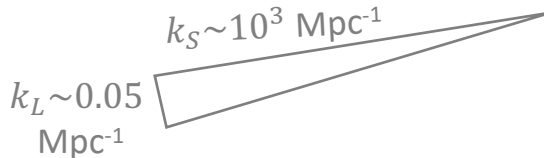
$\Rightarrow$ Anisotropic μ -distortions $\sim C_\ell^{\mu\mu}$

- ❑ Non-gaussian couplings $\Rightarrow$ correlation between CMB temperature and μ -distortion anisotropies!

$$\Rightarrow C_\ell^{\mu T} \simeq f_{\text{NL}}(k \simeq 10^3 \text{ Mpc}^{-1}) \langle \mu \rangle \rho(\ell) C_\ell^{TT, \text{SW}}$$

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⇒ Anisotropic μ - and y -distortions $\sim C_\ell^{\mu\mu}, C_\ell^{yy}$

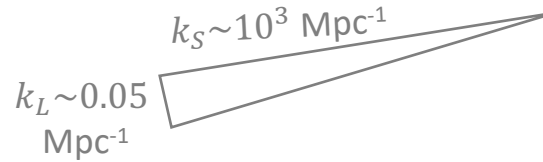
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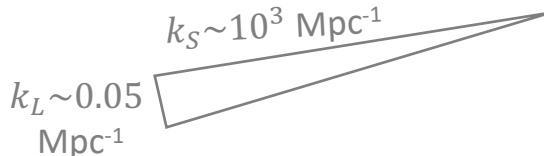
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Enhanced distortion signals by cross-correlation with CMB temperature anisotropies!

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Ganc & Komatsu, PRD 2012

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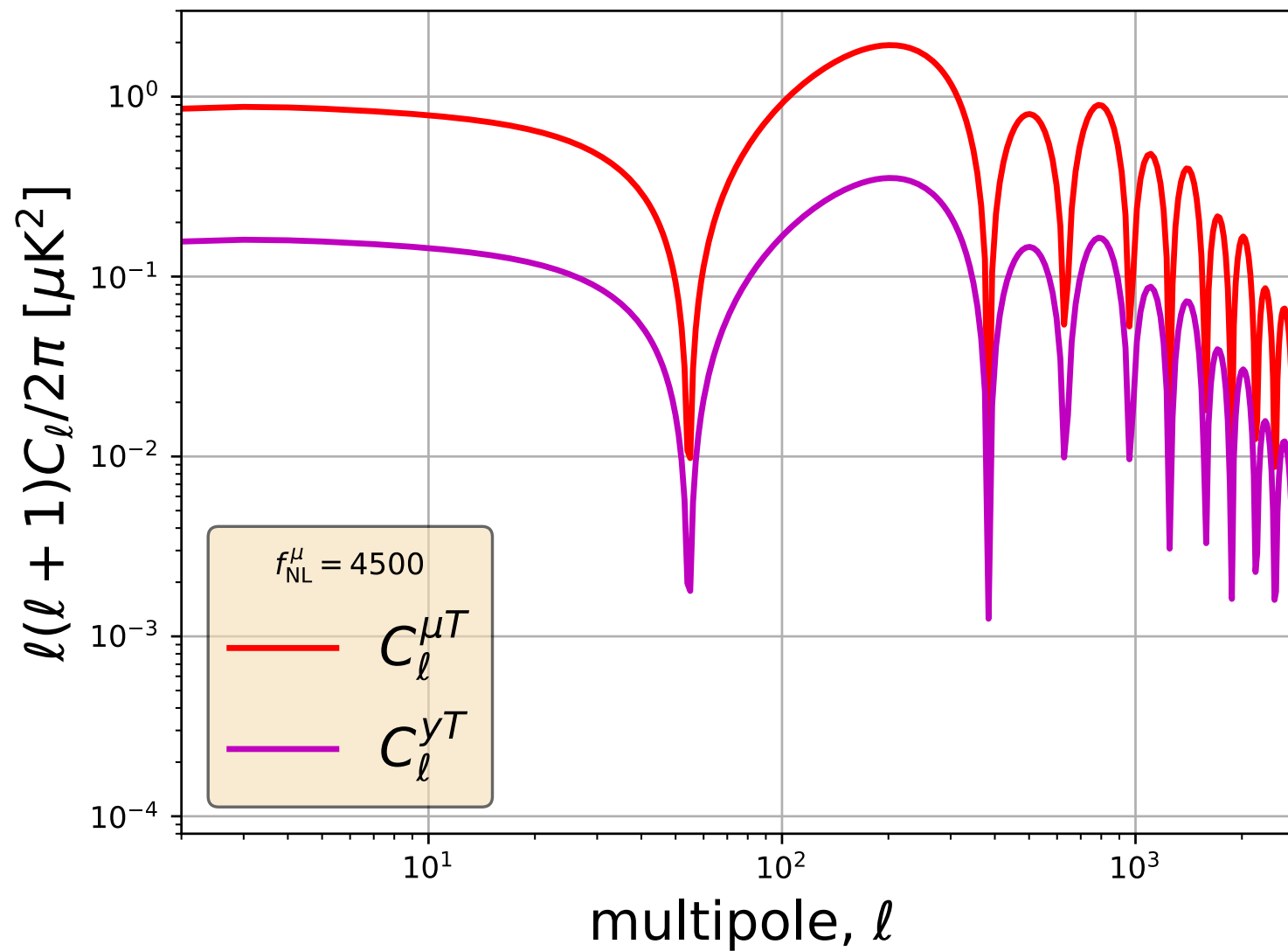
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New pivot scales to probe the scale-dependence of primordial non-Gaussianity!

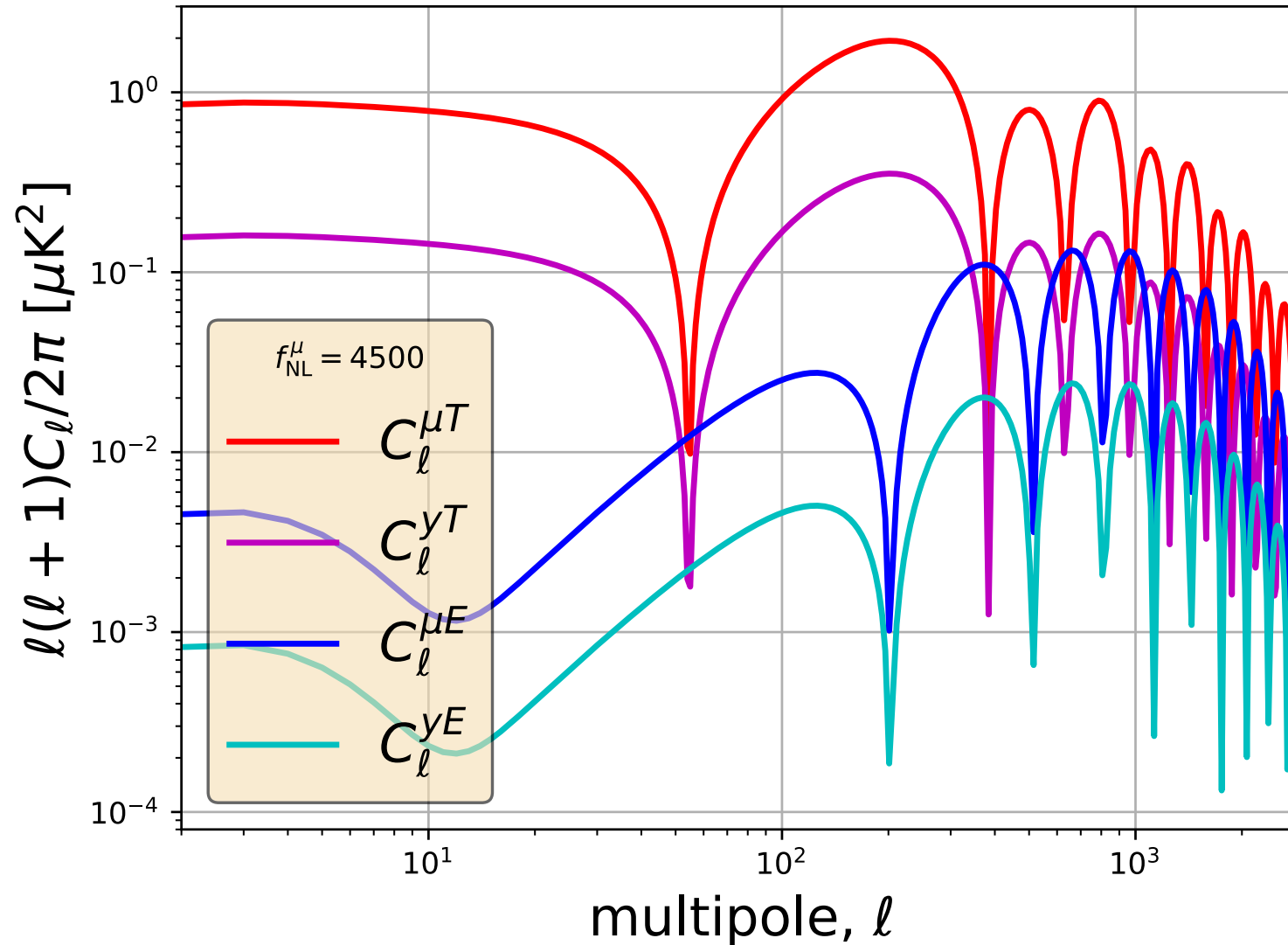
Theory

*Ravenni et al
JCAP 2017*



CMB polarization adds more leverage!

*Ravenni et al
JCAP 2017*



Extra bits
of information
from μE , yE
correlations!

Huge dynamic range of scales between CMB and μ -distortion probes

Mild scale dependence allows for large f_{NL} values at large wavenumber k

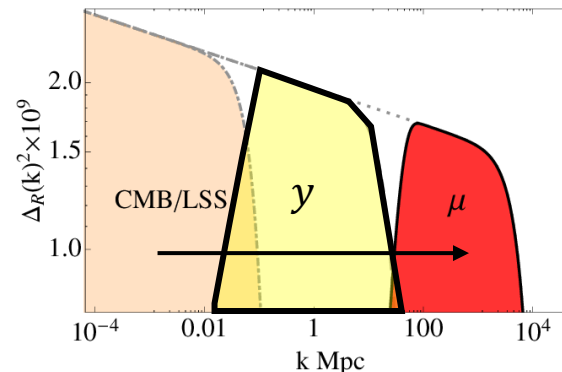
$$f_{\text{NL}}(k) = f_{\text{NL}}(k_0) \left(\frac{k}{k_0} \right)^{n_{\text{NL}} \lesssim 0.6}$$

$$f_{\text{NL}}(k \sim 10^{-2} \text{ Mpc}^{-1}) \simeq 5$$

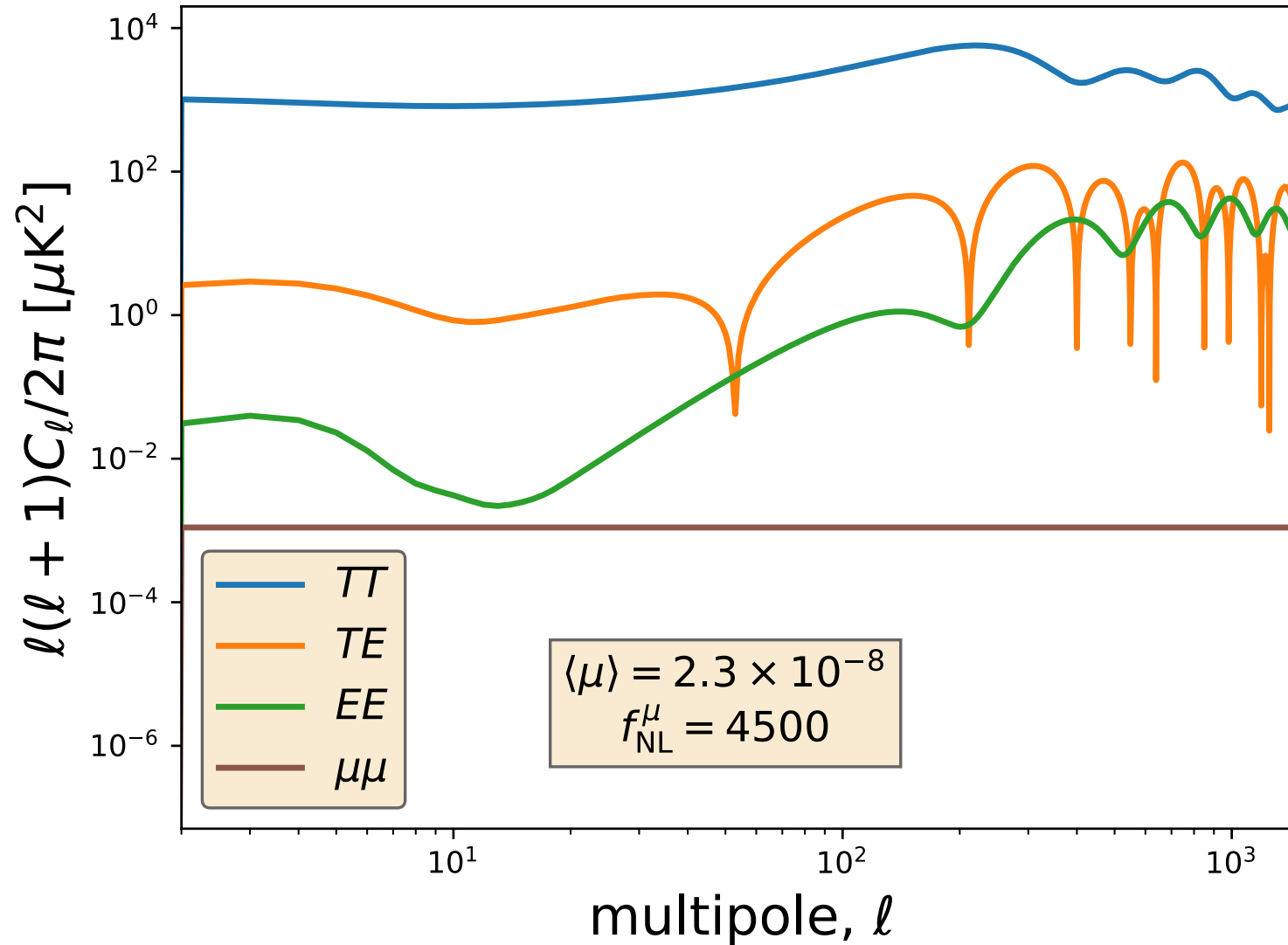
CMB anisotropies

$$f_{\text{NL}}(k \sim 10^3 \text{ Mpc}^{-1}) \simeq 5000$$

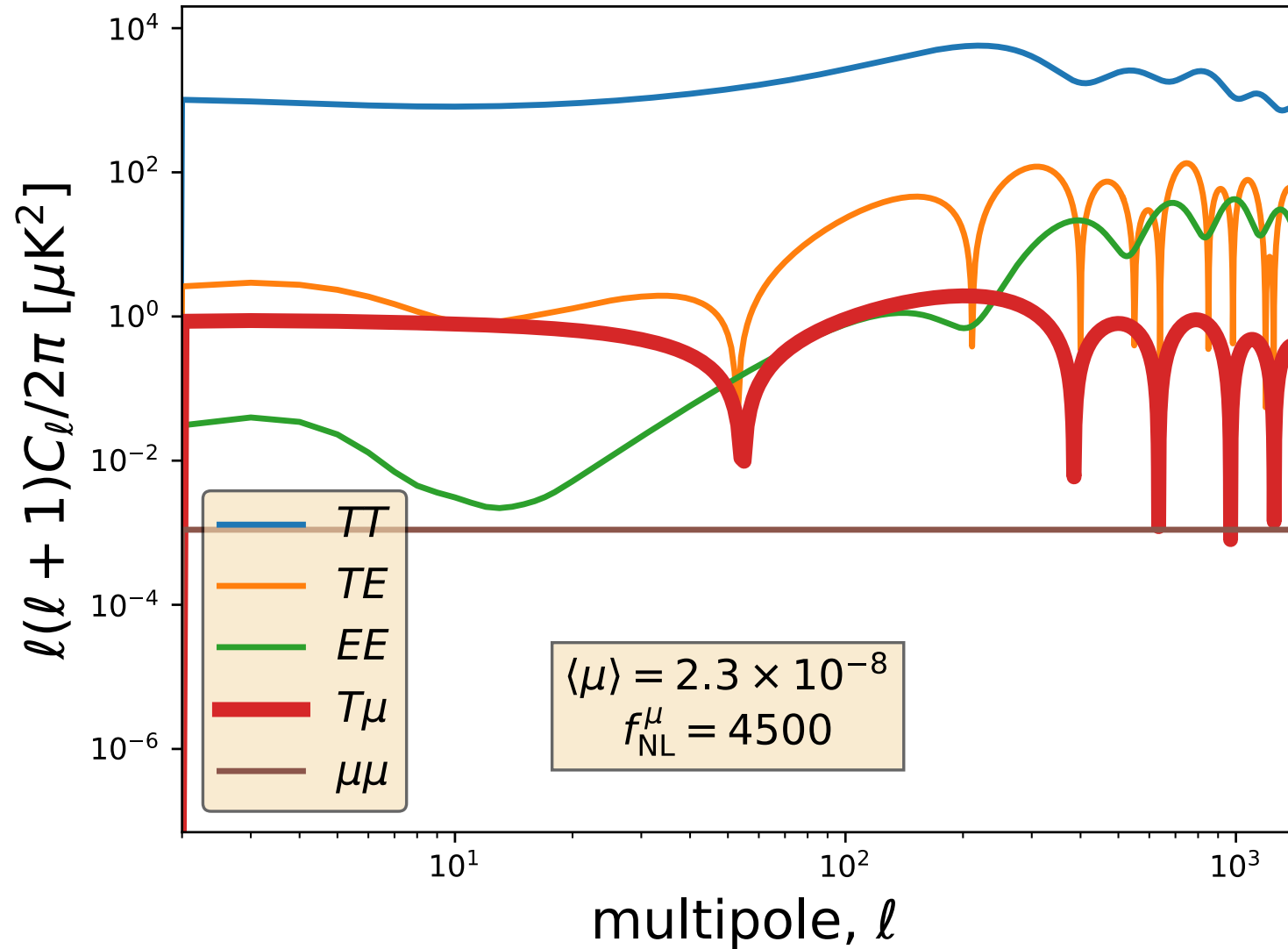
μ -distortion anisotropies



Orders of magnitude

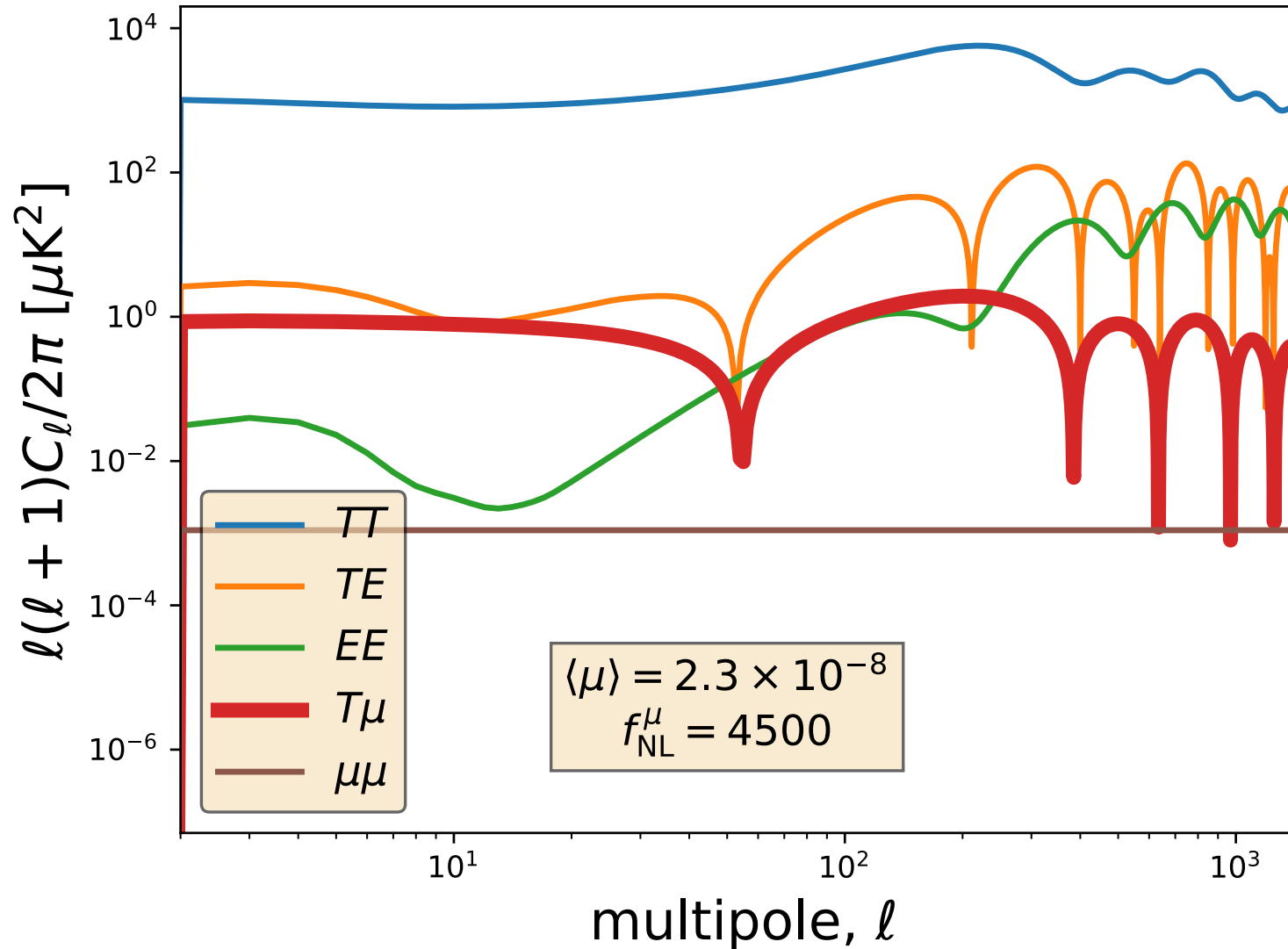


Orders of magnitude



For $f_{\text{NL}}^\mu \simeq 4500$
 μT comparable
to TE and EE

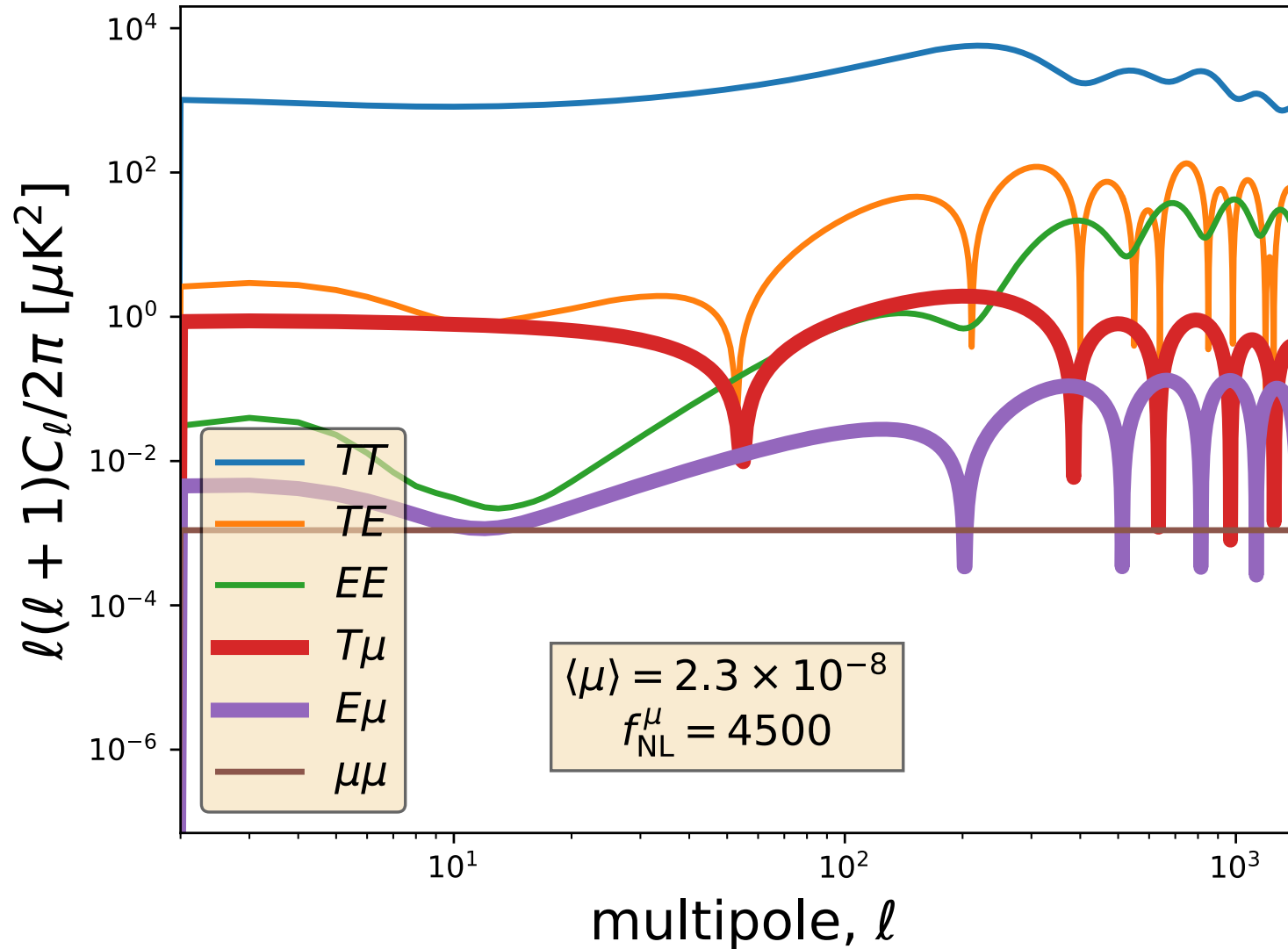
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**A science goal
for future
CMB imagers!**

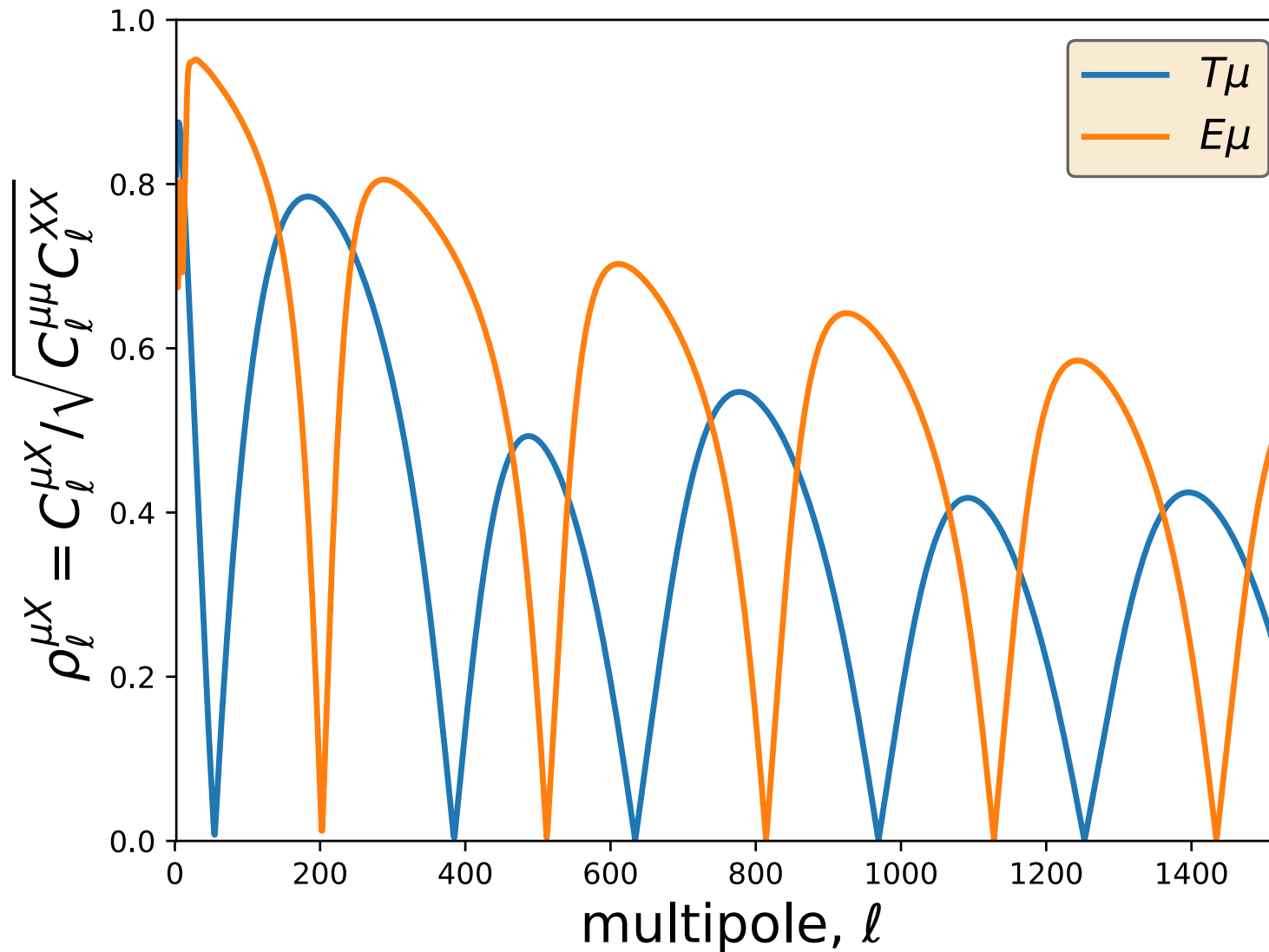
Orders of magnitude



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**A science goal
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Degree of correlation: $\mu \times E$ vs $\mu \times T$



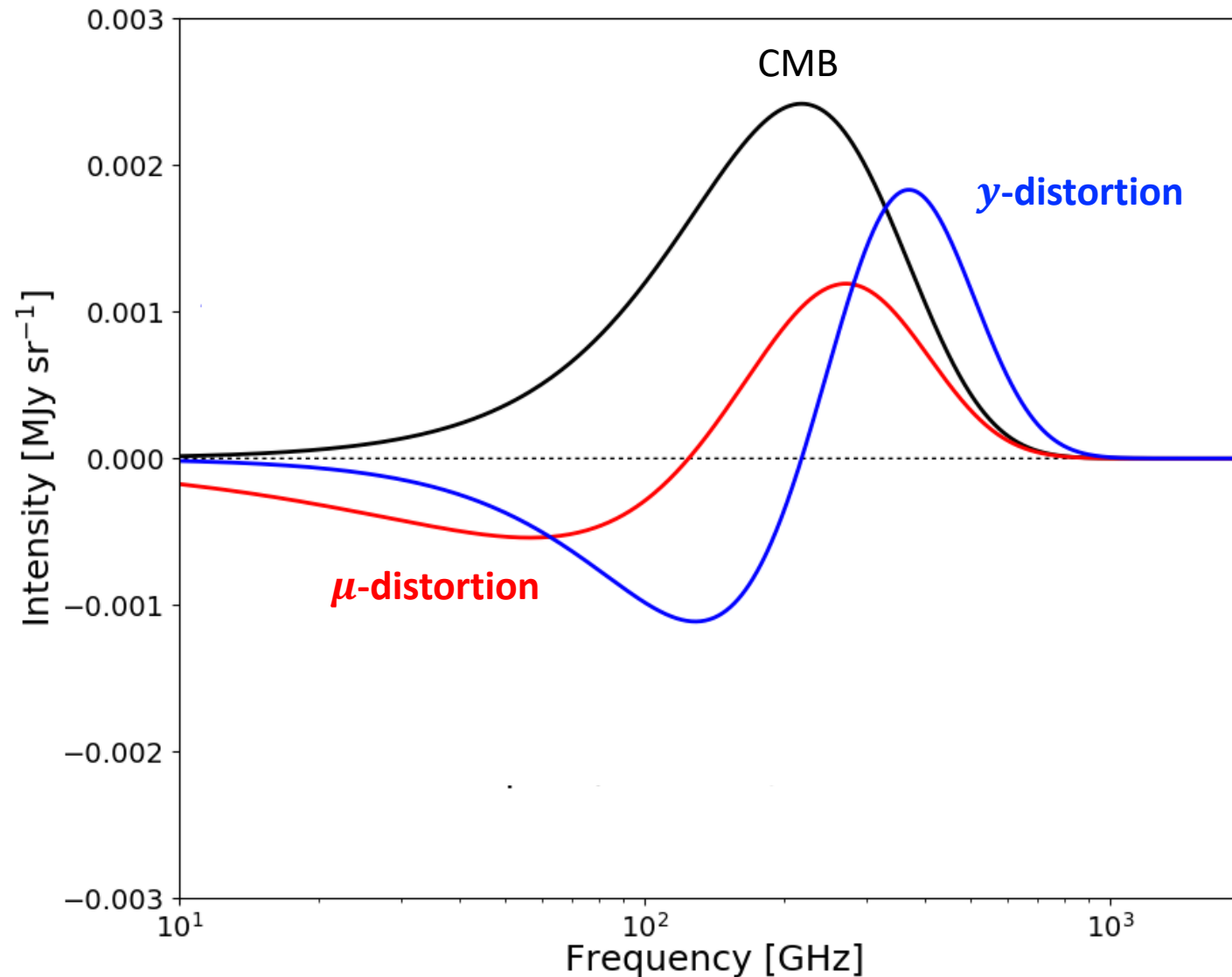
Remazeilles et al
MNRAS 2022

μE correlation
larger than
 μT correlation!

Questions

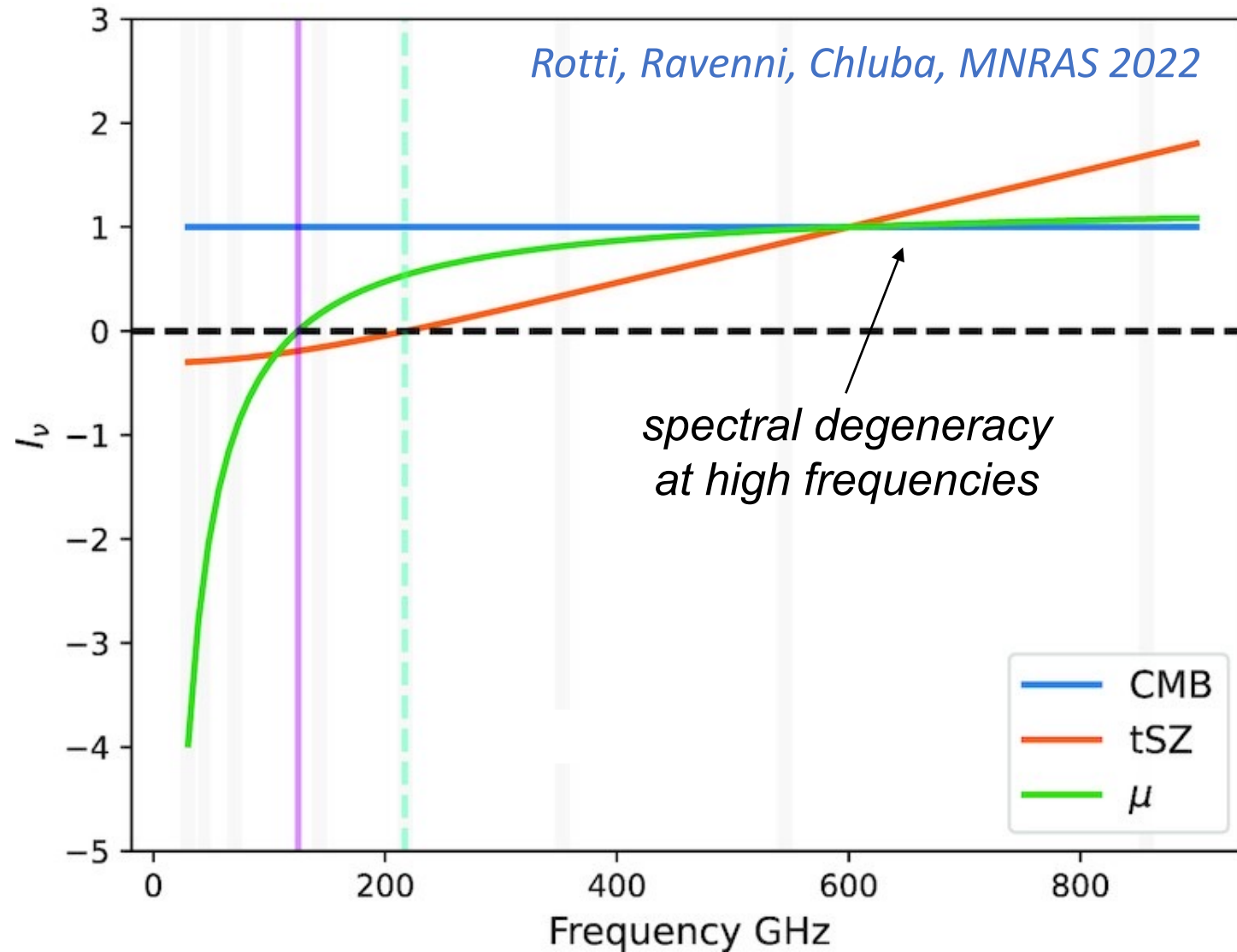
- ❑ Can we detect μT and μE correlated anisotropies with a future CMB satellite like *LiteBIRD*?
- ❑ What constraints on $f_{\text{NL}}^{\mu}(k \simeq 740 \text{ Mpc}^{-1})$ can be achieved with *LiteBIRD* in the presence of foregrounds?
- ❑ How much do we gain on f_{NL} sensitivity by including cross-correlations with CMB E -mode polarization?

Distinct spectral signatures of the distortions



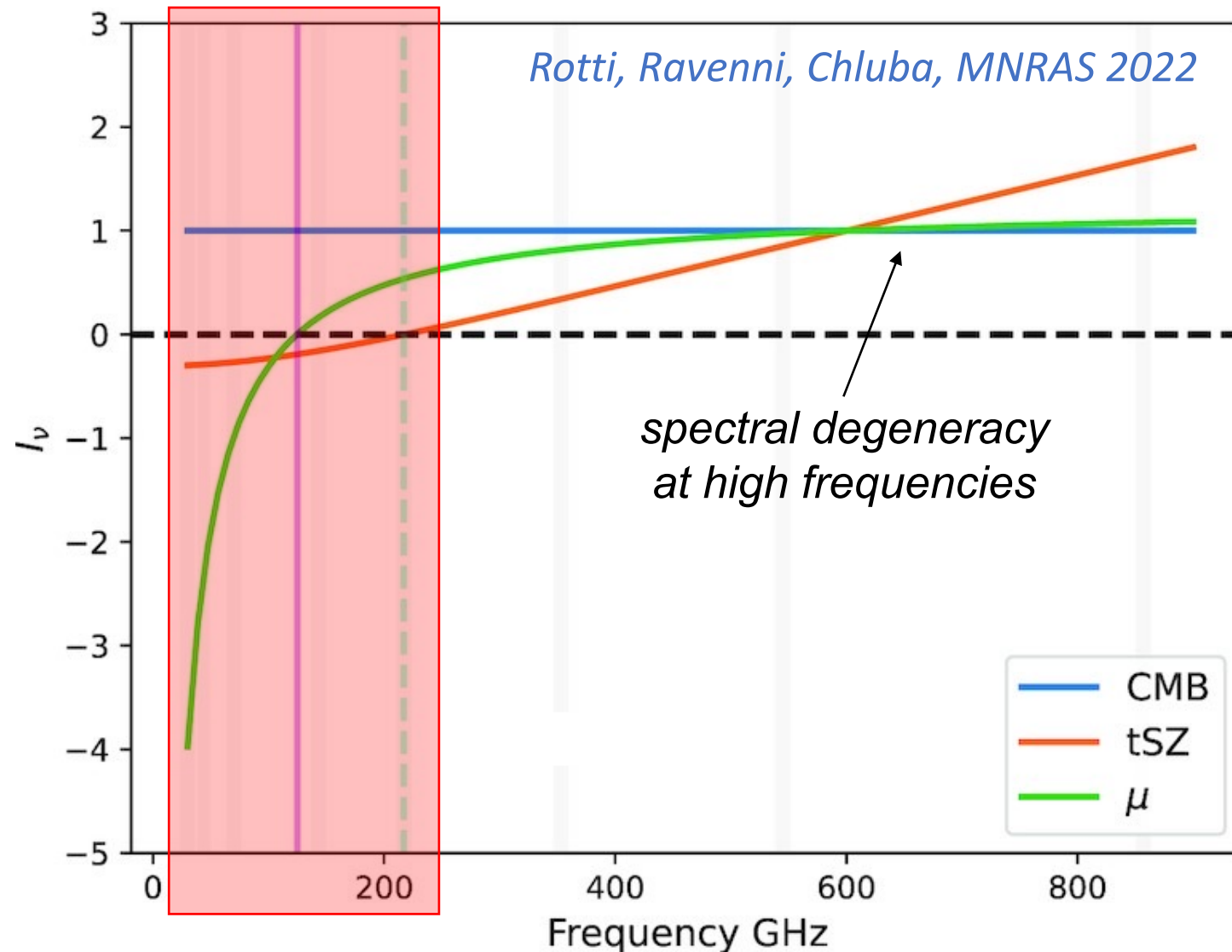
Multi-frequency observations should allow us to disentangle them

Spectral signatures in temperature units



Spectral signatures in temperature units

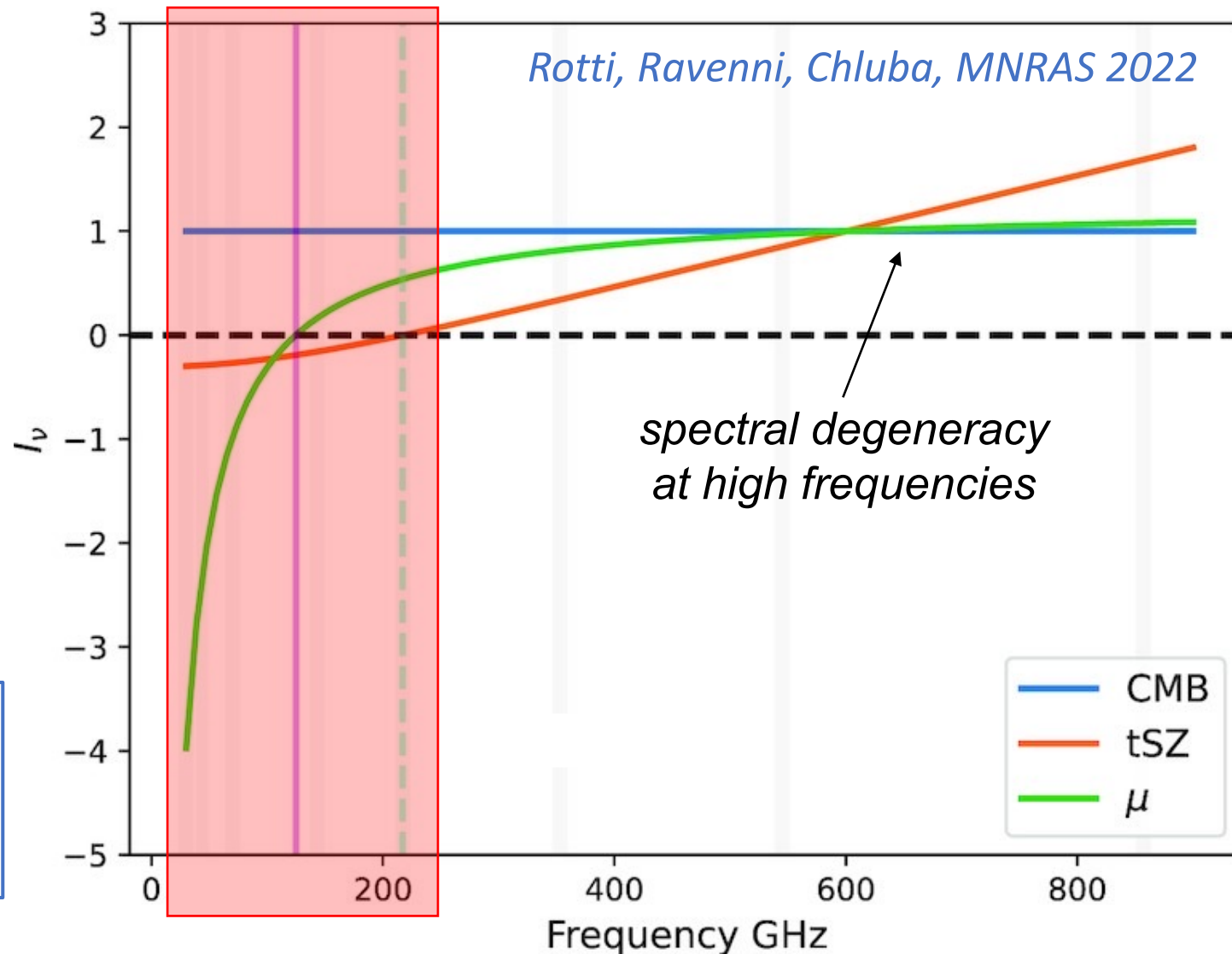
Low frequencies
are essential to
disentangle CMB
and μ -distortion
anisotropies!



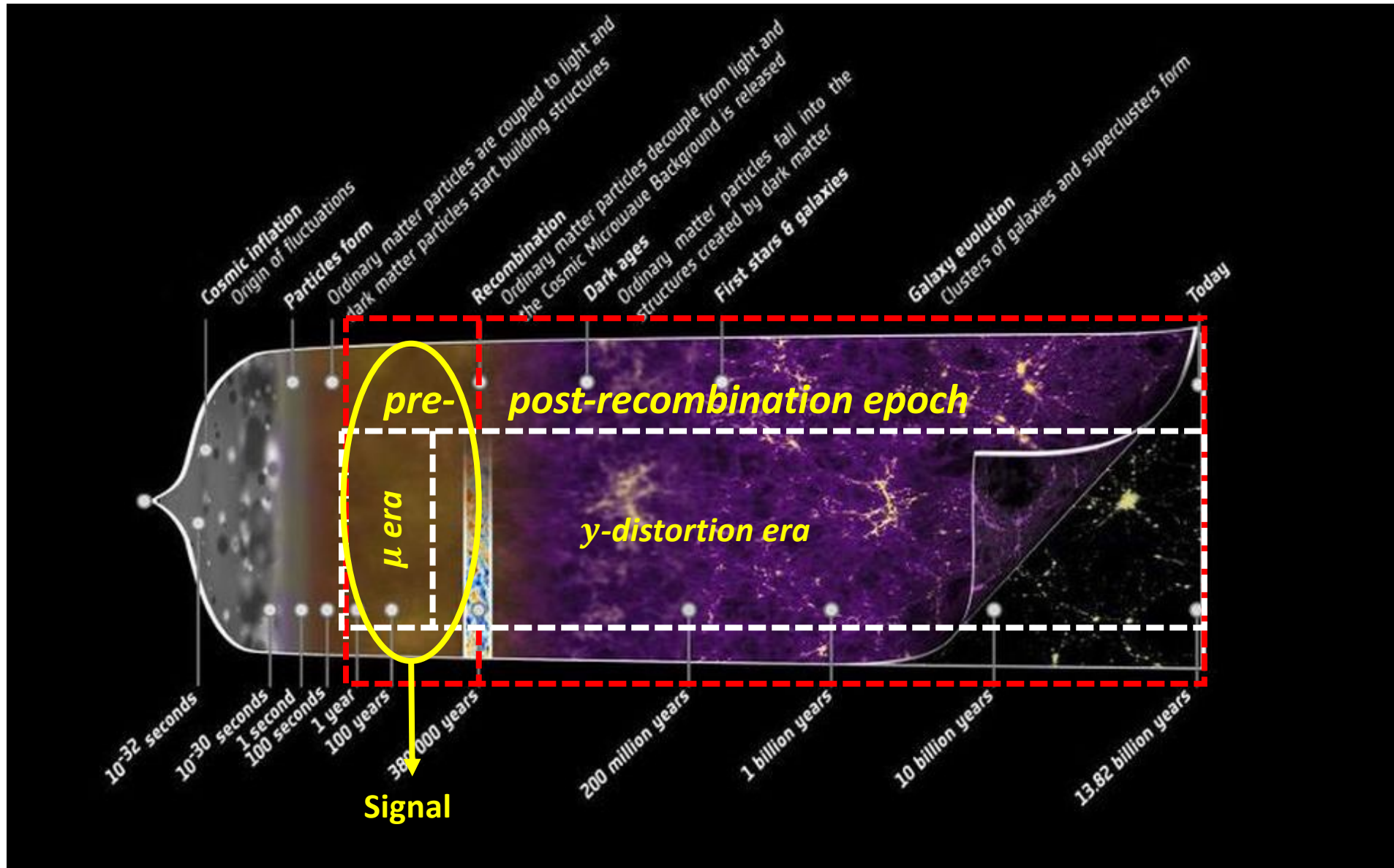
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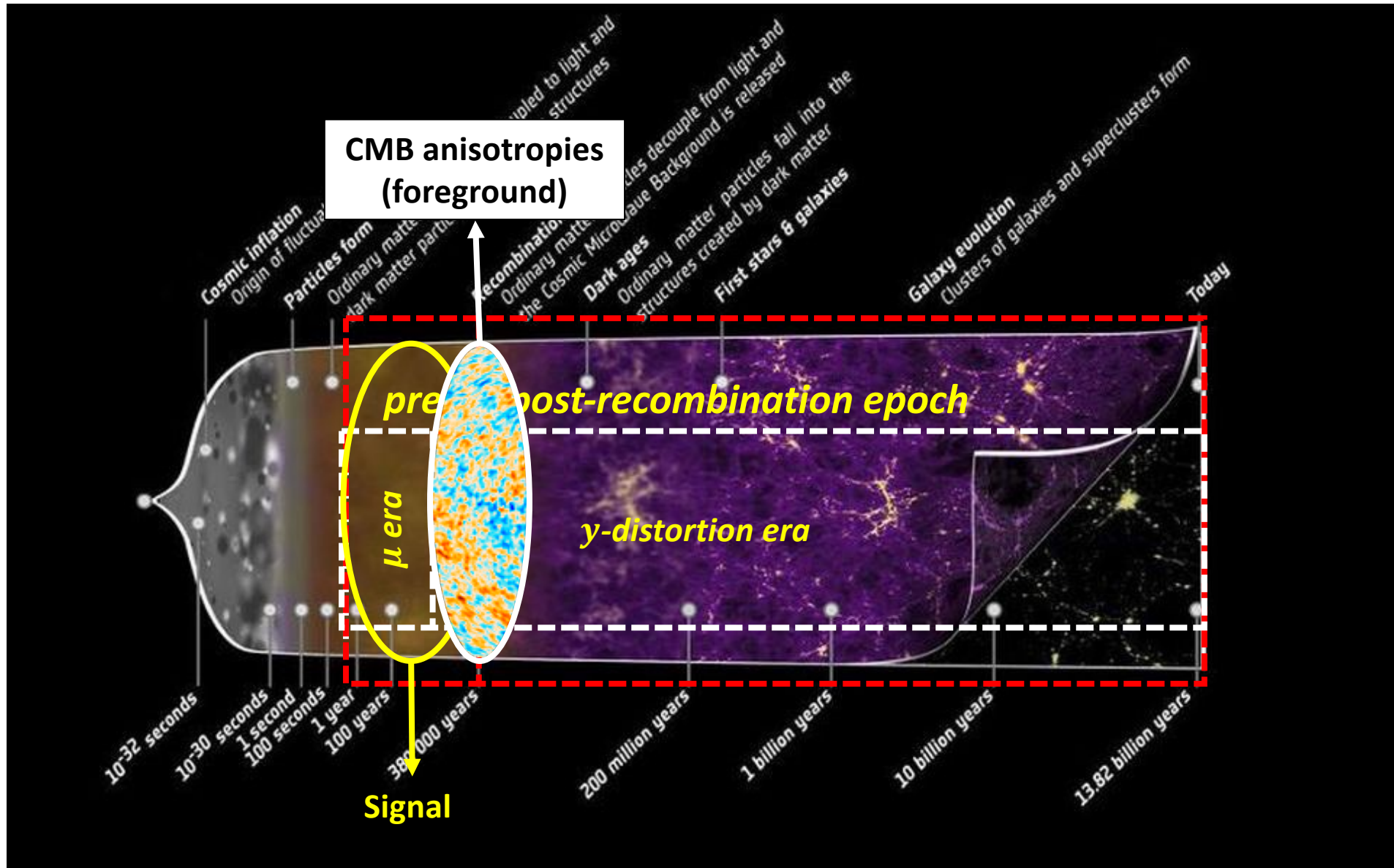
→ see talk by
David Zegeye
about using SKA



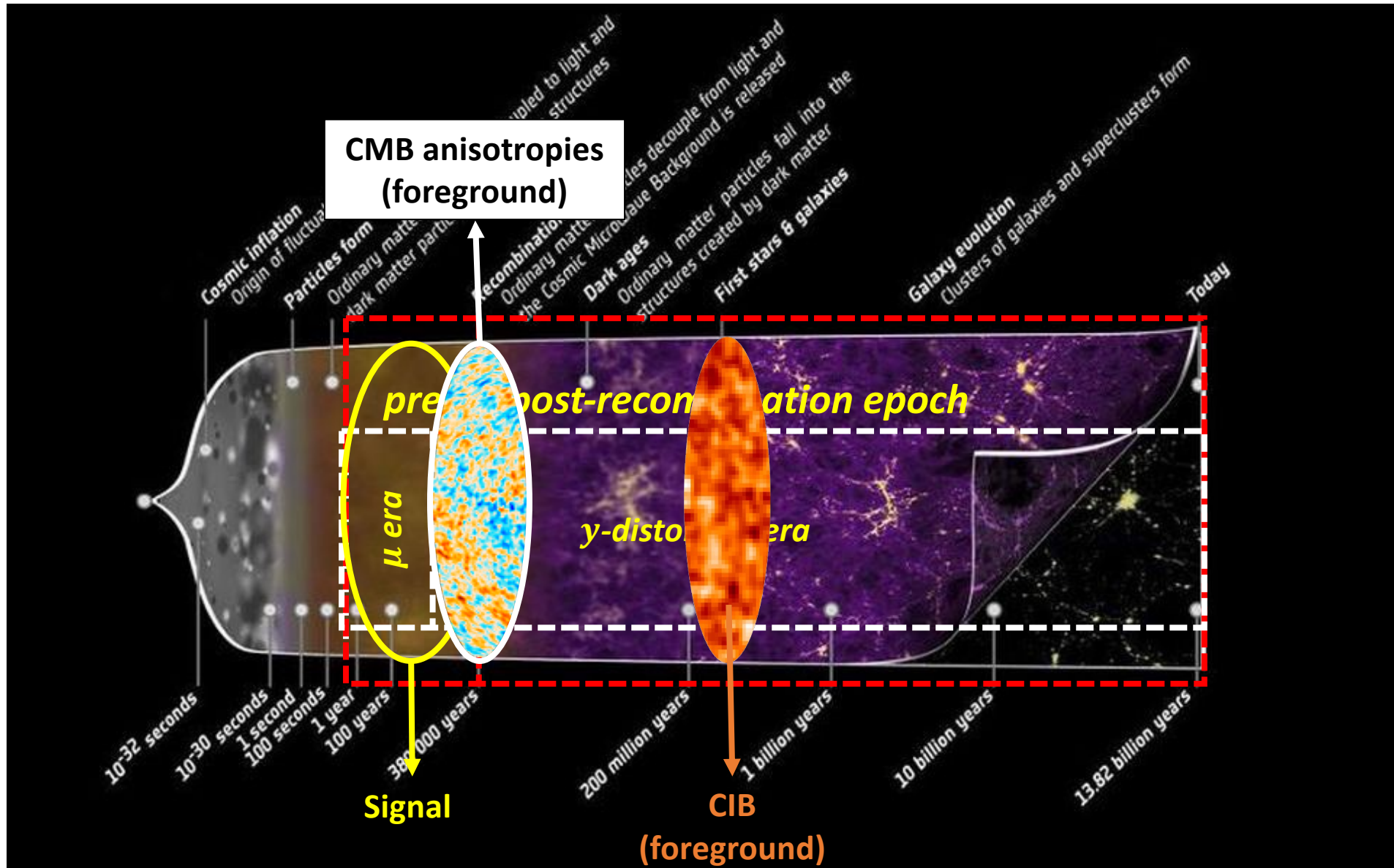
Foregrounds obscure SD anisotropies



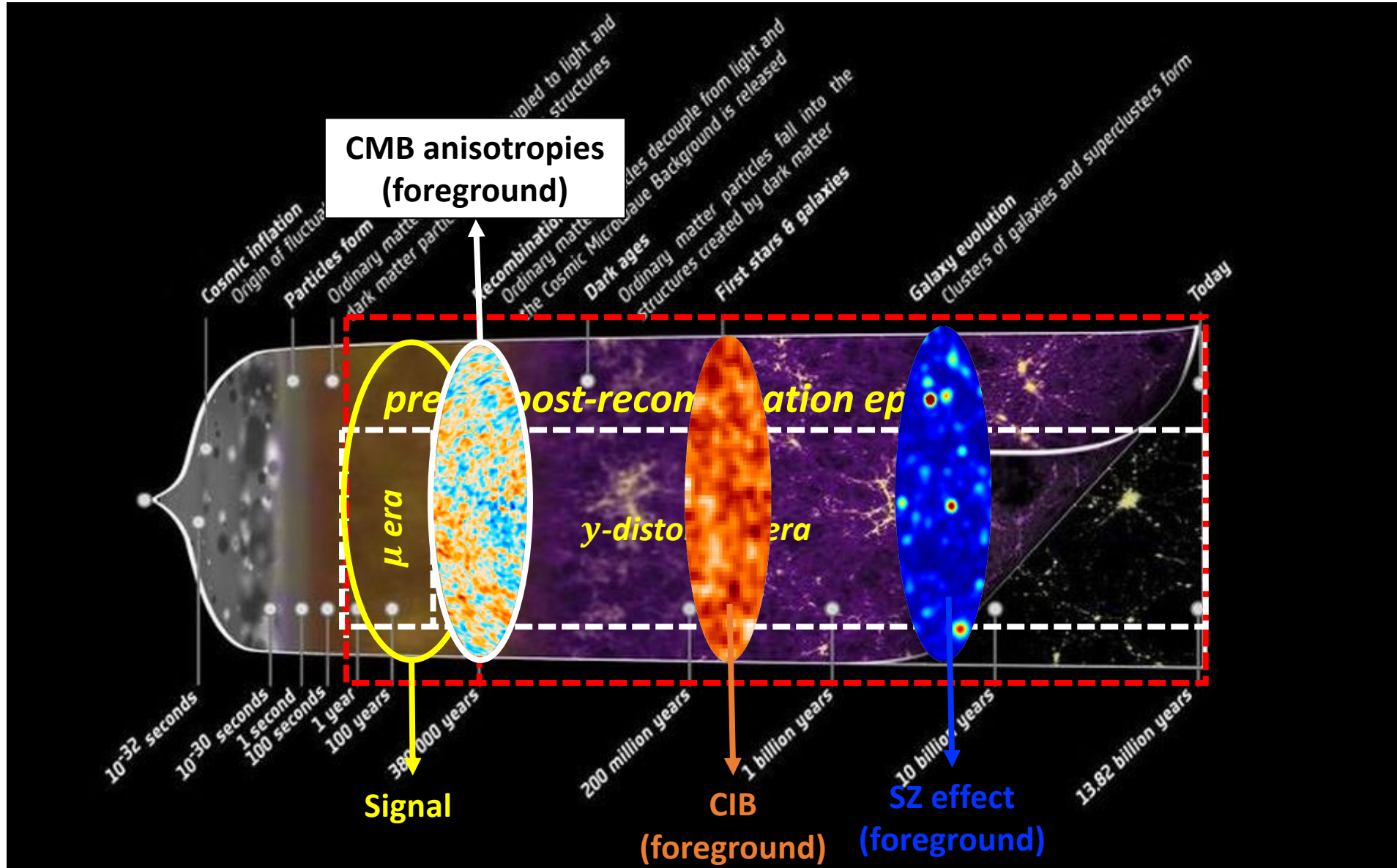
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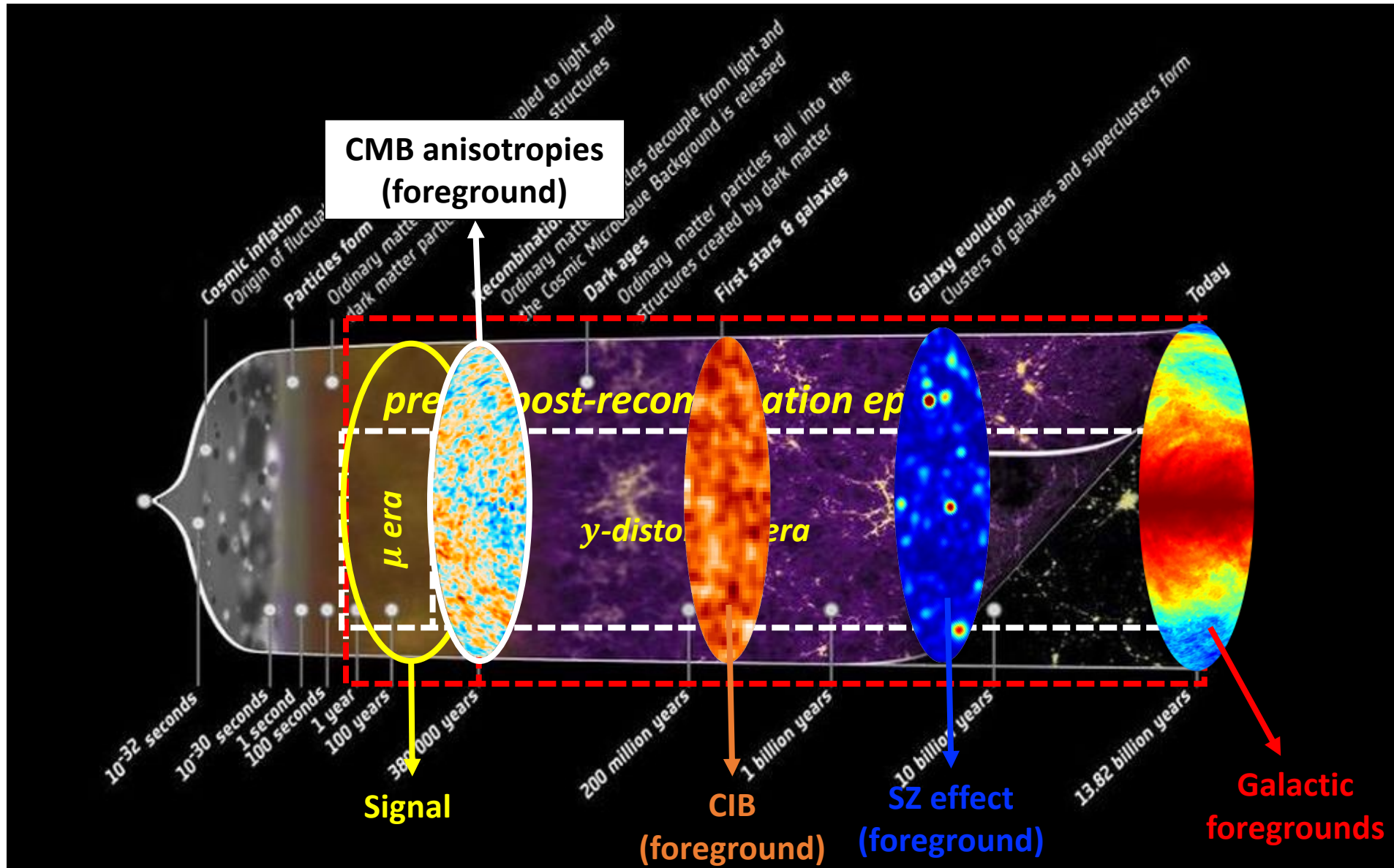
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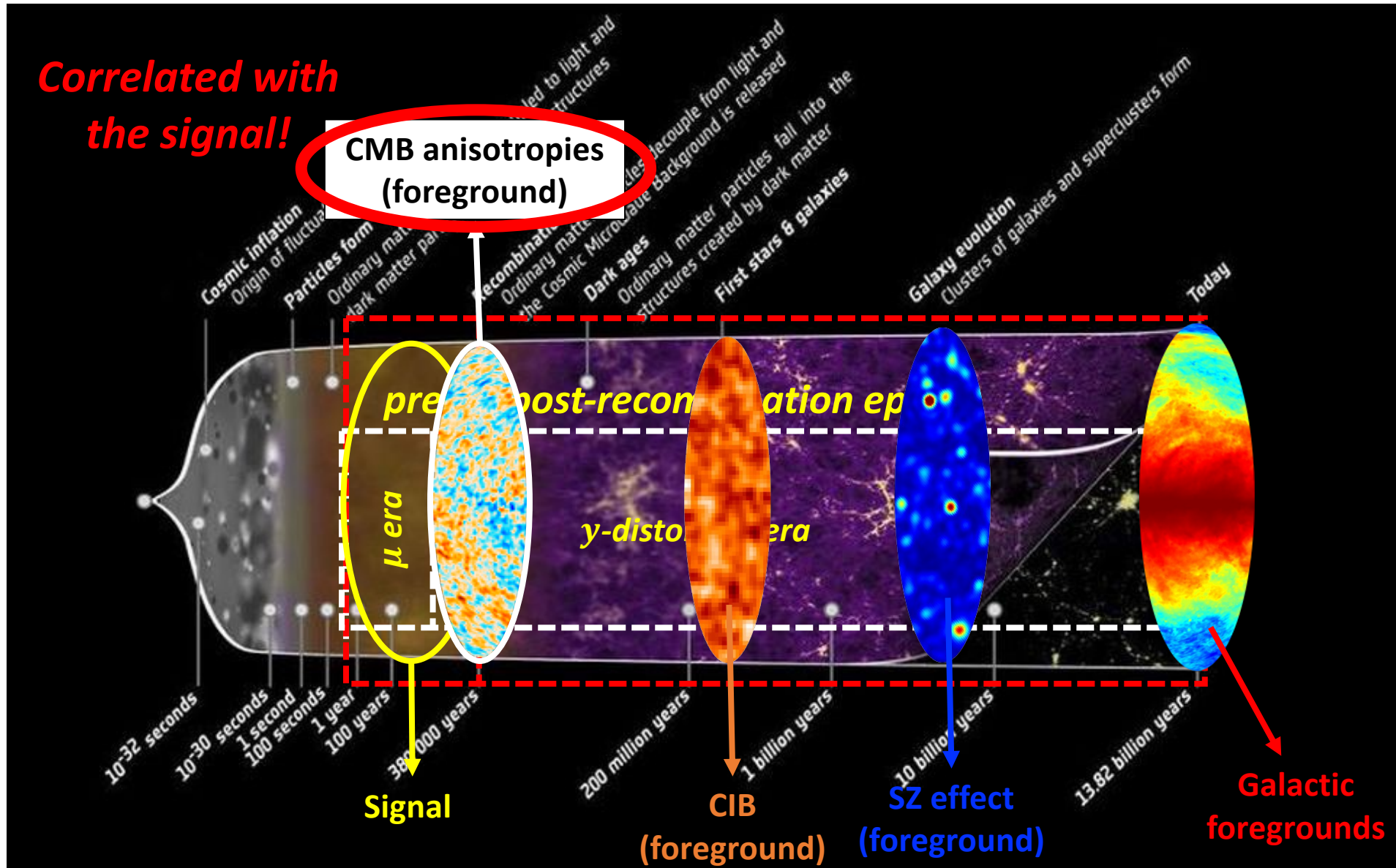
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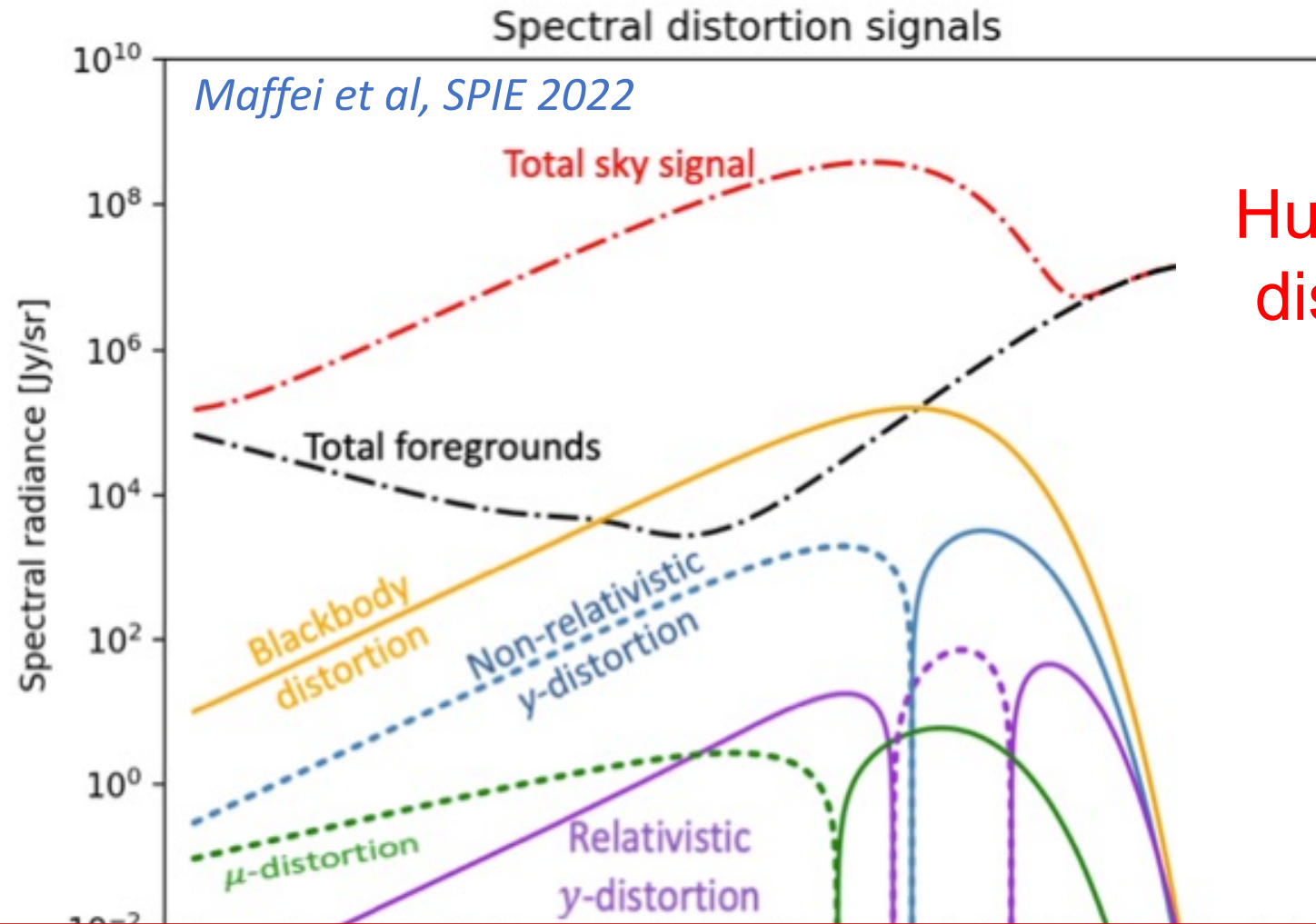
Foregrounds obscure SD anisotropies



Foregrounds obscure SD anisotropies



Foregrounds vs Spectral Distortions (SD)

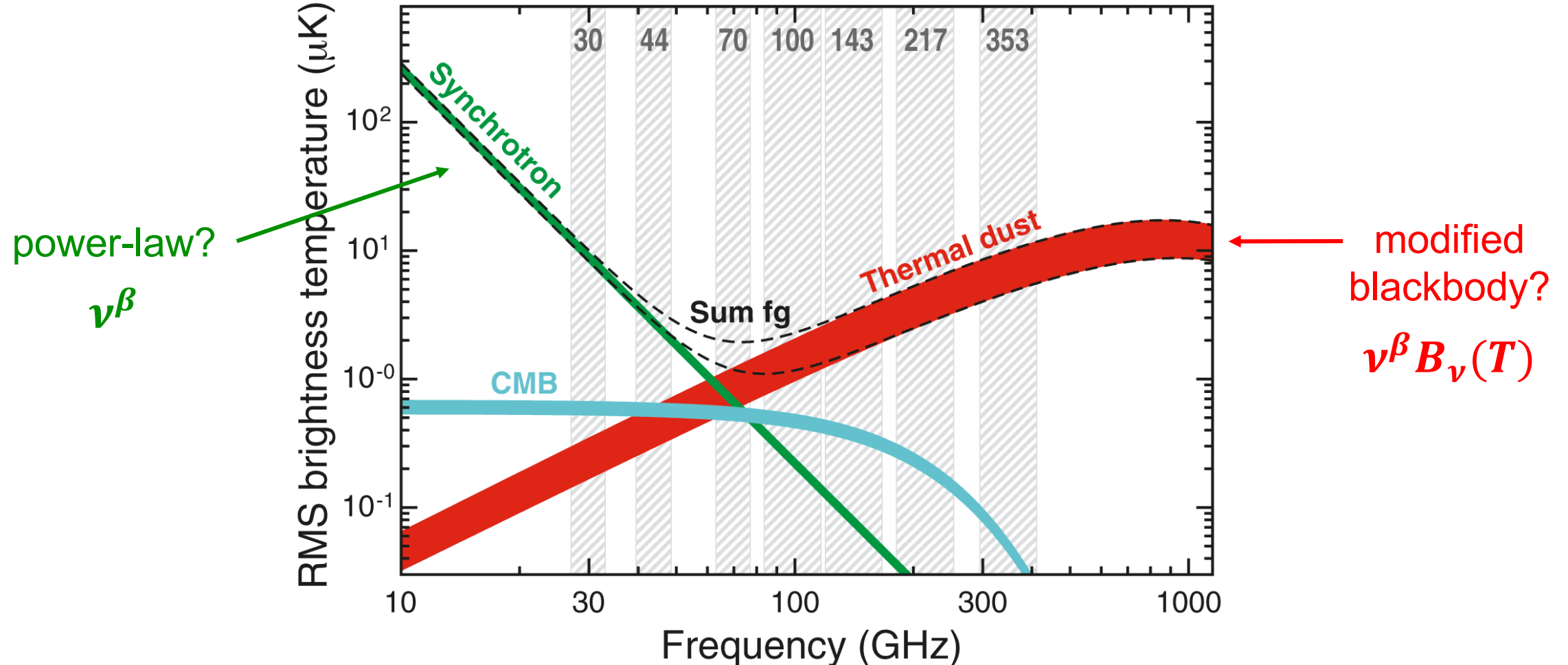


Huge amplitude discrepancies!

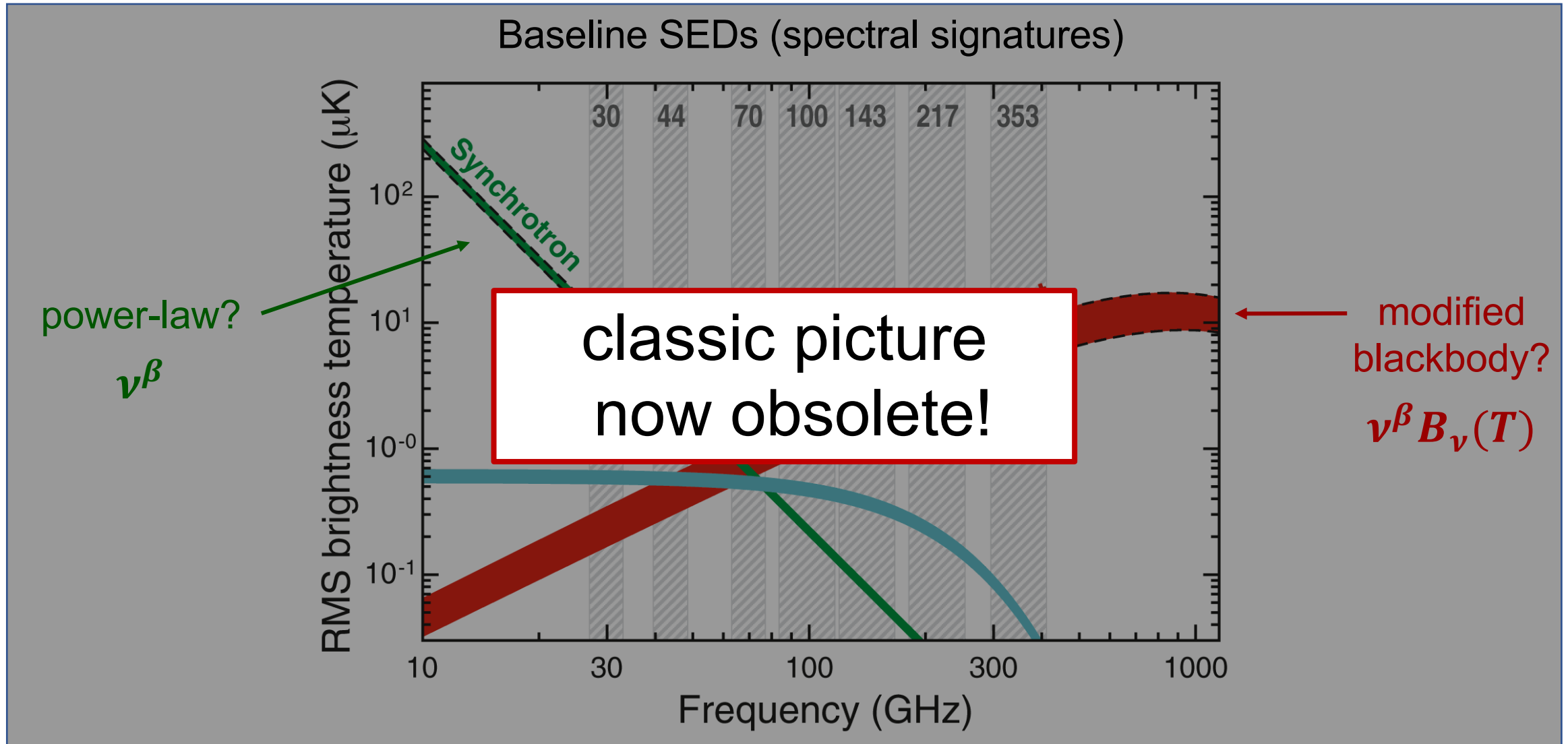
Tiny modelling errors on the foregrounds $\Rightarrow$ Large error / bias on the SD signal!

The “smoothness” of foregrounds is a myth

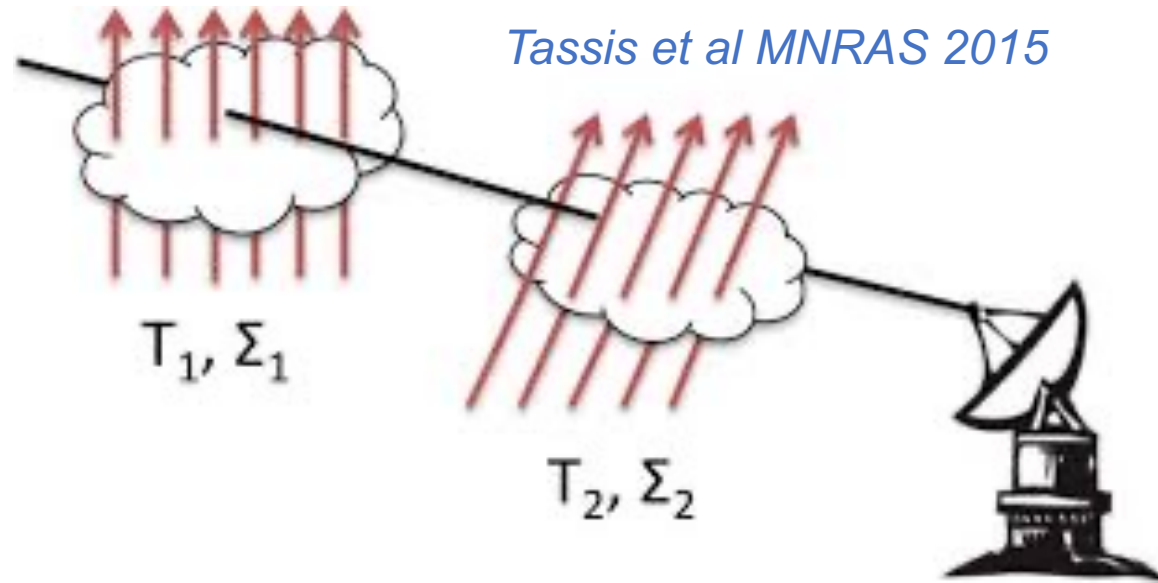
Baseline SEDs (spectral signatures)



The “smoothness” of foregrounds is a myth



Spectral distortions of the foregrounds!



Spectral variations averaged
along the line of sight

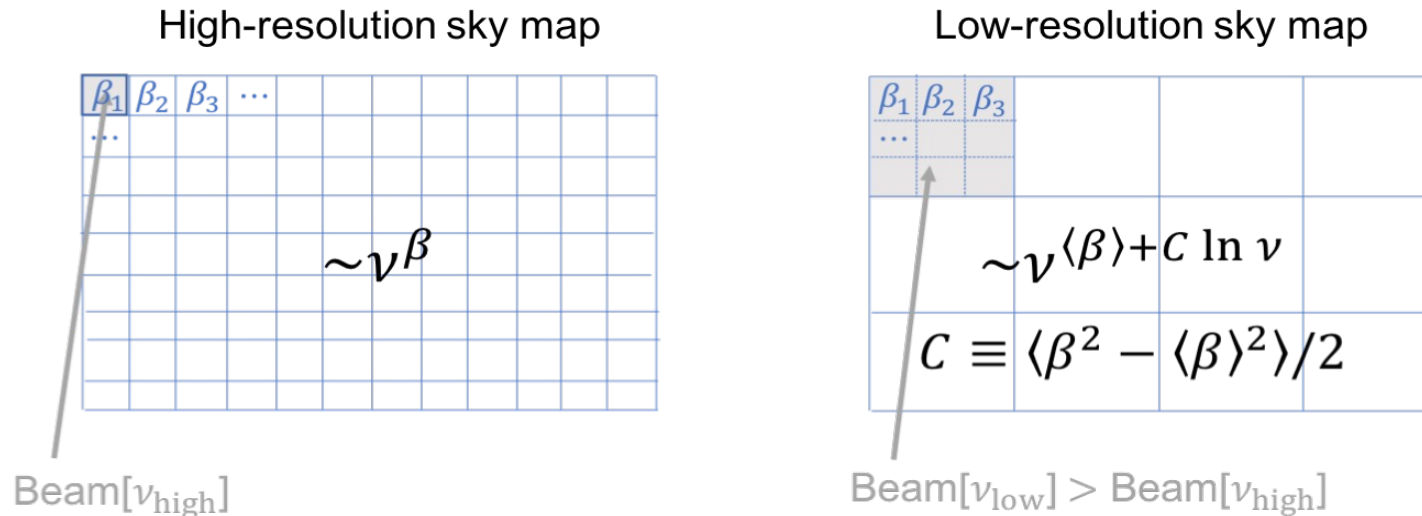
$$\langle \nu^{\beta_1} B_\nu(T_1) + \nu^{\beta_2} B_\nu(T_2) + \dots \rangle \neq \nu^{\langle \beta \rangle} B_\nu(\langle T \rangle)$$

Spectral distortions to
the modified blackbody

Chluba, Hill, Abitbol, MNRAS 2017

Spectral distortions of the foregrounds!

Remazeilles, Rotti, Chluba, MNRAS 2021



Spectral variations
averaged within the beam

$$\langle \nu \beta_1 + \nu \beta_2 + \dots \rangle = \nu \langle \beta \rangle + \frac{1}{2} \sigma_\beta^2 \ln \nu + \dots$$

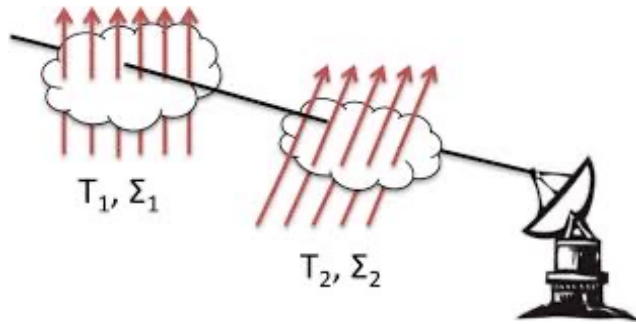
Spectral distortions
to the power-law
(curvature terms)

Chluba, Hill, Abitbol, MNRAS 2017

Spectral distortions of the foregrounds

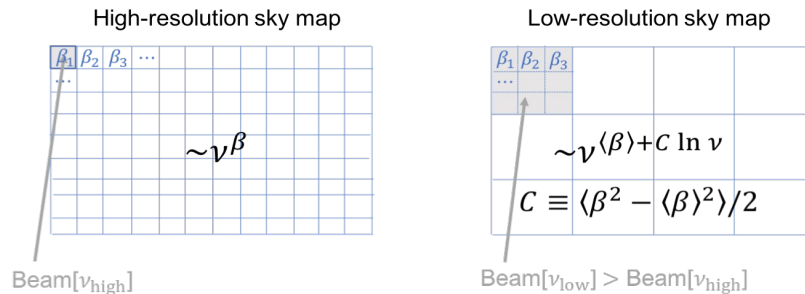
Foreground SED distortions

Averaging along the line of sight



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Averaging within the beam



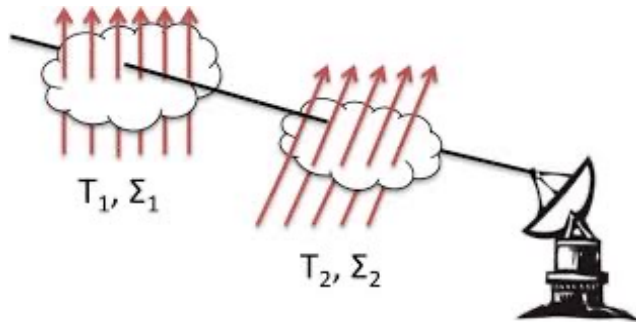
- Spectral distortions of the baseline foreground SEDs
- Complicates foreground modelling for parametric fitting
- Could mimic CMB spectral distortion signals

Chluba, Hill, Abitbol, MNRAS (2017)
Remazeilles, Rotti, Chluba, MNRAS (2021)

Spectral distortions of the foregrounds

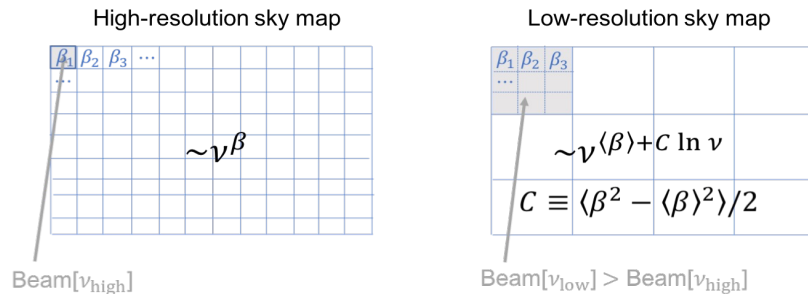
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Averaging within the beam



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Tiny distortions to foregrounds $\gg \mu$ -distortion !

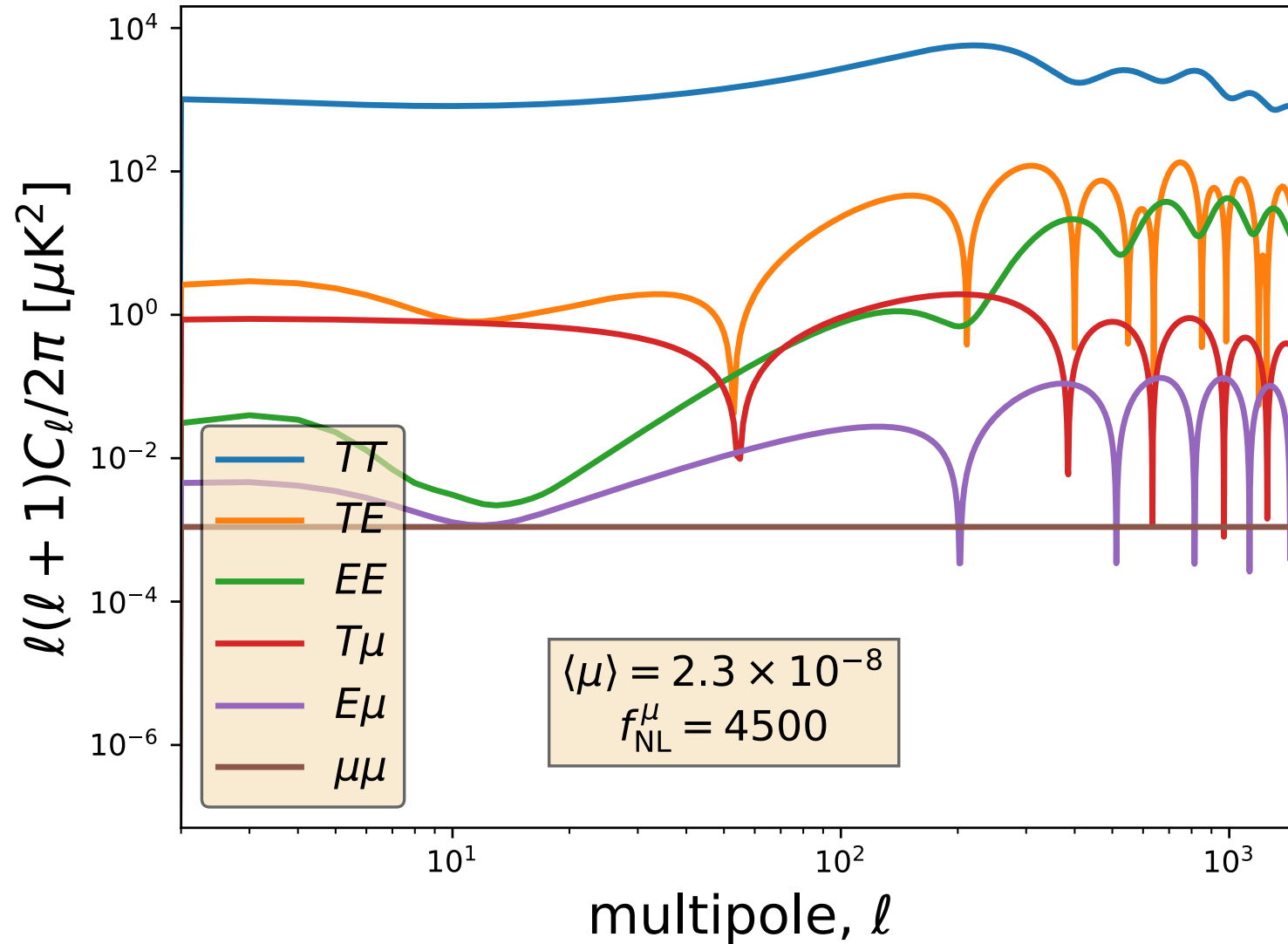
Chluba, Hill, Abitbol, MNRAS (2017)

Remazeilles, Rotti, Chluba, MNRAS (2021)

Analysis

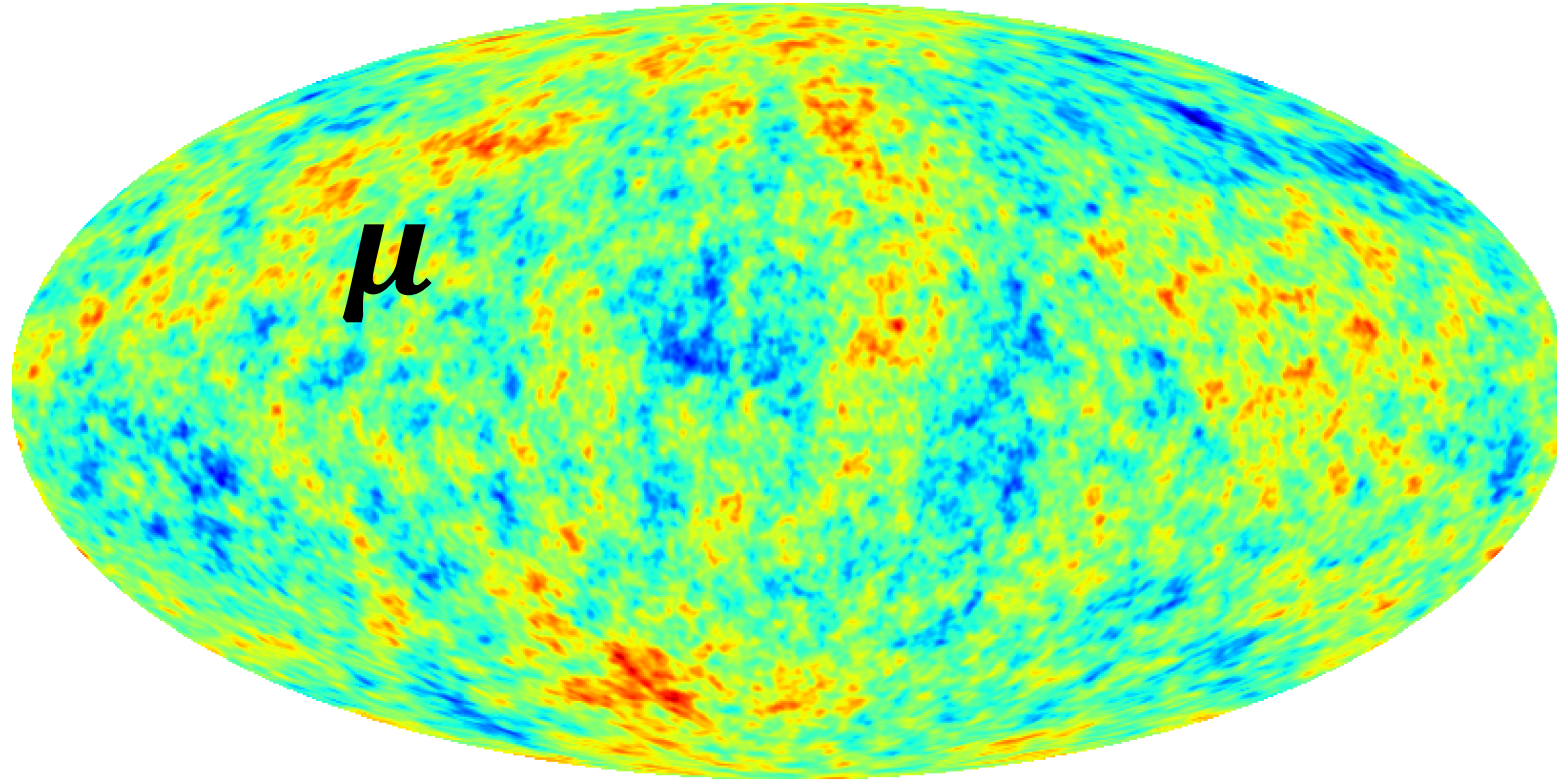
Theory

*Ravenni et al
JCAP 2017*

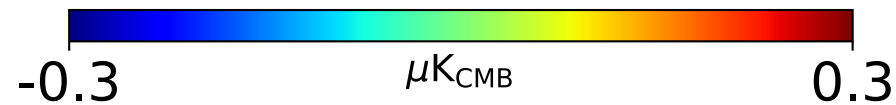


Correlated map simulations using Cholesky

μ -distortion anisotropies ($f_{\text{NL}}^{\mu} = 4500$)



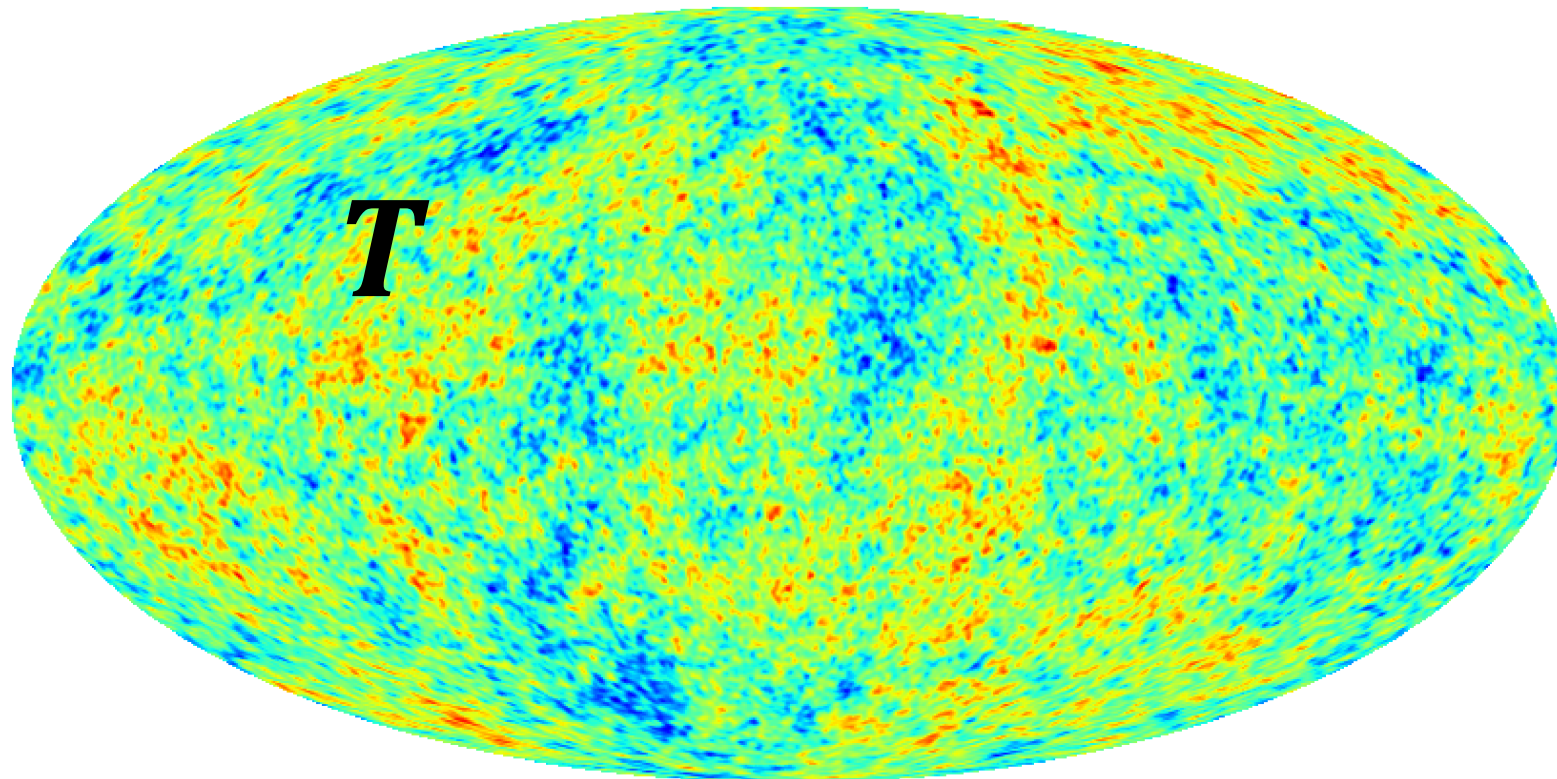
60' resolution



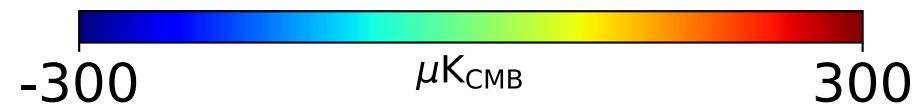
Remazeilles, Ravenni, Chluba MNRAS 2022

Correlated map simulations using Cholesky

CMB temperature anisotropies



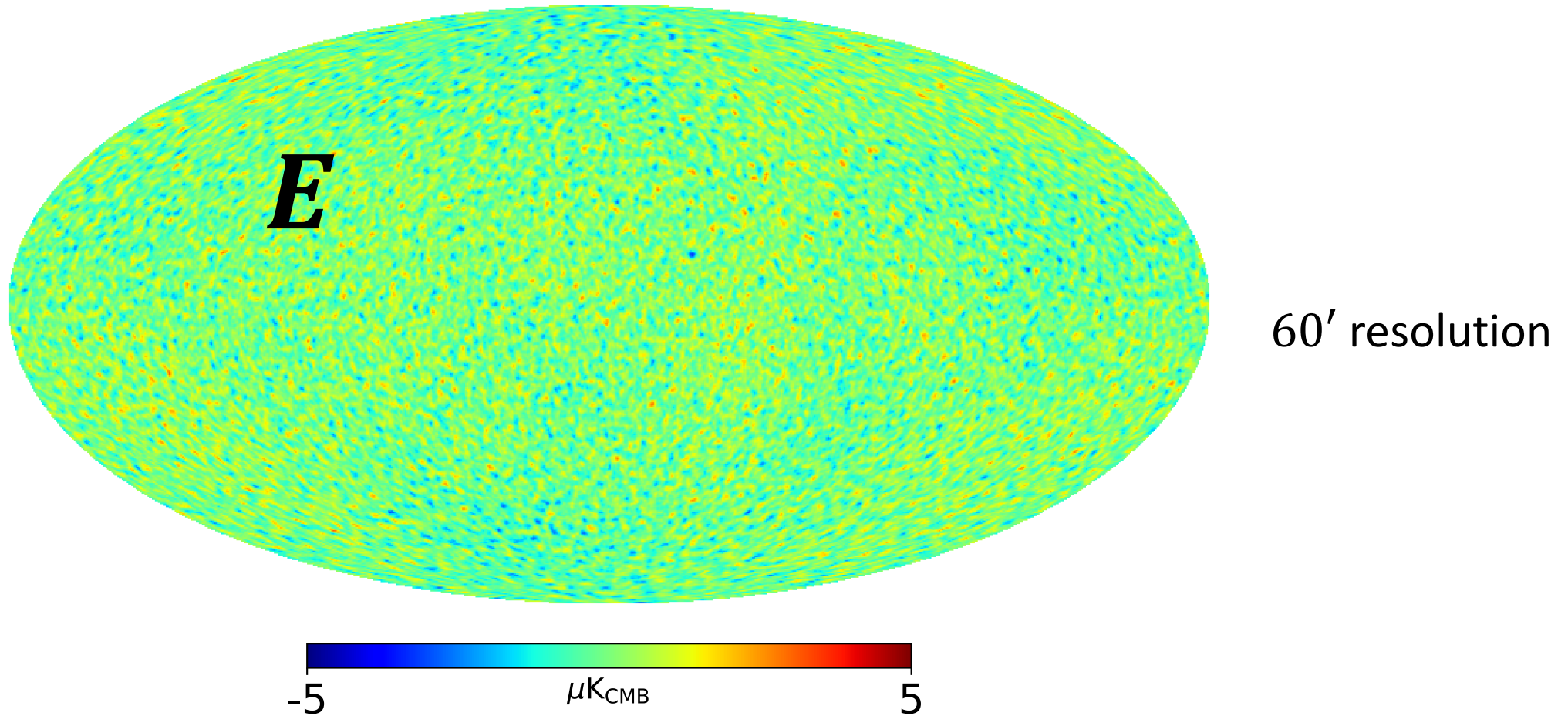
60' resolution



Remazeilles, Ravenni, Chluba MNRAS 2022

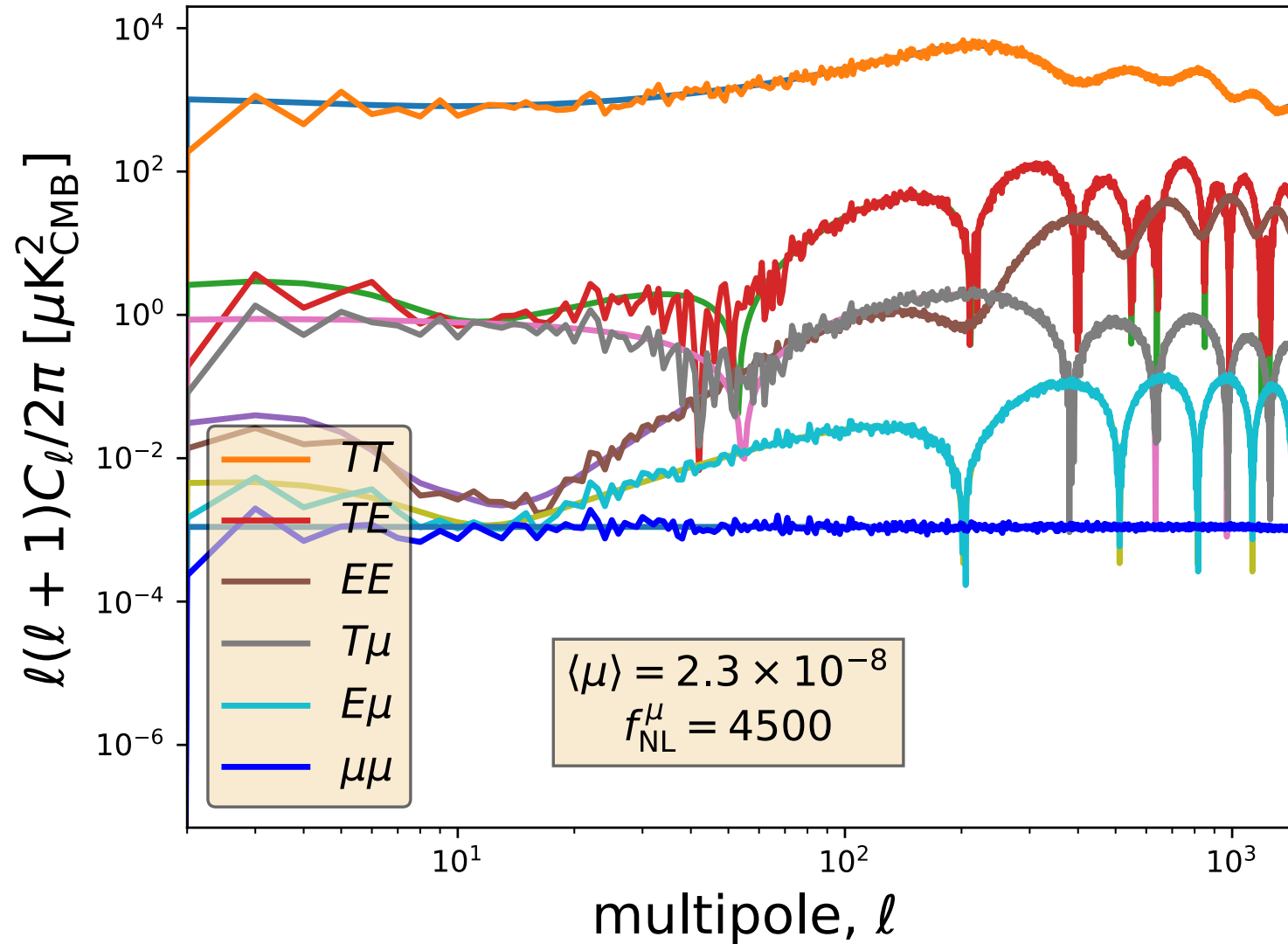
Correlated map simulations using Cholesky

CMB E-mode polarization anisotropies



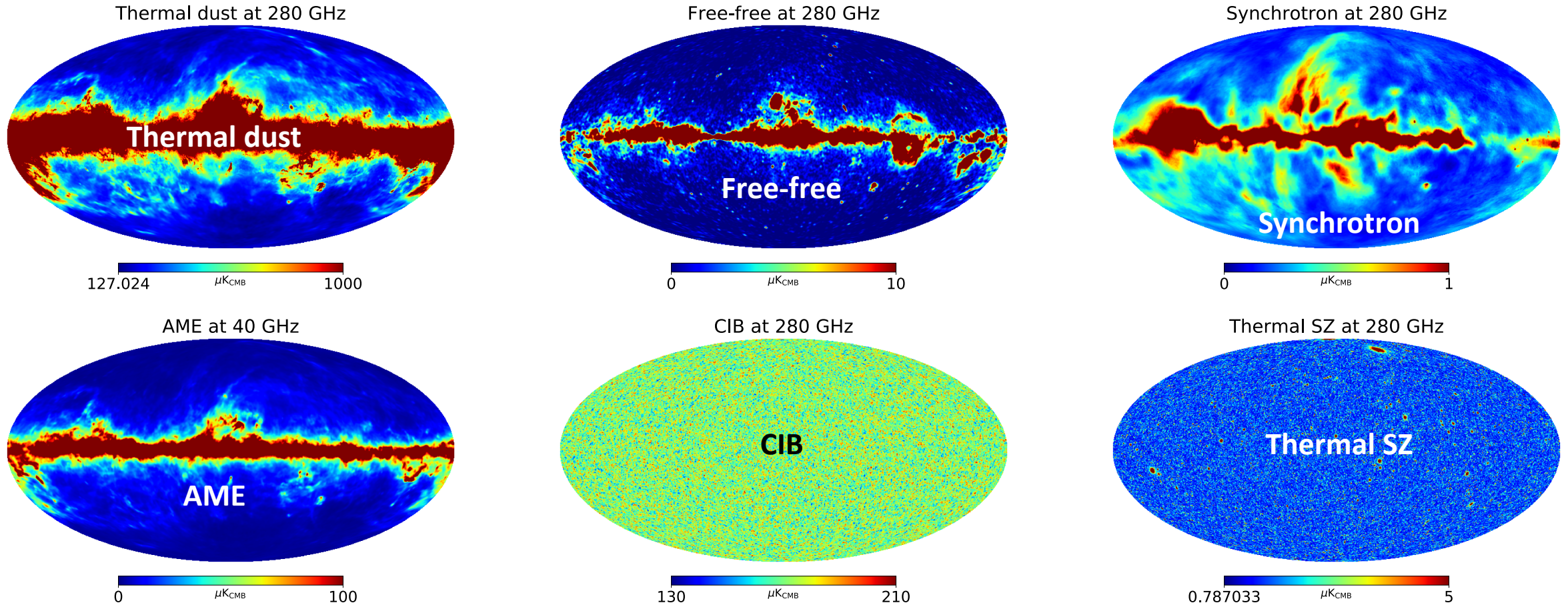
Remazeilles, Ravenni, Chluba MNRAS 2022

Correlated map simulations using Cholesky



*Remazeilles,
Ravenni, Chluba
MNRAS 2022*

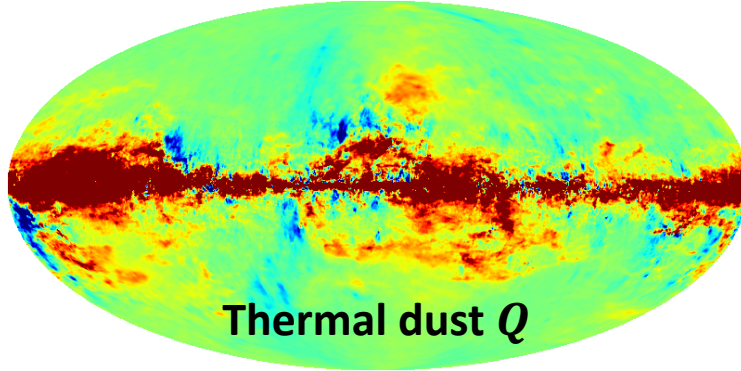
Foregrounds simulation (temperature)



Remazeilles, Ravenni, Chluba, MNRAS 2022

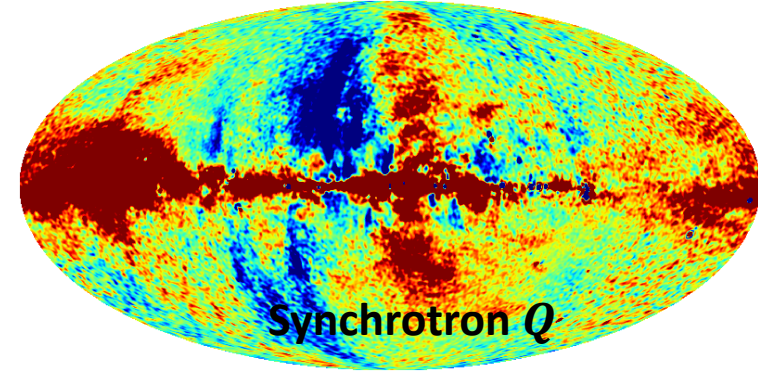
Foregrounds simulation (polarization)

Thermal dust (Q) at 280 GHz



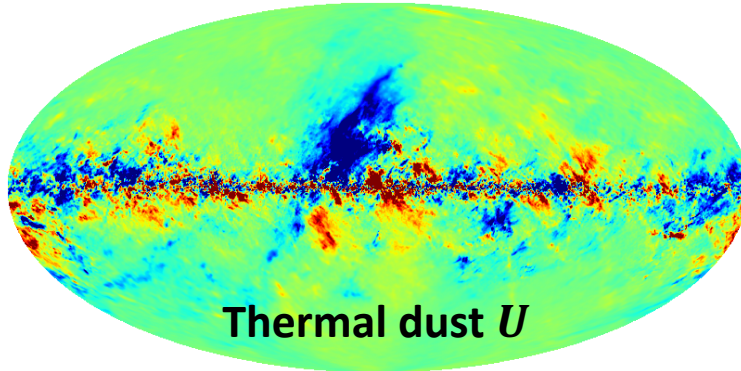
-100 μK_{CMB} 100

Synchrotron (Q) at 280 GHz



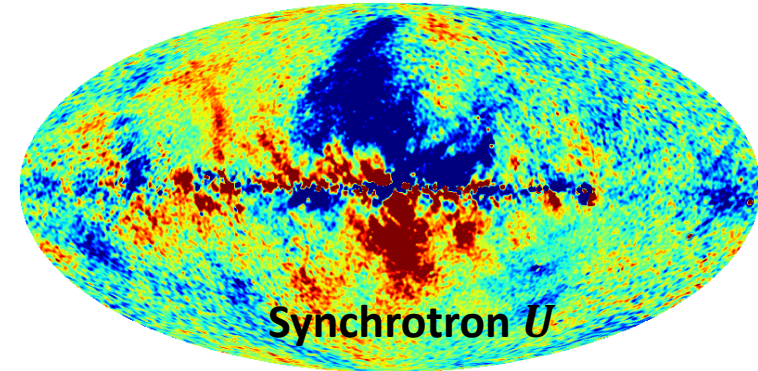
-0.1 μK_{CMB} 0.1

Thermal dust (U) at 280 GHz



-100 μK_{CMB} 100

Synchrotron (U) at 280 GHz

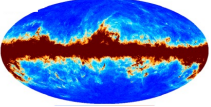


-0.1 μK_{CMB} 0.1

Remazeilles, Ravenni, Chluba, MNRAS 2022

Component separation: standard ILC ?

$$d(\nu, \vec{n}) = \color{red}{a}(\nu)\mu(\vec{n}) + \color{blue}{b}(\nu)T(\vec{n}) + \text{foregrounds}(\nu, \vec{n}) + \text{noise}(\nu, \vec{n})$$

data


μ -distortion
anisotropies

CMB temperature
anisotropies

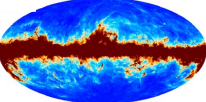
The standard ILC method forms an estimate of the μ -map as

$$\hat{\mu}(\vec{n}) = \sum_{\nu} w(\nu) d(\nu, \vec{n}) \quad \text{such that} \quad \left\{ \begin{array}{l} \langle \hat{\mu}(\vec{n})^2 \rangle \text{ of minimum variance} \\ \sum_{\nu} w(\nu) \color{red}{a}(\nu) = 1 \end{array} \right.$$

Component separation: standard ILC ?

$$d(\boldsymbol{\nu}, \vec{n}) = \color{red}{a}(\boldsymbol{\nu})\mu(\vec{n}) + \color{blue}{b}(\boldsymbol{\nu})T(\vec{n}) + \text{foregrounds}(\boldsymbol{\nu}, \vec{n}) + \text{noise}(\boldsymbol{\nu}, \vec{n})$$

data



↓

*μ-distortion
anisotropies*

↓

*CMB temperature
anisotropies*

The standard ILC method forms an estimate of the μ -map as

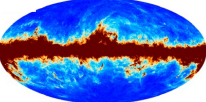
$$\hat{\mu}(\vec{n}) = \sum_{\boldsymbol{\nu}} w(\boldsymbol{\nu}) d(\boldsymbol{\nu}, \vec{n}) \quad \text{such that} \quad \left\{ \begin{array}{l} \langle \hat{\mu}(\vec{n})^2 \rangle \text{ of minimum variance} \\ \sum_{\boldsymbol{\nu}} w(\boldsymbol{\nu}) \color{red}{a}(\boldsymbol{\nu}) = 1 \end{array} \right.$$

$$\hat{\mu}(\vec{n}) = \left(\sum_{\boldsymbol{\nu}} w(\boldsymbol{\nu}) \color{red}{a}(\boldsymbol{\nu}) \right) \mu(\vec{n}) + \left(\sum_{\boldsymbol{\nu}} w(\boldsymbol{\nu}) \color{blue}{b}(\boldsymbol{\nu}) \right) T(\vec{n}) + \dots$$

Component separation: standard ILC ?

$$d(\nu, \vec{n}) = a(\nu)\mu(\vec{n}) + b(\nu)T(\vec{n}) + \text{foregrounds}(\nu, \vec{n}) + \text{noise}(\nu, \vec{n})$$

data



↓

*μ-distortion
anisotropies*

↓

*CMB temperature
anisotropies*

The standard ILC method forms an estimate of the μ -map as

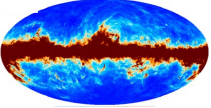
$$\hat{\mu}(\vec{n}) = \sum_{\nu} w(\nu) d(\nu, \vec{n}) \quad \text{such that} \quad \left\{ \begin{array}{l} \langle \hat{\mu}(\vec{n})^2 \rangle \text{ of minimum variance} \\ \sum_{\nu} w(\nu) a(\nu) = 1 \end{array} \right.$$

$$\hat{\mu}(\vec{n}) = \left(\overbrace{\sum_{\nu} w(\nu) a(\nu)}^{=1} \right) \mu(\vec{n}) + \left(\sum_{\nu} w(\nu) b(\nu) \right) T(\vec{n}) + \dots$$

Component separation: standard ILC ?

$$d(\nu, \vec{n}) = \mathbf{a}(\nu) \mu(\vec{n}) + \mathbf{b}(\nu) T(\vec{n}) + \text{foregrounds}(\nu, \vec{n}) + \text{noise}(\nu, \vec{n})$$

data



↓

*μ-distortion
anisotropies*

↓

*CMB temperature
anisotropies*

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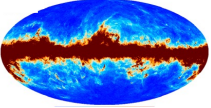
$$\hat{\mu}(\vec{n}) = \sum_{\nu} w(\nu) d(\nu, \vec{n}) \quad \text{such that} \quad \left\{ \begin{array}{l} \langle \hat{\mu}(\vec{n})^2 \rangle \text{ of minimum variance} \\ \sum_{\nu} w(\nu) \mathbf{a}(\nu) = \mathbf{1} \end{array} \right.$$

$$\hat{\mu}(\vec{n}) = \mu(\vec{n}) + \left(\sum_{\nu} w(\nu) \mathbf{b}(\nu) \right) T(\vec{n}) + \dots$$

Component separation: standard ILC ?

$$d(\boldsymbol{\nu}, \vec{n}) = \textcolor{red}{a}(\boldsymbol{\nu})\mu(\vec{n}) + \textcolor{blue}{b}(\boldsymbol{\nu})T(\vec{n}) + \text{foregrounds}(\boldsymbol{\nu}, \vec{n}) + \text{noise}(\boldsymbol{\nu}, \vec{n})$$

data



↓

*μ-distortion
anisotropies*

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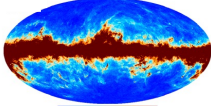
residual CMB anisotropies!

$$\hat{\mu}(\vec{n}) = \mu(\vec{n}) + \underbrace{\left(\sum_{\boldsymbol{\nu}} w(\boldsymbol{\nu}) \textcolor{blue}{b}(\boldsymbol{\nu}) \right) T(\vec{n})}_{\text{residual CMB anisotropies!}} + \dots$$

Component separation: standard ILC ?

$$d(\nu, \vec{n}) = \mathbf{a}(\nu) \mu(\vec{n}) + \mathbf{b}(\nu) T(\vec{n}) + \text{foregrounds}(\nu, \vec{n}) + \text{noise}(\nu, \vec{n})$$

data



↓

*μ-distortion
anisotropies*

↓

*CMB temperature
anisotropies*

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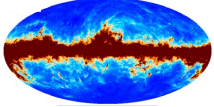
residual CMB anisotropies!

$$\hat{\mu}(\vec{n}) = \mu(\vec{n}) + \underbrace{\left(\sum_{\nu} w(\nu) \mathbf{b}(\nu) \right) T(\vec{n})}_{\text{residual CMB anisotropies!}} + \dots$$

$$\Rightarrow C_{\ell}^{\hat{\mu} \times \hat{T}} = C_{\ell}^{\mu T} + \epsilon C_{\ell}^{TT} + \dots$$

Component separation: standard ILC ?

$$d(\nu, \vec{n}) = \mathbf{a}(\nu) \mu(\vec{n}) + \mathbf{b}(\nu) T(\vec{n}) + \text{foregrounds}(\nu, \vec{n}) + \text{noise}(\nu, \vec{n})$$



data

$\downarrow$
 μ -distortion
anisotropies

$\downarrow$
 CMB temperature
anisotropies

The standard ILC method forms an estimate of the μ -map as

$$\hat{\mu}(\vec{n}) = \sum_{\nu} w(\nu) d(\nu, \vec{n}) \quad \text{such that} \quad \begin{cases} \langle \hat{\mu}(\vec{n})^2 \rangle \text{ of minimum variance} \\ \sum_{\nu} w(\nu) \mathbf{a}(\nu) = \mathbf{1} \end{cases}$$

residual CMB anisotropies!

$$\hat{\mu}(\vec{n}) = \mu(\vec{n}) + \left(\sum_{\nu} w(\nu) \mathbf{b}(\nu) \right) T(\vec{n}) + \dots$$

$$\Rightarrow C_{\ell}^{\hat{\mu} \times \hat{T}} = C_{\ell}^{\mu T} + \underbrace{\varepsilon C_{\ell}^{TT}}_{\text{residual } TT \text{ correlations!}} + \dots$$

Component separation: constrained ILC !

$$\underset{\substack{\text{data} \\ \img alt="A map of the CMB showing temperature anisotropies." data-bbox="174 245 256 318}}{d(\boldsymbol{\nu}, \vec{n})} = \underset{\substack{\mu\text{-distortion} \\ \text{anisotropies}}}{\boldsymbol{a}(\boldsymbol{\nu})\boldsymbol{\mu}(\vec{n})} + \underset{\substack{\text{CMB temperature} \\ \text{anisotropies}}}{\boldsymbol{b}(\boldsymbol{\nu})\boldsymbol{T}(\vec{n})} + \text{foregrounds}(\boldsymbol{\nu}, \vec{n}) + \text{noise}(\boldsymbol{\nu}, \vec{n})$$

The standard ILC **constrained ILC** method forms an estimate of the μ -map as

$$\hat{\boldsymbol{\mu}}(\vec{n}) = \sum_{\boldsymbol{\nu}} \boldsymbol{w}(\boldsymbol{\nu}) d(\boldsymbol{\nu}, \vec{n}) \quad \text{such that} \quad \left\{ \begin{array}{l} \langle \hat{\boldsymbol{\mu}}(\vec{n})^2 \rangle \text{ of minimum variance} \\ \sum_{\boldsymbol{\nu}} \boldsymbol{w}(\boldsymbol{\nu}) \boldsymbol{a}(\boldsymbol{\nu}) = \mathbf{1} \\ \sum_{\boldsymbol{\nu}} \boldsymbol{w}(\boldsymbol{\nu}) \boldsymbol{b}(\boldsymbol{\nu}) = \mathbf{0} \end{array} \right.$$

Component separation: constrained ILC !

$$\underset{\substack{\text{data} \\ \text{CMB map}}} {d(\boldsymbol{\nu}, \vec{n})} = \underset{\substack{\mu\text{-distortion} \\ \text{anisotropies}}} {\boldsymbol{a}(\boldsymbol{\nu})\boldsymbol{\mu}(\vec{n})} + \underset{\substack{\text{CMB temperature} \\ \text{anisotropies}}} {\boldsymbol{b}(\boldsymbol{\nu})\boldsymbol{T}(\vec{n})} + \text{foregrounds}(\boldsymbol{\nu}, \vec{n}) + \text{noise}(\boldsymbol{\nu}, \vec{n})$$

The standard ILC **constrained ILC** method forms an estimate of the μ -map as

$$\hat{\boldsymbol{\mu}}(\vec{n}) = \sum_{\boldsymbol{\nu}} \boldsymbol{w}(\boldsymbol{\nu}) d(\boldsymbol{\nu}, \vec{n}) \quad \text{such that} \quad \left\{ \begin{array}{l} \langle \hat{\boldsymbol{\mu}}(\vec{n})^2 \rangle \text{ of minimum variance} \\ \sum_{\boldsymbol{\nu}} \boldsymbol{w}(\boldsymbol{\nu}) \boldsymbol{a}(\boldsymbol{\nu}) = \mathbf{1} \\ \sum_{\boldsymbol{\nu}} \boldsymbol{w}(\boldsymbol{\nu}) \boldsymbol{b}(\boldsymbol{\nu}) = \mathbf{0} \end{array} \right.$$

Extra constraint to guarantee the cancellation of residual CMB anisotropies

Component separation: constrained ILC !

$$d(\nu, \vec{n}) = \underset{\substack{\text{data} \\ \text{CMB map}}} {\color{blue}d}(\nu, \vec{n}) = \color{red}{a}(\nu) \underset{\substack{\mu\text{-distortion} \\ \text{anisotropies}}} {\mu}(\vec{n}) + \color{blue}{b}(\nu) \underset{\substack{\text{CMB temperature} \\ \text{anisotropies}}} {T}(\vec{n}) + \text{foregrounds}(\nu, \vec{n}) + \text{noise}(\nu, \vec{n})$$

The standard ILC **constrained ILC** method forms an estimate of the μ -map as

$$\hat{\mu}(\vec{n}) = \sum_{\nu} w(\nu) d(\nu, \vec{n}) \quad \text{such that} \quad \left\{ \begin{array}{l} \langle \hat{\mu}(\vec{n})^2 \rangle \text{ of minimum variance} \\ \sum_{\nu} w(\nu) \color{red}{a}(\nu) = 1 \\ \sum_{\nu} w(\nu) \color{blue}{b}(\nu) = 0 \end{array} \right.$$

$$\hat{\mu}(\vec{n}) = \mu(\vec{n}) + \overbrace{\left(\sum_{\nu} w(\nu) \color{blue}{b}(\nu) \right)}^{=0} T(\vec{n}) + \dots$$

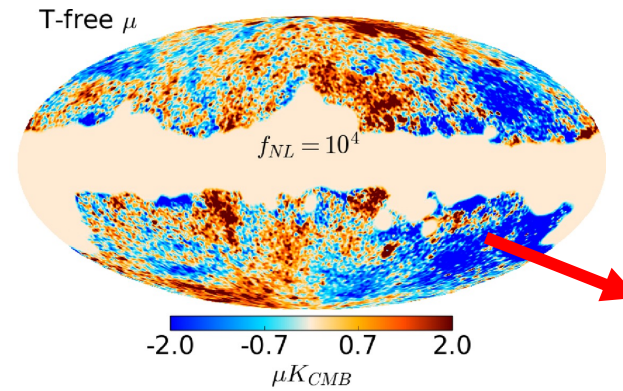
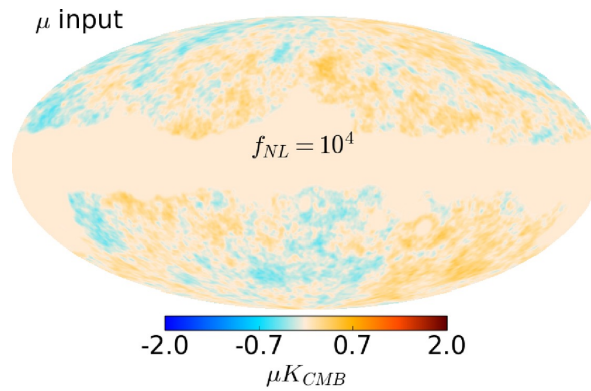
$$\Rightarrow C_{\ell}^{\hat{\mu} \times T} = C_{\ell}^{\mu \times T} + \cancel{\varepsilon C_{\ell}^{TT}} + \dots$$

*Zero residual
TT correlation!*

Results

μ -map reconstruction with Constrained ILC

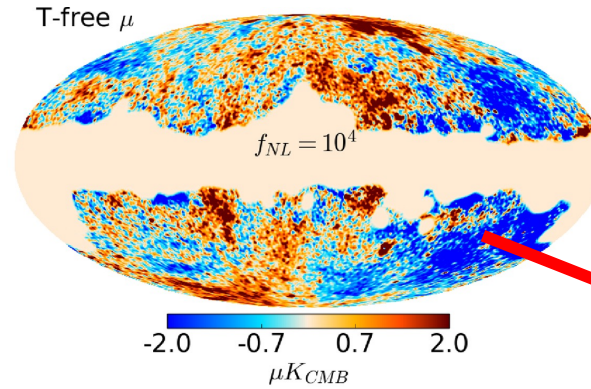
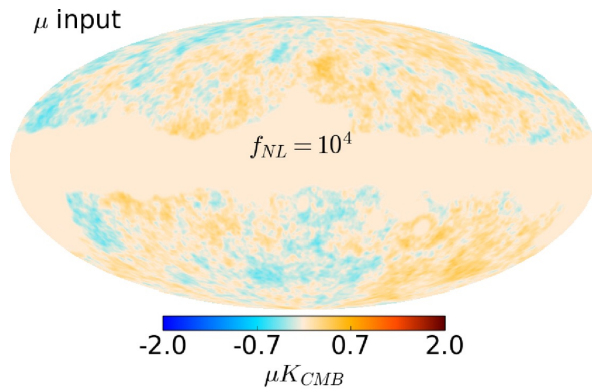
$$f_{\text{NL}}^{\mu} = 10^4$$



significant foreground
contamination

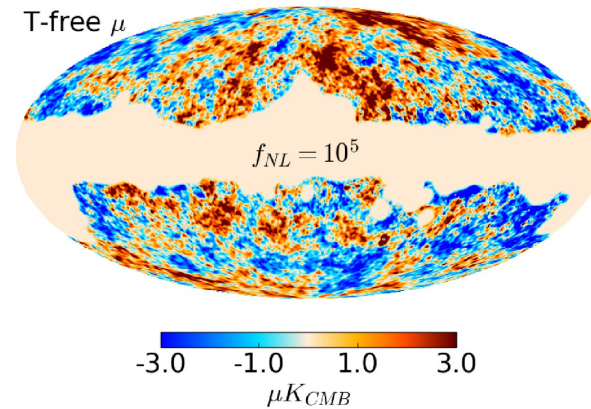
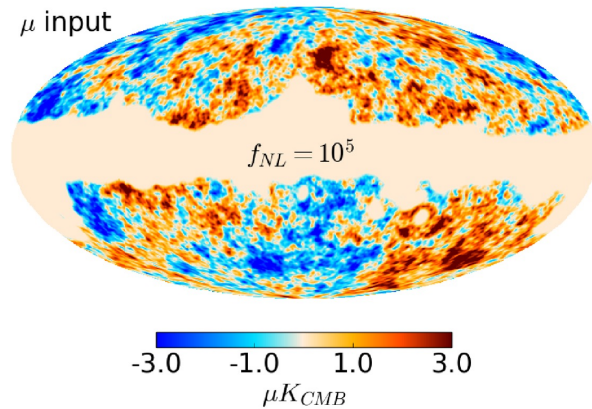
μ -map reconstruction with Constrained ILC

$$f_{\text{NL}}^{\mu} = 10^4$$



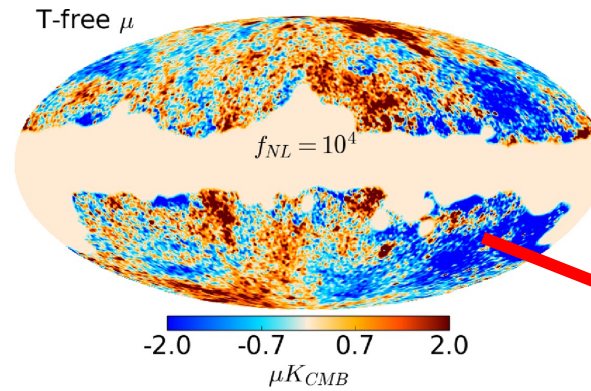
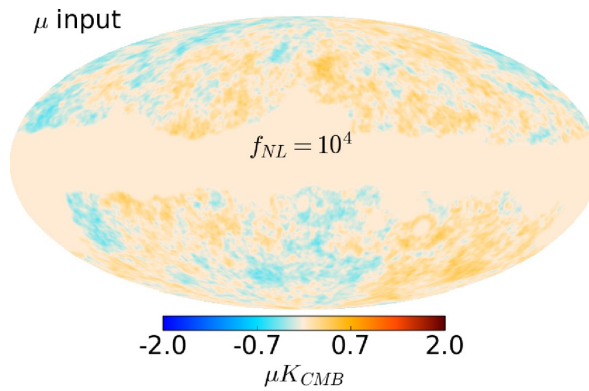
significant foreground
contamination

$$f_{\text{NL}}^{\mu} = 10^5$$



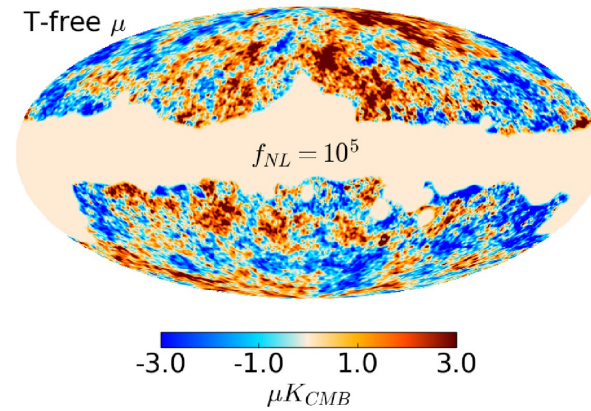
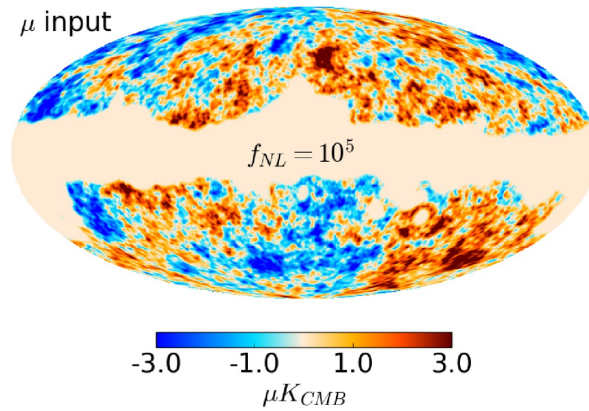
μ -map reconstruction with Constrained ILC

$$f_{\text{NL}}^{\mu} = 10^4$$

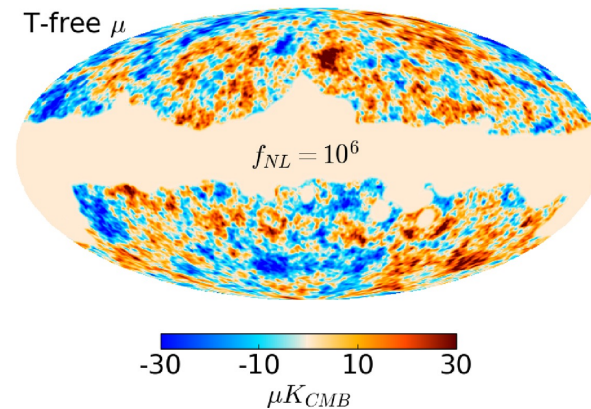
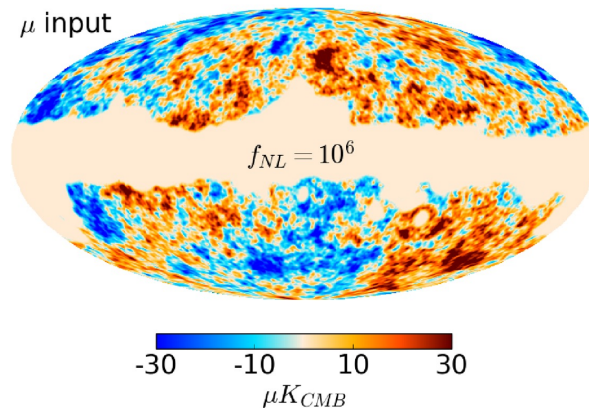


significant foreground
contamination

$$f_{\text{NL}}^{\mu} = 10^5$$

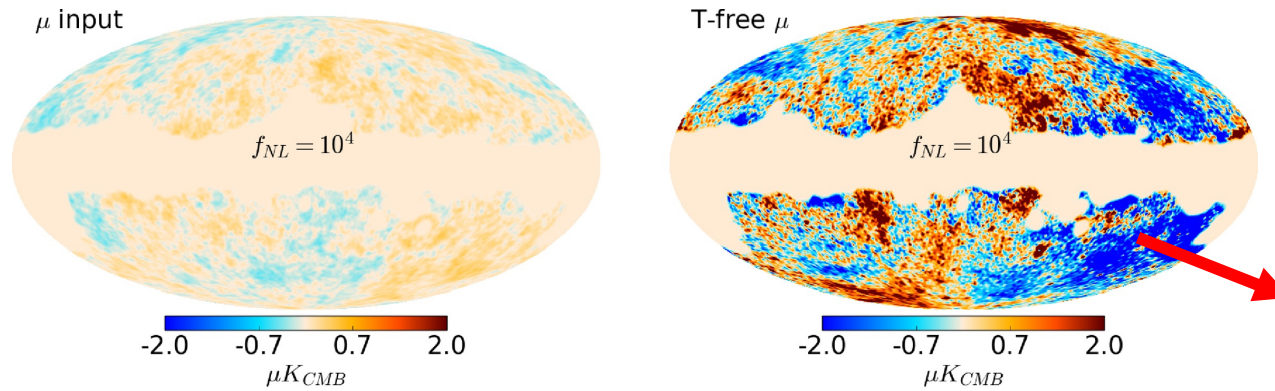


$$f_{\text{NL}}^{\mu} = 10^6$$

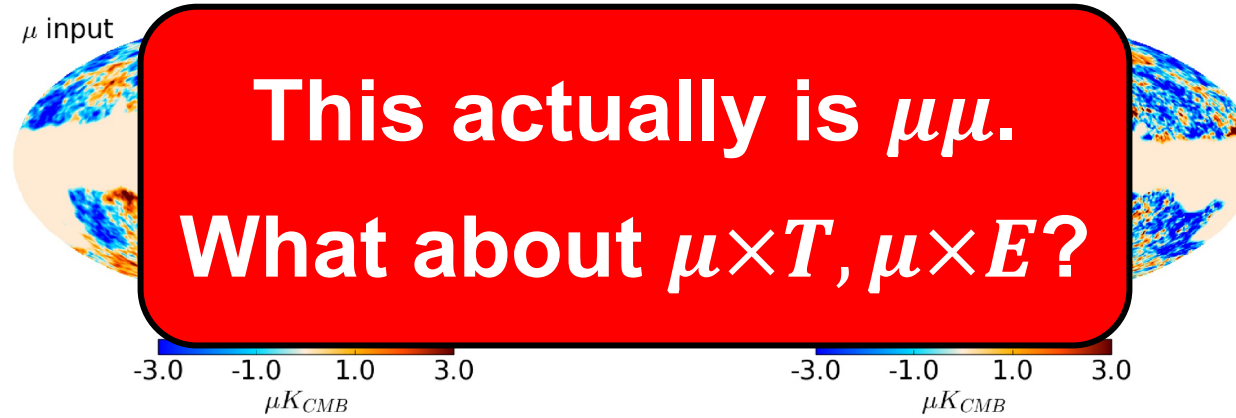


μ -map reconstruction with Constrained ILC

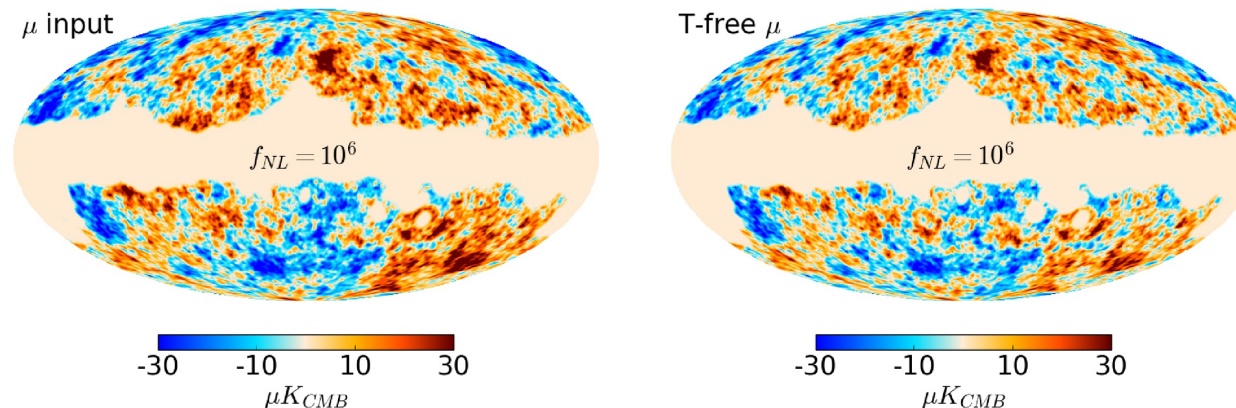
$$f_{\text{NL}}^{\mu} = 10^4$$



$$f_{\text{NL}}^{\mu} = 10^5$$



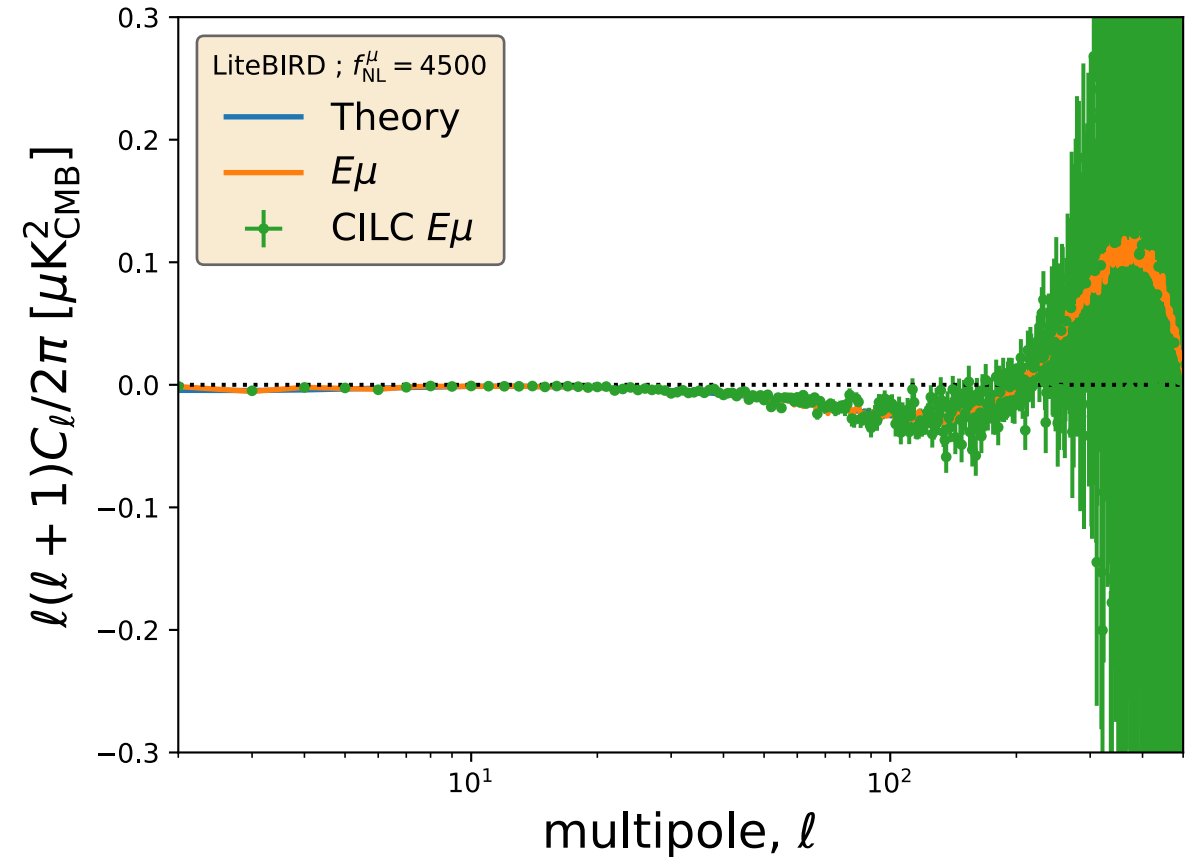
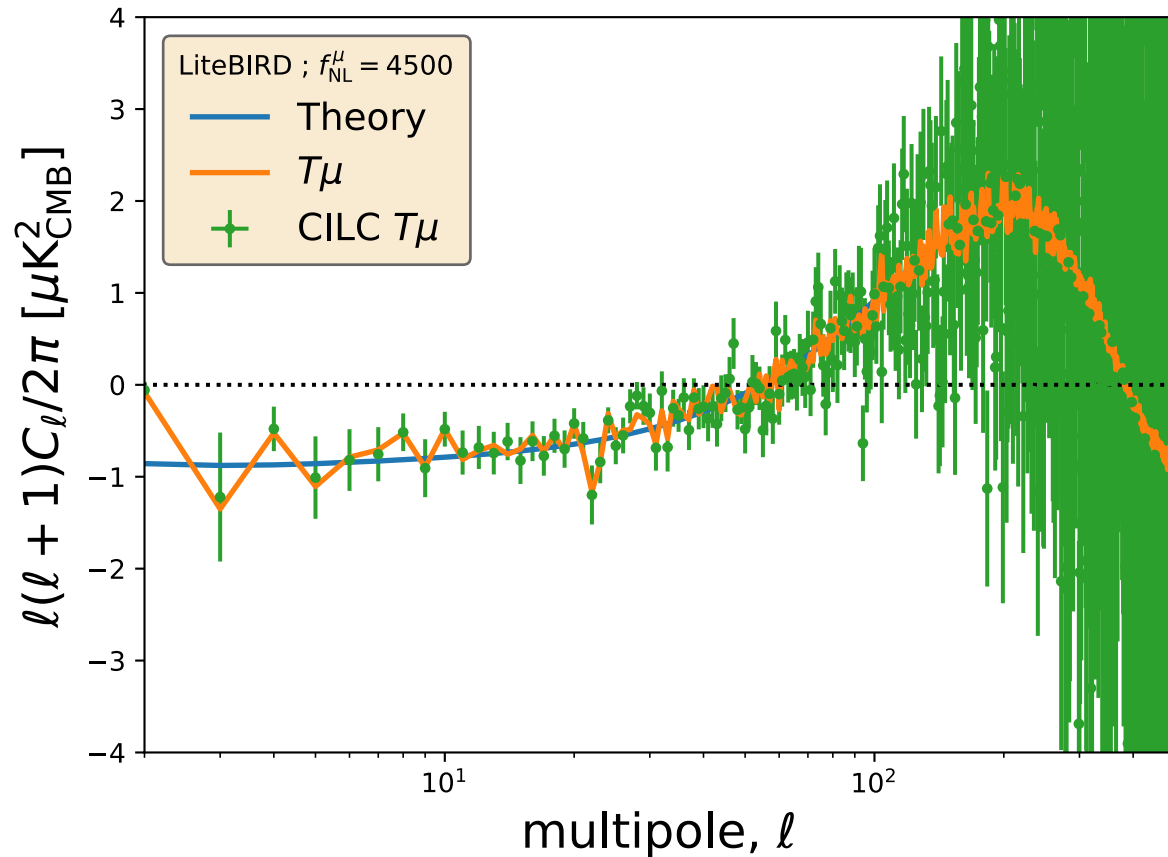
$$f_{\text{NL}}^{\mu} = 10^6$$



No binning

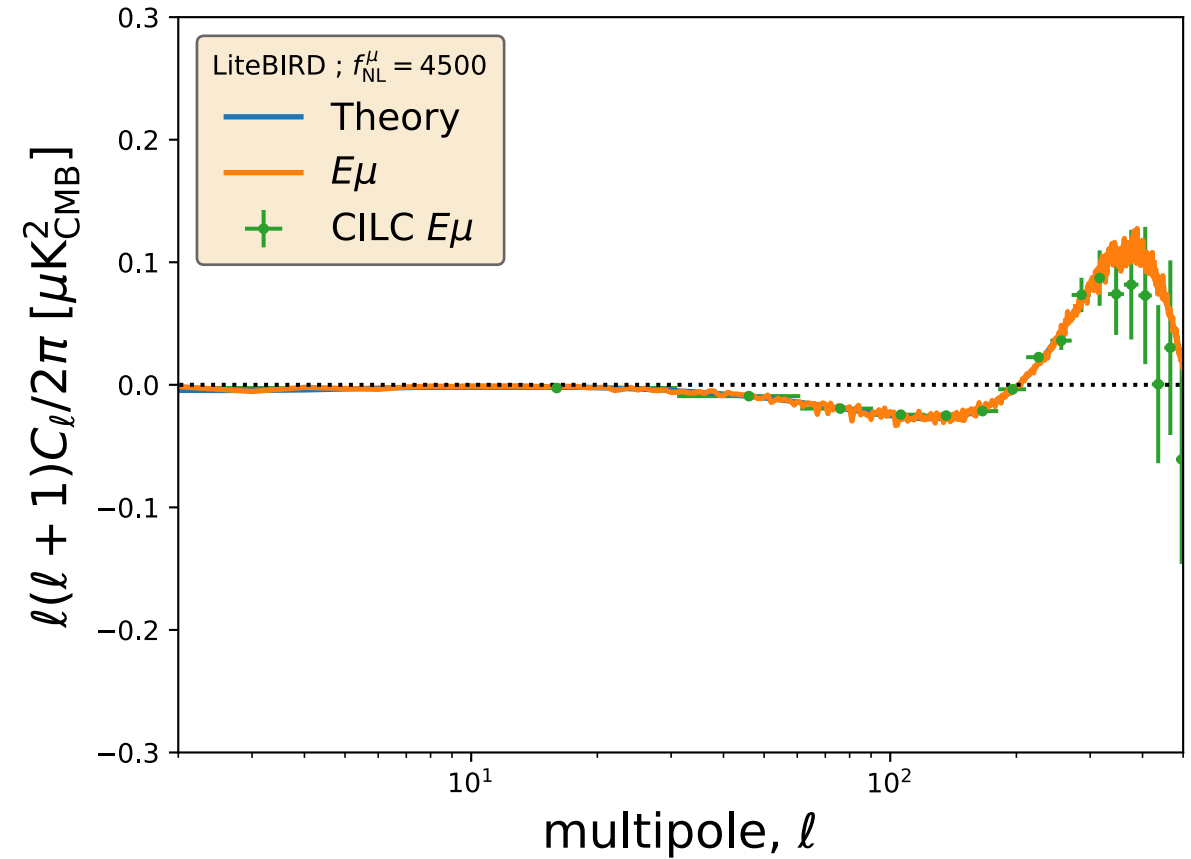
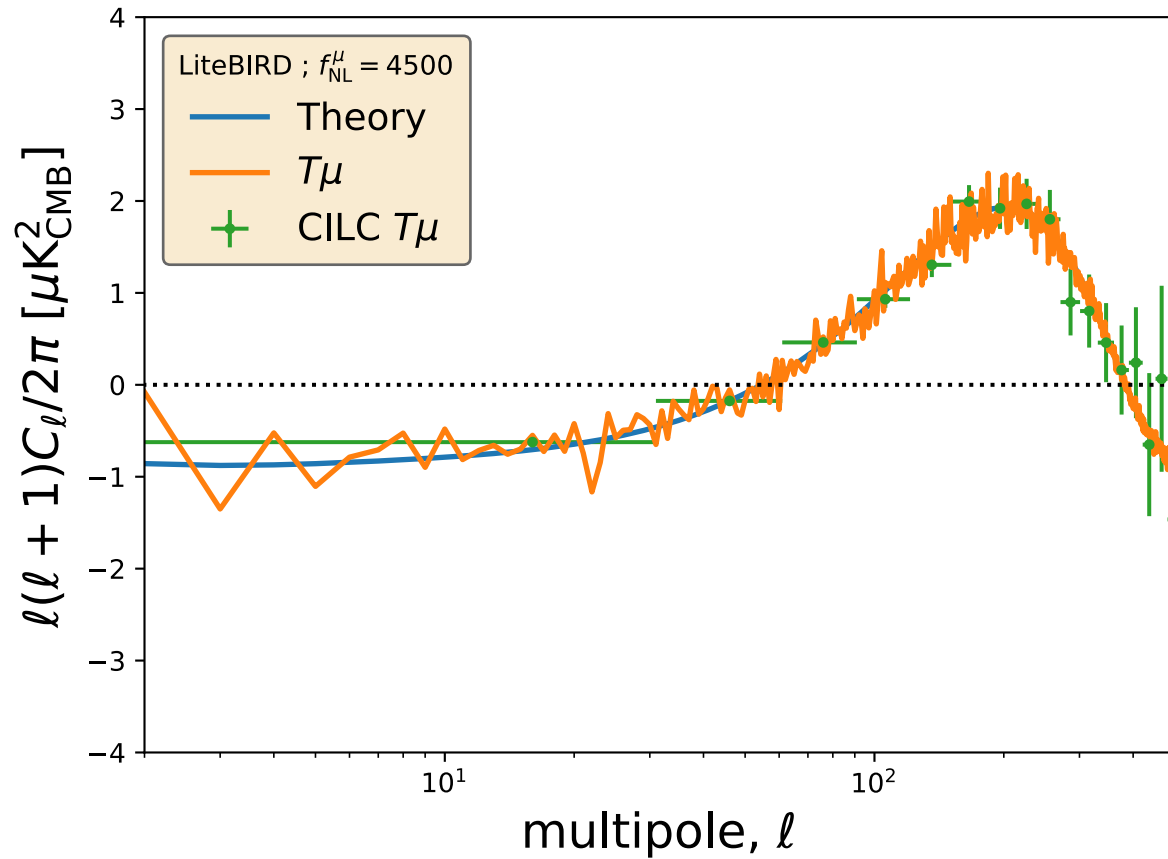
LiteBIRD, $f_{NL}^{\mu} = 4500$ without foregrounds

Remazeilles,
Ravenni, Chluba
MNRAS 2022

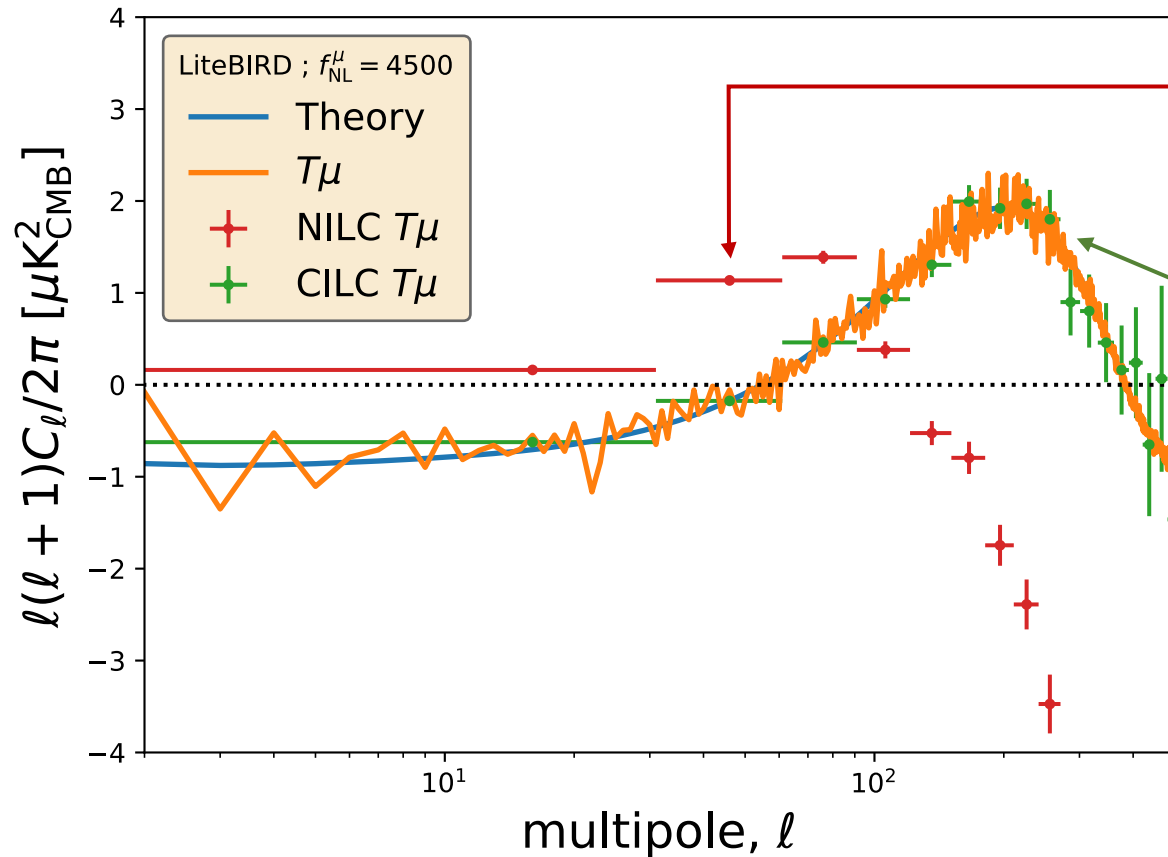


LiteBIRD, $f_{NL}^{\mu} = 4500$ without foregrounds

Remazeilles,
Ravenni, Chluba
MNRAS 2022



Standard ILC vs Constrained ILC



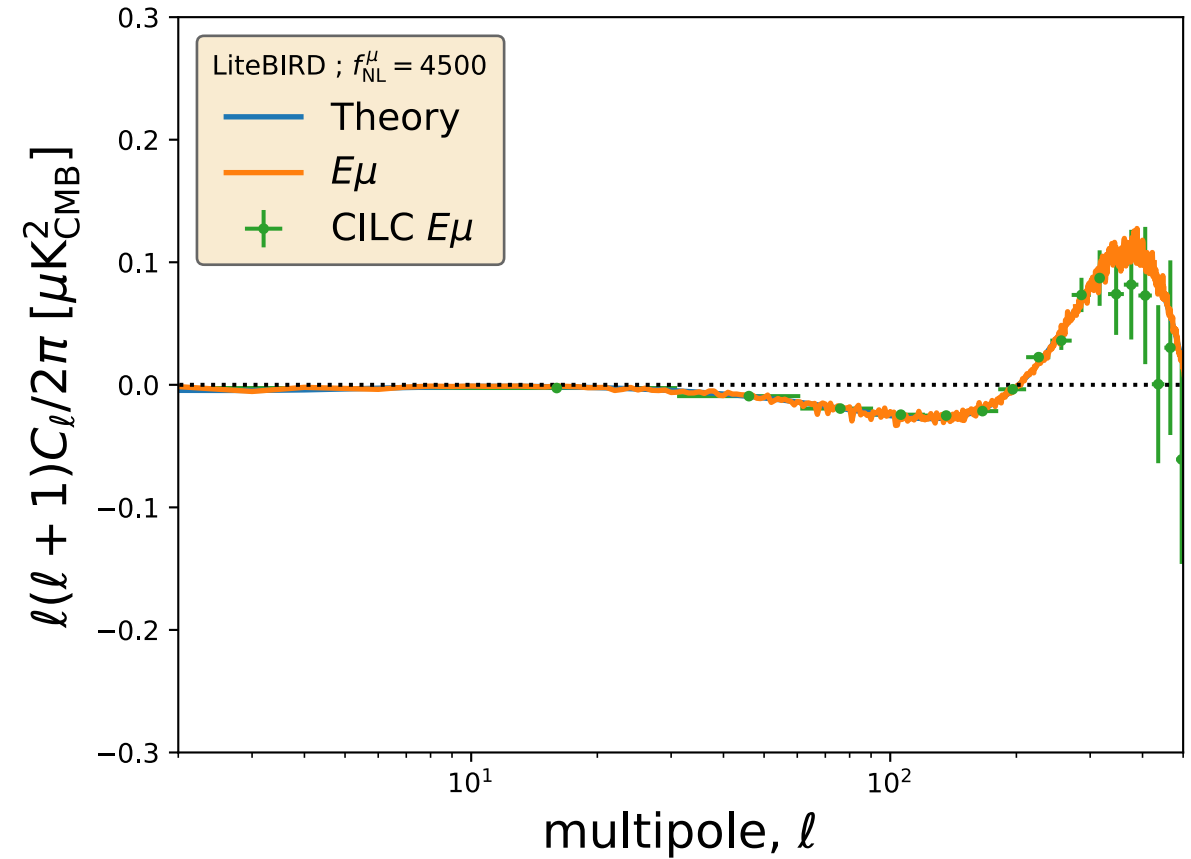
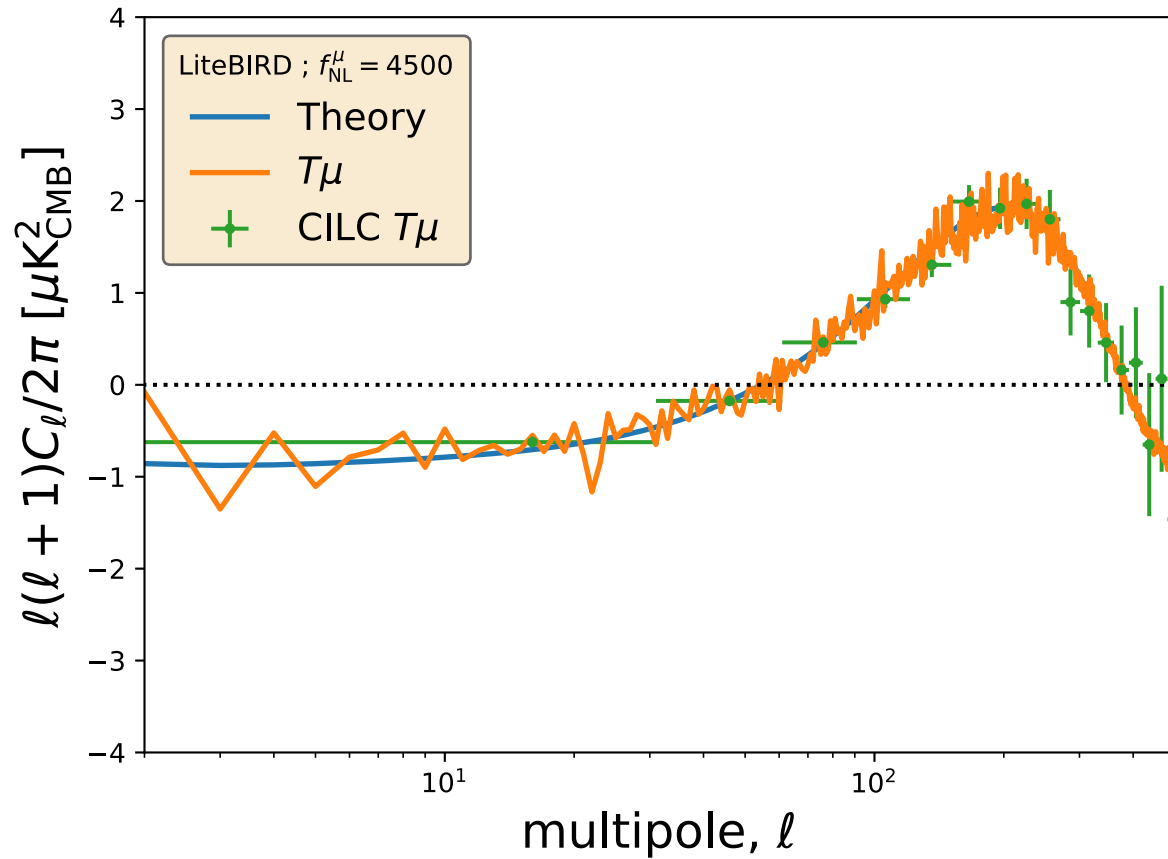
Standard ILC methods suffer from spurious TT correlations due to residual CMB anisotropies in the μ -map

The Constrained ILC fully recovers the correlated μT signal without bias

Remazeilles, Ravenni, Chluba, MNRAS 2022
Remazeilles & Chluba, MNRAS 2018

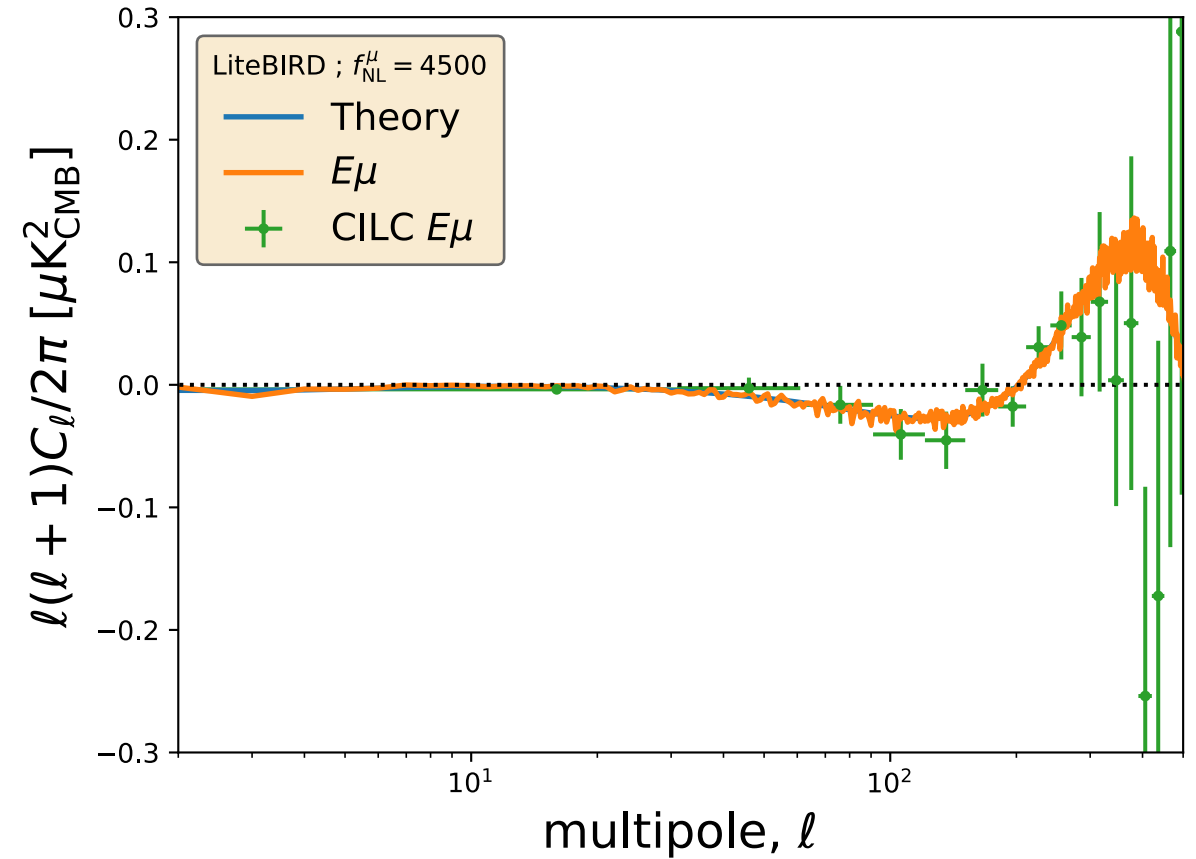
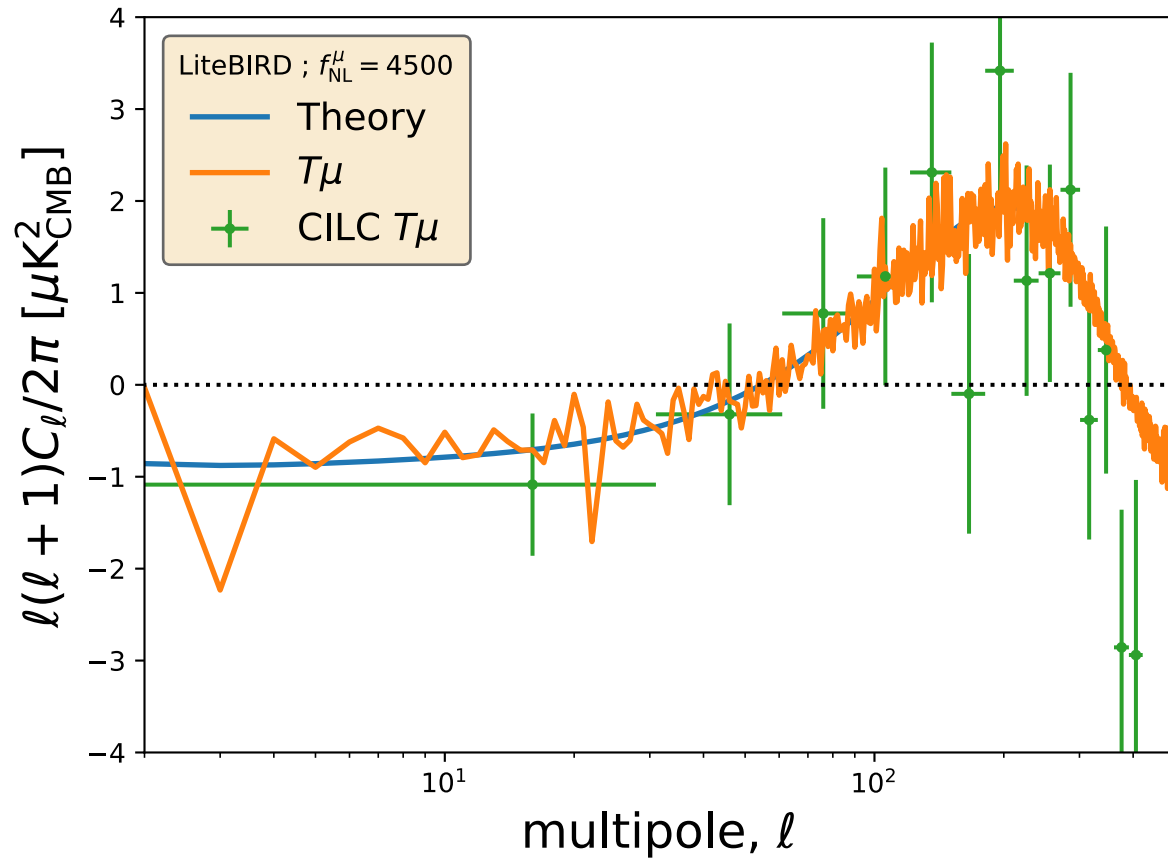
LiteBIRD, $f_{NL}^{\mu} = 4500$ without foregrounds

Remazeilles,
Ravenni, Chluba
MNRAS 2022



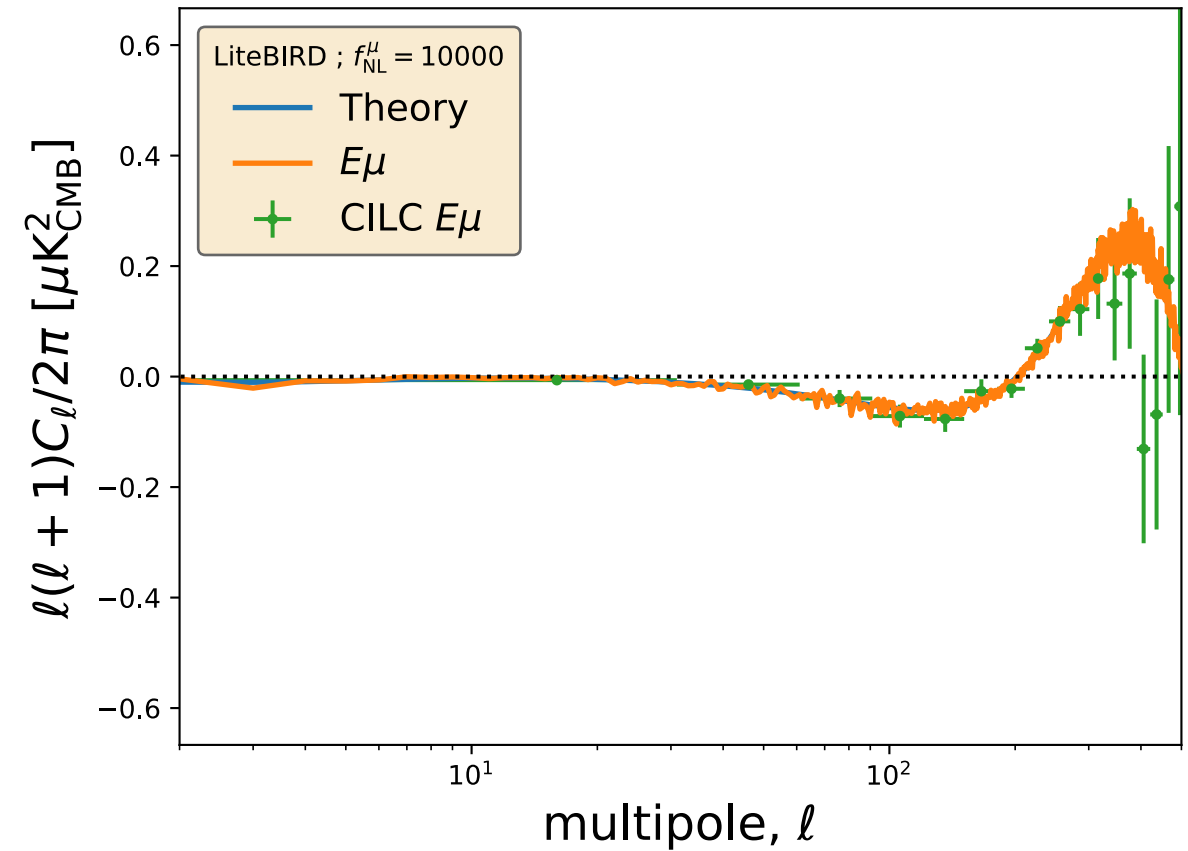
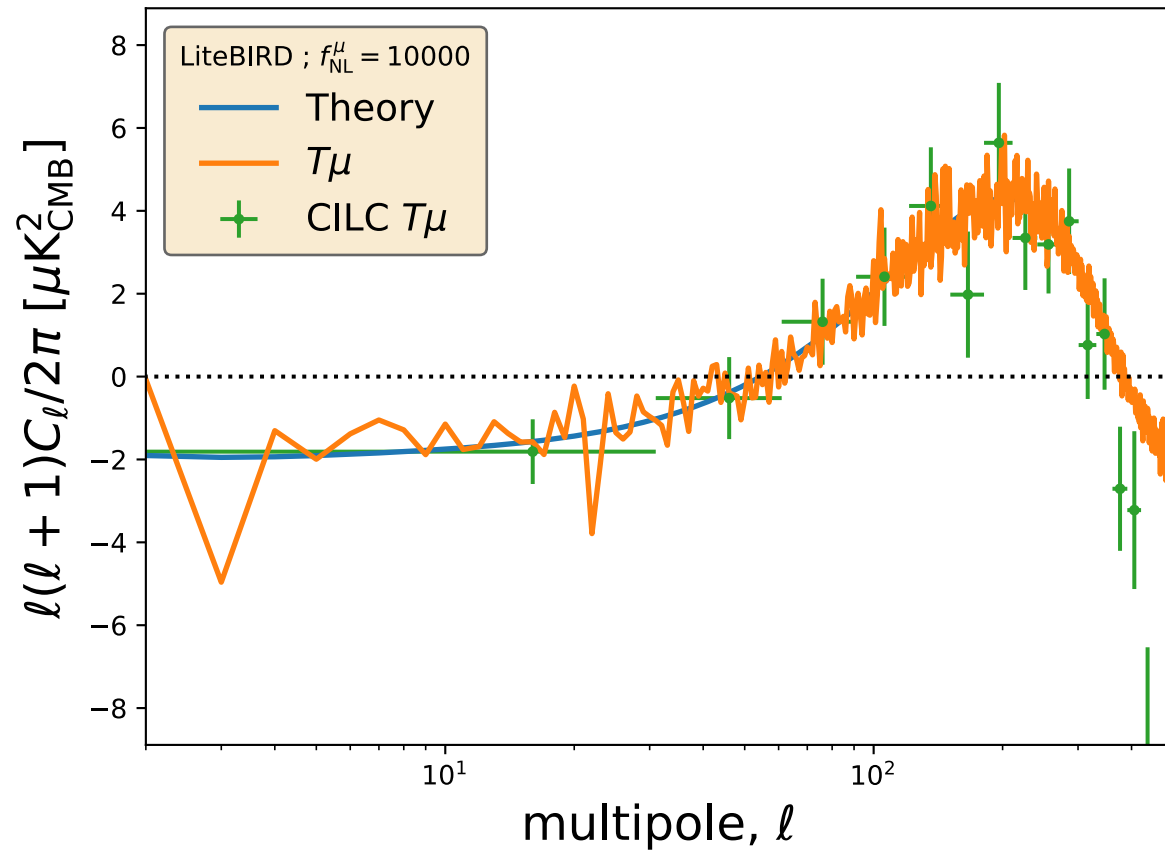
LiteBIRD, $f_{NL}^{\mu} = 4500$ with foregrounds

Remazeilles,
Ravenni, Chluba
MNRAS 2022



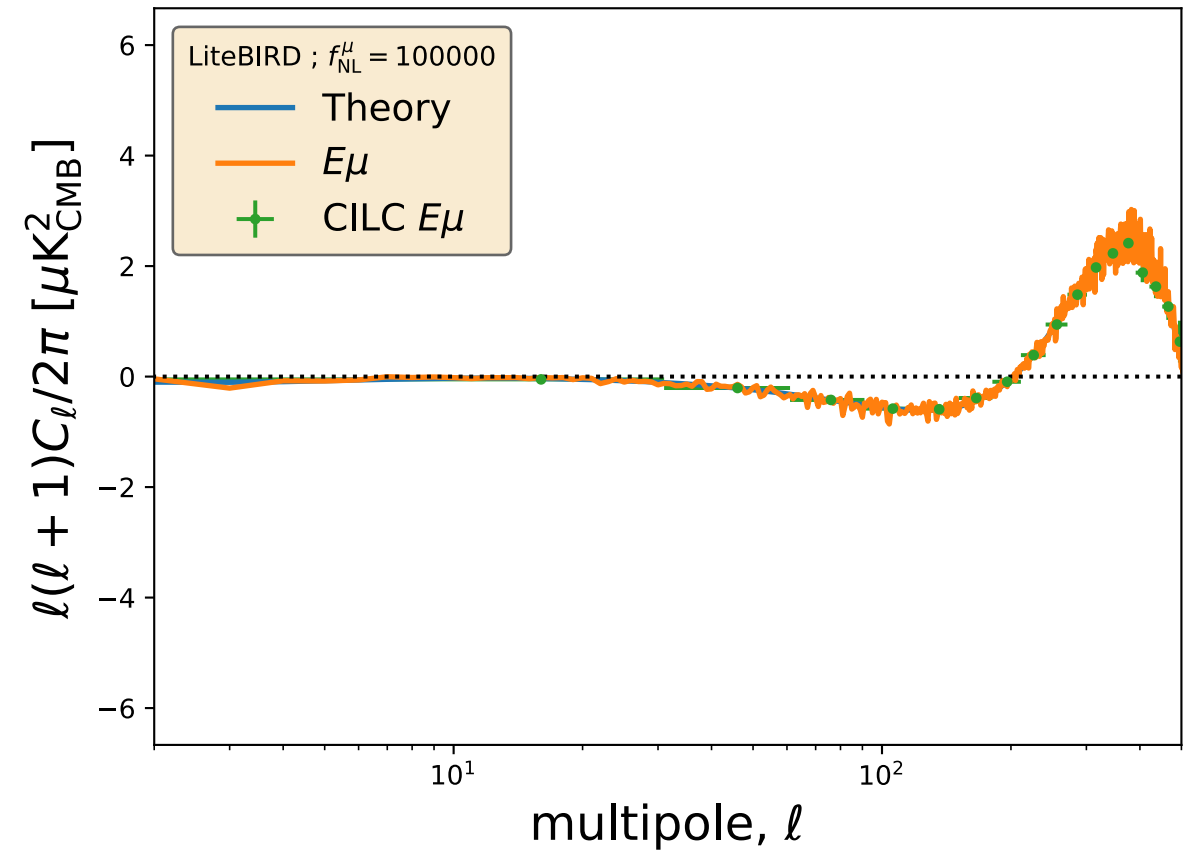
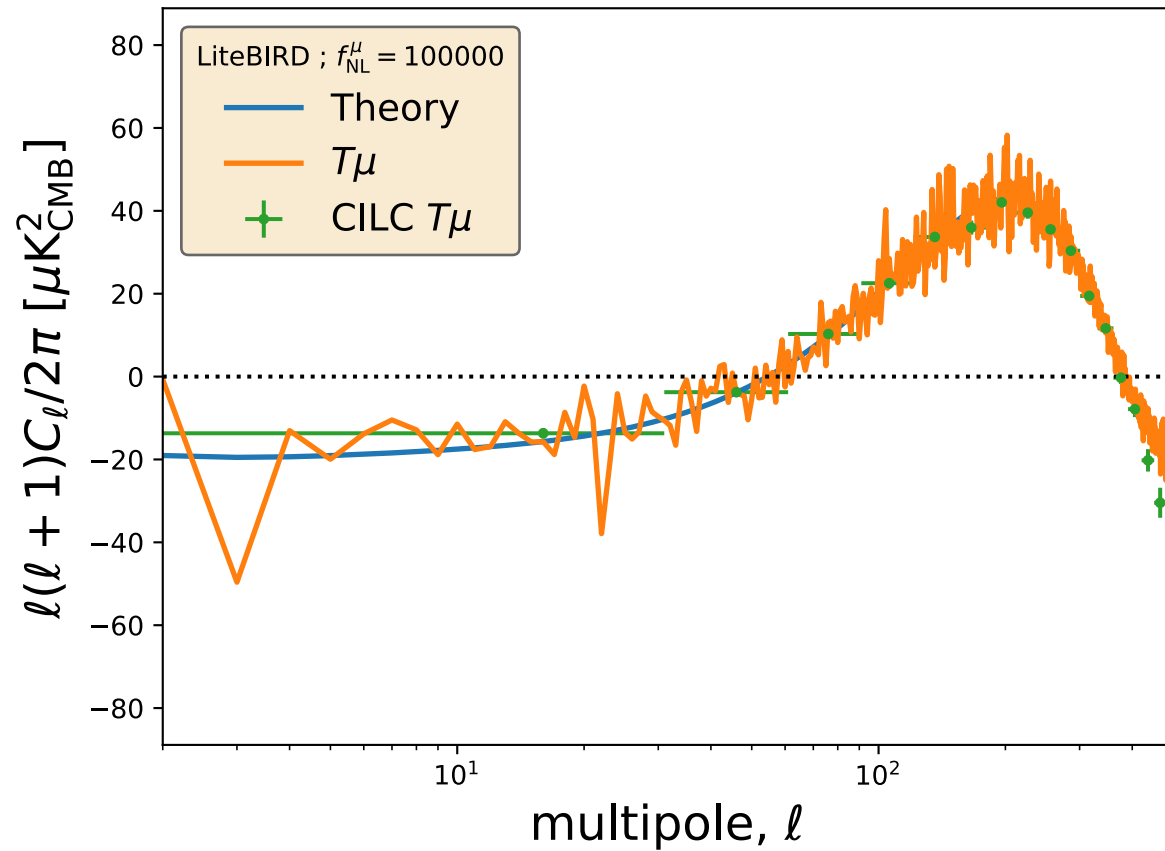
LiteBIRD, $f_{NL}^{\mu} = 10^4$ with foregrounds

Remazeilles,
Ravenni, Chluba
MNRAS 2022



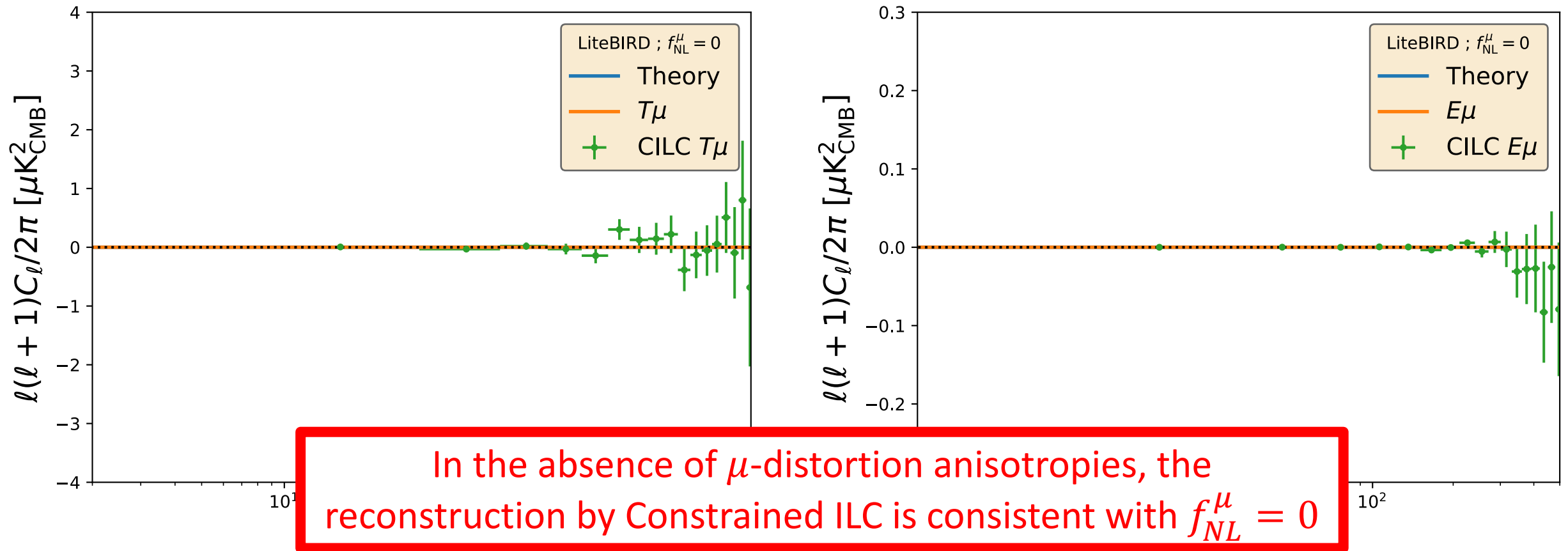
LiteBIRD, $f_{NL}^{\mu} = 10^5$ with foregrounds

Remazeilles,
Ravenni, Chluba
MNRAS 2022



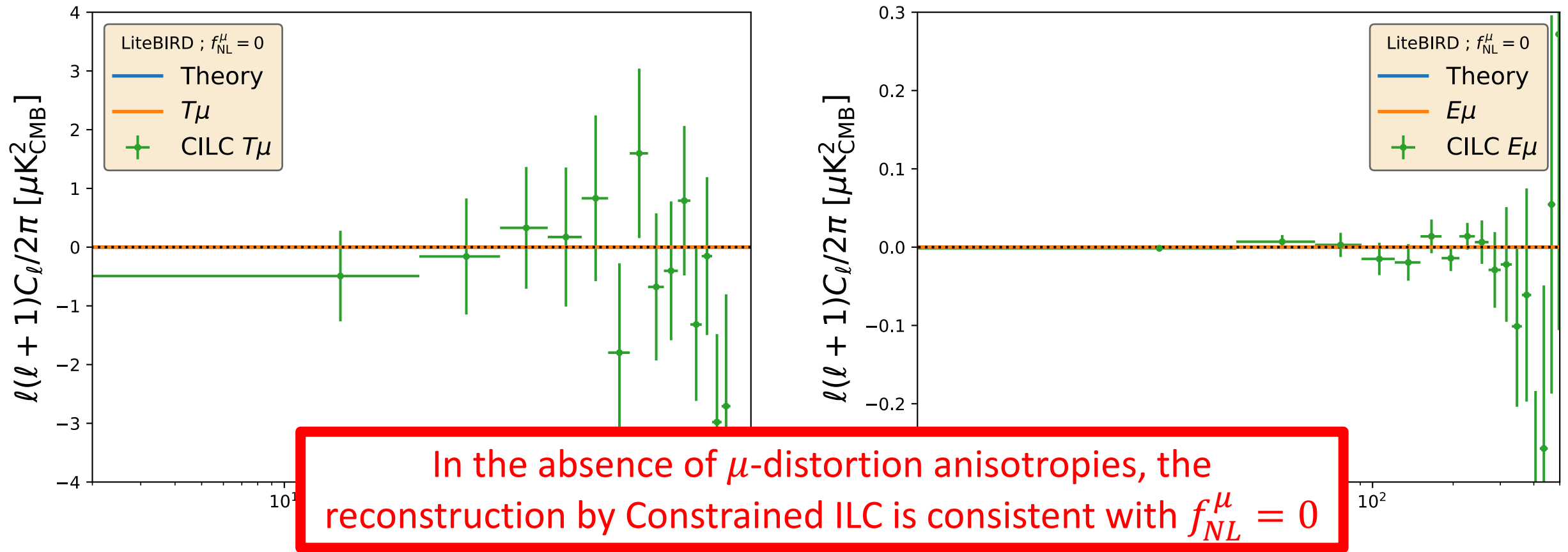
LiteBIRD null test, $f_{NL}^\mu = 0$ without foregrounds

Remazeilles,
Ravenni, Chluba
MNRAS 2022



LiteBIRD null test, $f_{NL}^{\mu} = 0$ with foregrounds

Remazeilles,
Ravenni, Chluba
MNRAS 2022



Forecasts on $f_{NL}^{\mu} (k \simeq 740 \text{ Mpc}^{-1})$

$\mu \times T$

Remazeilles, Ravenni, Chluba, MNRAS 2022

LiteBIRD simulation

f_{NL}^{μ} (fiducial)	10^5	10^4	4500	0	4500 (w/o foregrounds)	0 (w/o foregrounds)
$\mu \times T$	$(0.97 \pm 0.02) \times 10^5$ [50 σ]	$(1.05 \pm 0.12) \times 10^4$ [8 σ]	5264 ± 1286 [3.5 σ]	951 ± 1286 -	4348 ± 152 [30 σ]	8.2 ± 103 -

Forecasts on $f_{NL}^\mu (k \simeq 740 \text{ Mpc}^{-1})$

$\mu \times T$

Remazeilles, Ravenni, Chluba, MNRAS 2022

LiteBIRD simulation

f_{NL}^μ (fiducial)	10^5	10^4	4500	0	4500 (w/o foregrounds)	0 (w/o foregrounds)
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Foregrounds degrade the sensitivity to f_{NL}^μ by about a factor of 10

Forecasts on f_{NL}^{μ} ($k \simeq 740 \text{ Mpc}^{-1}$)

$\mu \times E$

Remazeilles, Ravenni, Chluba, MNRAS 2022

LiteBIRD simulation

f_{NL}^{μ} (fiducial)	10^5	10^4	4500	0	4500 (w/o foregrounds)	0 (w/o foregrounds)
$\mu \times T$	$(0.97 \pm 0.02) \times 10^5$ [50 σ]	$(1.05 \pm 0.12) \times 10^4$ [8 σ]	5264 ± 1286 [3.5 σ]	951 ± 1286 -	4348 ± 152 [30 σ]	8.2 ± 103 -
$\mu \times E$	$(0.96 \pm 0.01) \times 10^5$ [100 σ]	$(0.91 \pm 0.11) \times 10^4$ [9 σ]	3779 ± 1089 [4 σ]	-534 ± 1084 -	4366 ± 108 [42 σ]	0.9 ± 76 -

μE provides more constraining power than μT on f_{NL}^{μ}

Forecasts on f_{NL}^{μ} ($k \simeq 740 \text{ Mpc}^{-1}$)

$\mu \times T, E$ (joint)

Remazeilles, Ravenni, Chluba, MNRAS 2022

LiteBIRD simulation

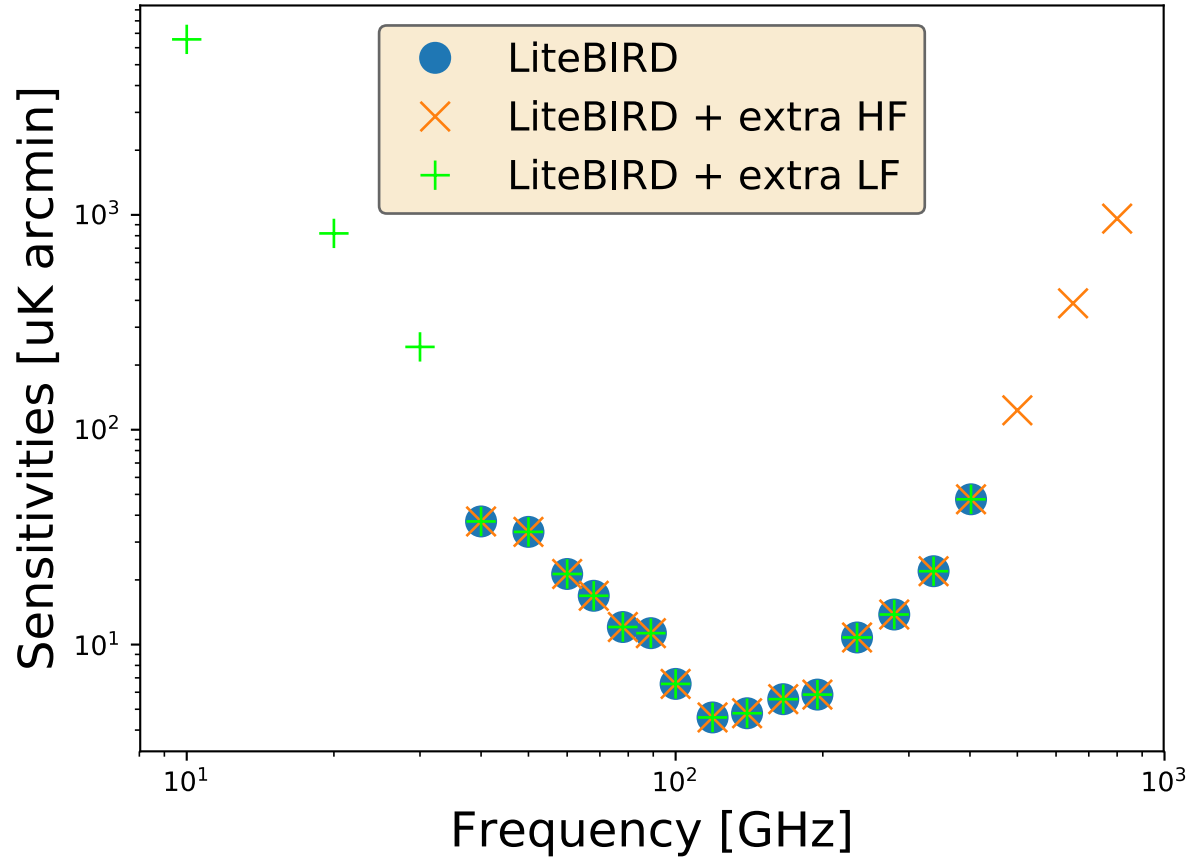
f_{NL}^{μ} (fiducial)	10^5	10^4	4500	0	4500 (w/o foregrounds)	0 (w/o foregrounds)
$\mu \times T$	$(0.97 \pm 0.02) \times 10^5$ [50 σ]	$(1.05 \pm 0.12) \times 10^4$ [8 σ]	5264 ± 1286 [3.5 σ]	951 ± 1286 -	4348 ± 152 [30 σ]	8.2 ± 103 -
$\mu \times E$	$(0.96 \pm 0.01) \times 10^5$ [100 σ]	$(0.91 \pm 0.11) \times 10^4$ [9 σ]	3779 ± 1089 [4 σ]	-534 ± 1084 -	4366 ± 108 [42 σ]	0.9 ± 76 -
$\mu \times T, E$ (joint)	$(0.97 \pm 0.01) \times 10^5$ [100 σ]	$(0.97 \pm 0.08) \times 10^4$ [11 σ]	4425 ± 827 [5 σ]	95 ± 824 -	4329 ± 90 [48 σ]	-2.8 ± 62 -

LiteBIRD: 5σ detection of $f_{NL}^{\mu} = 4500$ after foreground cleaning

LiteBIRD: $\sigma(f_{NL}^{\mu} = 0) \lesssim 800$ in the presence of foregrounds

Focal plane optimization for μ -distortion anisotropies?

Optimization of focal plane for μ anisotropies?

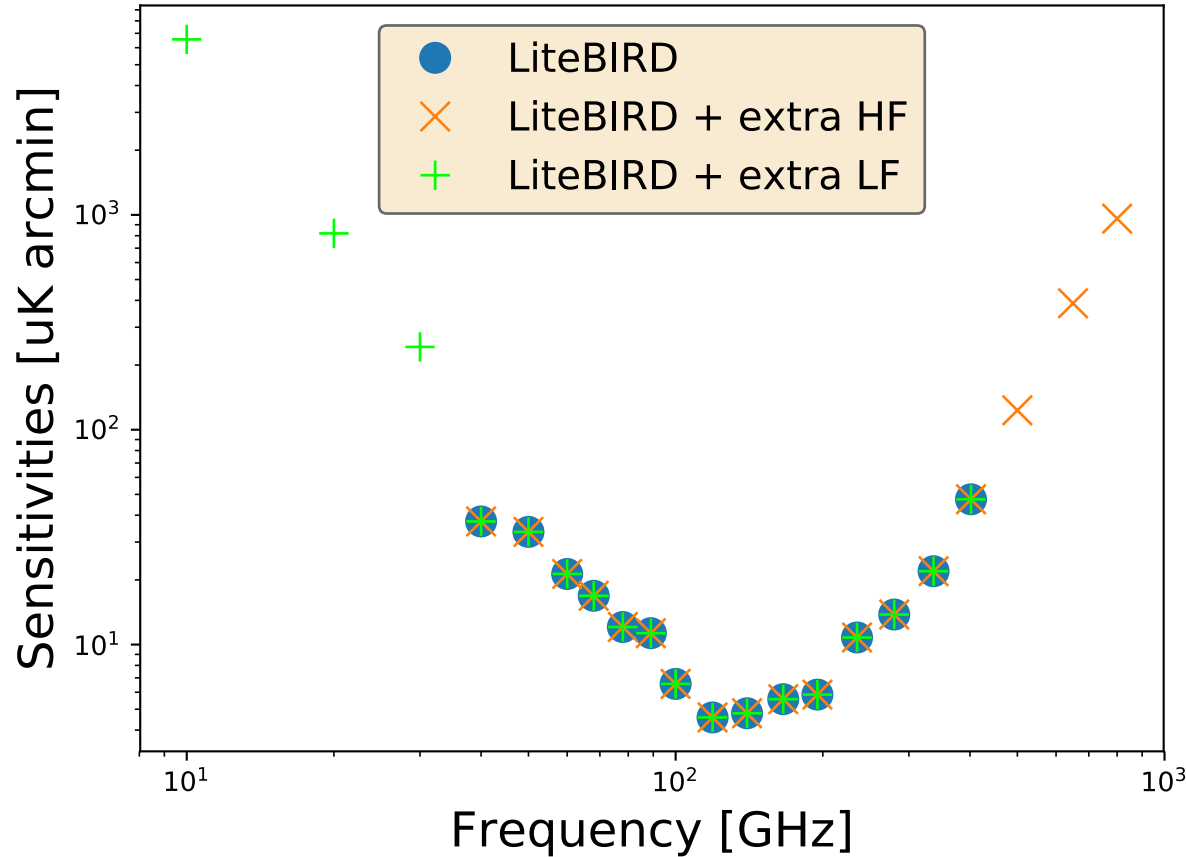


Combined sensitivity of all frequency channels:

$$\sigma = \left(\sum_{i=1}^N \frac{1}{\sigma_i^2} \right)^{-1/2}$$

σ_{LB} VS $\sigma_{\text{LB+HF}}$ VS $\sigma_{\text{LB+LF}}$?

Optimization of focal plane for μ anisotropies?



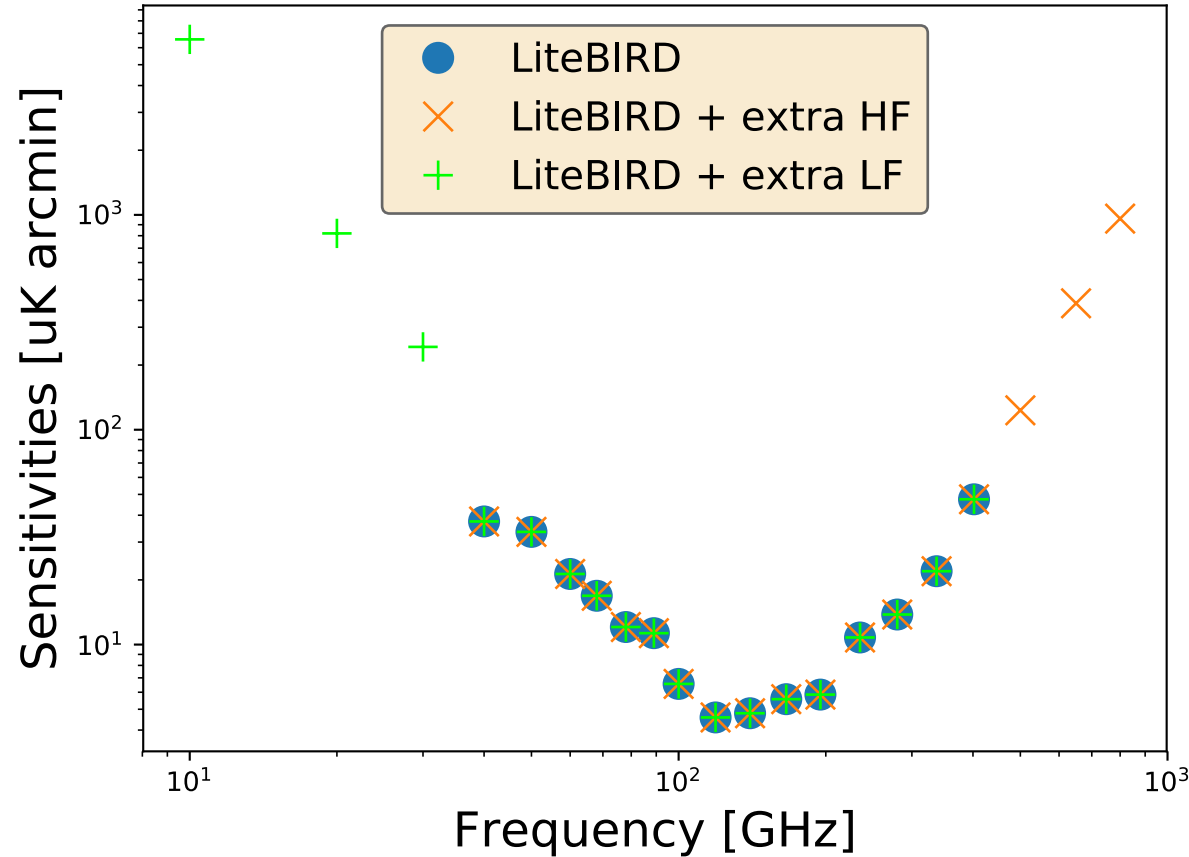
Combined sensitivity of all frequency channels:

$$\sigma = \left(\sum_{i=1}^N \frac{1}{\sigma_i^2} \right)^{-1/2}$$

This is the sensitivity to the **achromatic CMB signal**

Equivalently, ILC noise RMS for CMB in the absence of foregrounds

Optimization of focal plane for μ anisotropies?



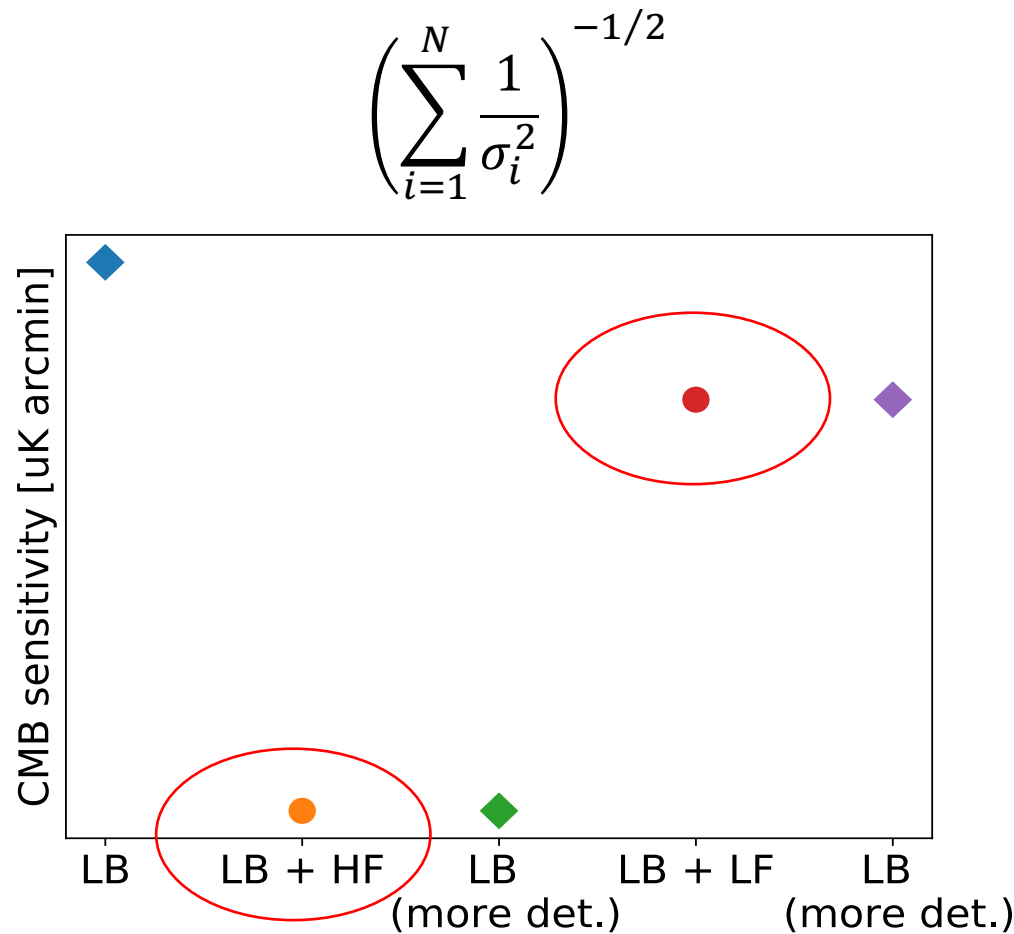
Sensitivity to **non-achromatic μ -distortion signal:**

$$\sigma = \left(\sum_{i=1}^N \frac{\left(a_i^{(\mu)} \right)^2}{\sigma_i^2} \right)^{-1/2}$$

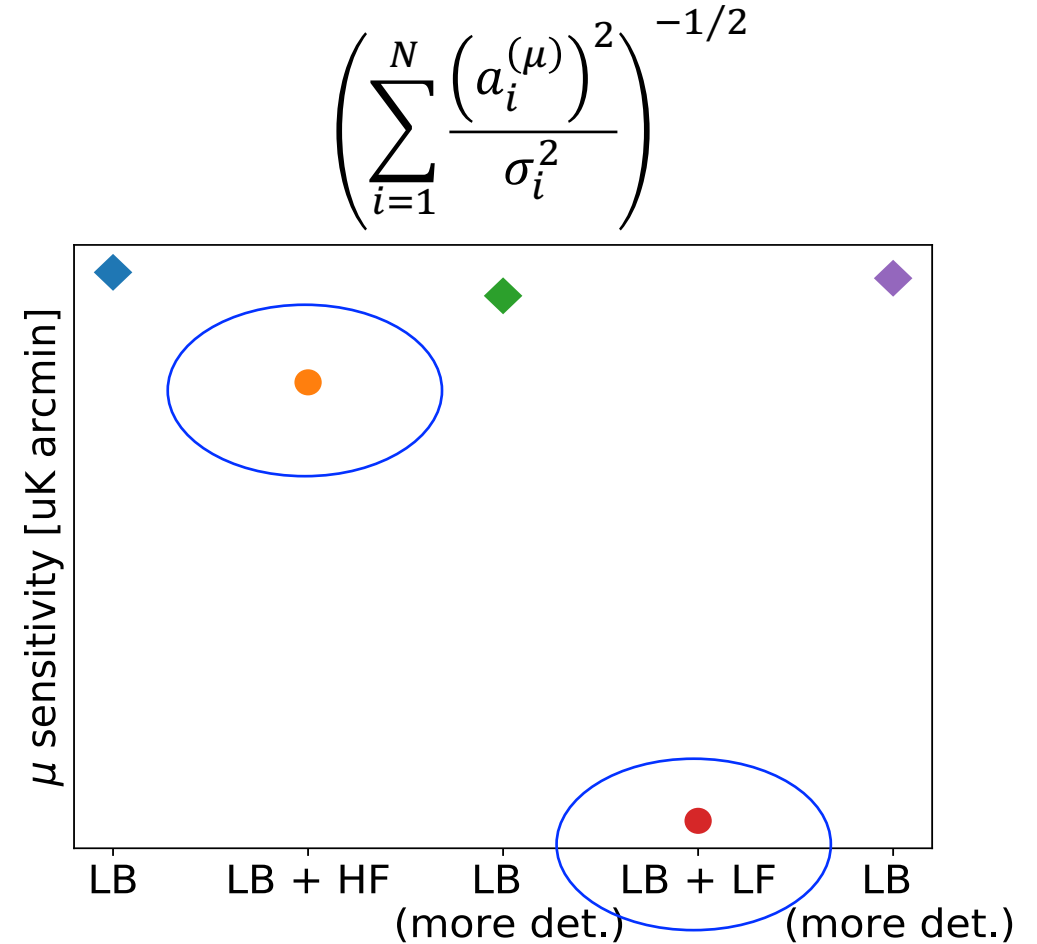
extra weighting by the μ SED

Equivalently, ILC noise for μ in the absence of foregrounds

Optimization of focal plane for μ anisotropies?

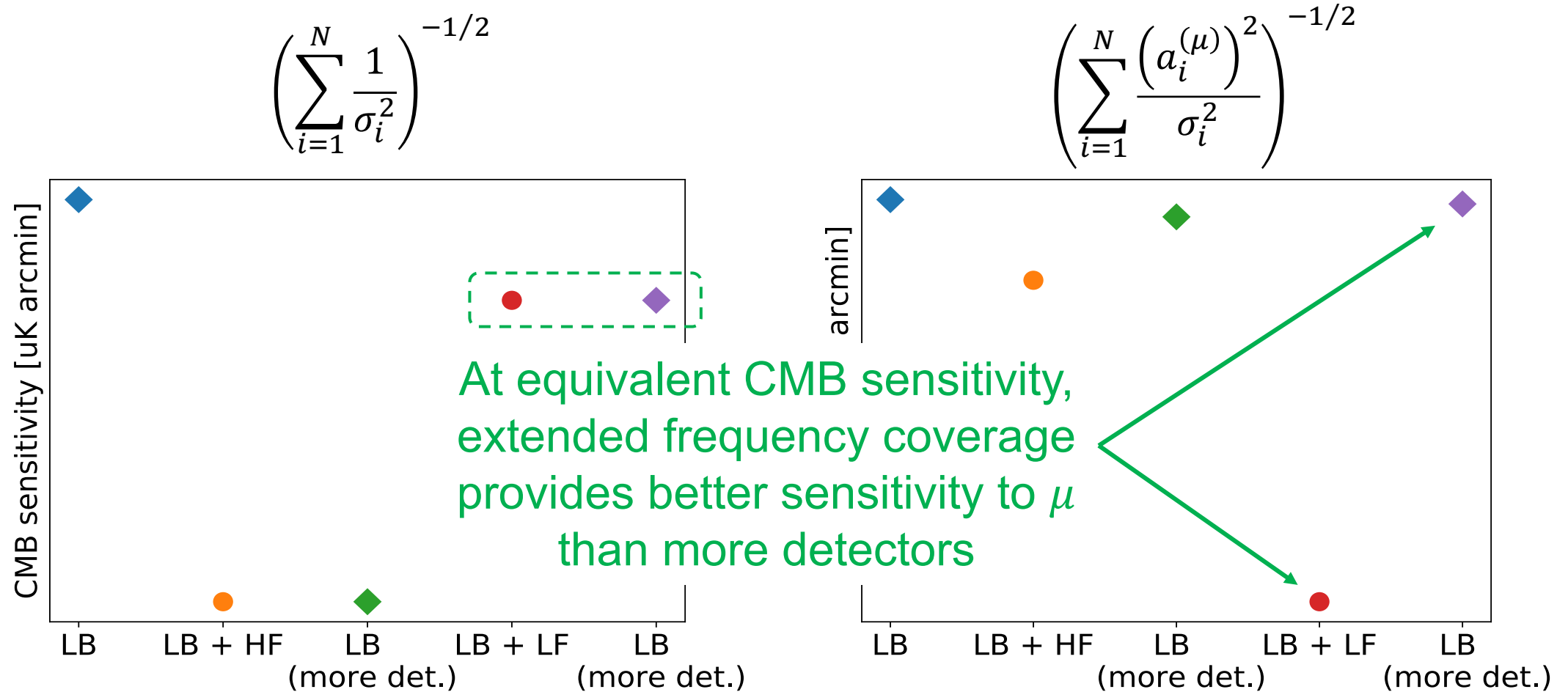


High frequencies better for CMB



Low frequencies better for μ

Optimization of focal plane for μ anisotropies?



High frequencies better for CMB

Low frequencies better for μ

Takeaway

- ❑ The Constrained ILC method enables to recover μT and μE correlation signals without bias
- ❑ Foregrounds degrade LiteBIRD sensitivity to $f_{\text{NL}}^{\mu}(k \simeq 740 \text{ Mpc}^{-1})$ by a factor of ten
- ❑ *LiteBIRD* detection limit $\sigma(f_{\text{NL}}^{\mu} = 0) \lesssim 800$ from joint μT , μE analysis after foreground cleaning
- ❑ μE correlations provide more constraining power than μT correlations on f_{NL}^{μ}
 - Because the degree of correlation between μ and E is larger than that between μ and T
 - Because foregrounds are less complex in polarization than in intensity
 - Because the CMB E -mode is immune from μ -distortion anisotropies
- ❑ In contrast to CMB anisotropies, μ -distortion anisotropies would get better sensitivity by adding low frequencies to LiteBIRD than adding high frequencies
- ❑ Extended frequency coverage provides more leverage than increased detector sensitivity